

# Heterogeneous Occupational Supply Elasticities and Changes in Labour Demand \*

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## Abstract

We propose a theoretically founded and interpretable measure of labour supply elasticities across occupations that can be implemented using observed transition rates. We use these to study the heterogeneous impact of demand shifts in Germany during the past decades within an equilibrium model. Employment growth per unit of wage growth is twice as large for occupations ex-ante classified as relatively elastic compared to inelastic occupations. We find that cross-occupation effects, capturing the role of wage changes in close substitute occupations, are particularly important in explaining employment growth heterogeneity. We validate the estimated elasticities with external correlates, including occupational licensing and task distance. The model explains substantially more of the occupational changes during 1985–2010 than an approach with homogeneous labour supplies.

**JEL Classification:** J21, J24, J31

**Keywords:** Labour Supply Elasticities, Heterogeneity, Occupational Similarity, Occupational Changes

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# 1 Introduction

Today it is well-established that sustained shifts in the demand for occupations have led to large changes in employment and wages, with many economic and societal consequences.<sup>1</sup> These shifts in demand have been attributed to a variety of sources, including changes to patterns of trade (see e.g. [Autor et al., 2013](#)), to households' consumption of goods ([Mazzolari & Ragusa, 2013](#)) and to technology ([Dauth et al., 2021](#); [Acemoglu & Restrepo, 2022](#)). In adapting to these shifts, a key concern for policy makers is the responsiveness of labour supply: While meeting an increased demand for some occupations may be straightforward, supplying workers in other occupations may be much harder. Equally, workers may reallocate from some occupations in decline more easily than from others. Indeed, research has found that the reallocation and supply of labour across sectors is heterogeneous (e.g. [Cortes, 2016](#); [Caliendo et al., 2019](#)). The aim of this paper is to characterise the role of this labour supply heterogeneity in explaining the evolution of employment and wages over recent decades.

This paper's main contributions are as follows. (i) We develop a tractable equilibrium model of the labour market that captures heterogeneity in supplies across occupations in a simple yet flexible way. These labour supply functions account for variable substitutabilities across occupations, which induce heterogeneous occupational spillovers to shocks. An important feature of the model is that the labour supply elasticities can be estimated directly from patterns of worker flows. (ii) We document the empirical relevance of the estimated elasticities, displaying their distribution, their relationship to existing metrics used in the literature and, accordingly, their potential for future application. (iii) Using the German labour market as a laboratory, we show that the resulting heterogeneous supplies are quantitatively important for explaining the evolution of occupational employment and wages. In particular, we find a key role for the joint distribution of substitutabilities with observed demand shifts. (iv) In a related way, we show that neglecting the resulting heterogeneous spillovers leads to a substantial *understatement* of the response of occupational employment to wage changes, as studied in, for example, [Mishel et al. \(2013\)](#) and [Hsieh et al. \(2019\)](#).

As such, we contribute to an extensive literature which has sought to provide a rich characterisation of the distribution of labour market changes, most notably including job 'polarisation'.<sup>2</sup> Moving forward, our results are important for understanding the likely

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<sup>1</sup>[Acemoglu & Autor \(2011\)](#) provide a comprehensive analysis of the evidence on the labour market over several decades (see also [Autor, 2019](#)). For recent analyses of societal consequences beyond the labour market, see, among others, [Autor et al. \(2020\)](#) on political polarisation, [Adda & Fawaz \(2020\)](#) on health, and [Keller & Utar \(2022\)](#) on family structure.

<sup>2</sup>The literature characterising labour market polarisation is extensive. See the discussion towards the end of this Introduction.

effect of ongoing changes to demand, such as through advanced automation (Felten et al., 2018; Brynjolfsson et al., 2018; Webb, 2020; Eloundou et al., 2023).

The supply side of our framework is based on a random utility model of workers' occupational preferences related to, among others, Cortes & Gallipoli (2018) and Card et al. (2018). In this model, the choices of occupation can be solved for as standard probability formulae which depend on wages in a destination occupation as well as pairwise occupational switching costs. We show that these probabilities, together with occupational employment shares, are sufficient statistics for the elasticity of each occupation's employment with respect to occupational prices. Given that transition probabilities vary substantially across occupations, the model provides an intuitive reason for why these supply elasticities vary. Generally, the framework is highly tractable and its mechanisms have intuitive economic interpretations, which we explore in detail.

As comes naturally out of the model, we distinguish between 'cross-price' elasticities, which capture the impact on employment of changes in the wage in a *different* occupation, and 'own-price' elasticities, which capture the impact of wage changes in the occupation itself. The model can then be used to theoretically assess the outcome of a set of wage changes across the whole economy. We decompose the predicted employment changes into those coming from own-occupation and *total* cross-occupation effects. The own-occupation effect is determined both by the own-price elasticity and the size of the wage change. Similarly, the total cross effect depends on the interaction of cross-price elasticities and outside wage changes: the resulting outcome depends subtly on whether close substitute occupations see wage increases or declines. We find that it is the spillovers resulting from this total cross-occupation effect which are of particular quantitative importance. The heterogeneous spillovers that arise are typically missing from related analyses, such as those relating to firm-level distortions in, for example, Card et al. (2018), Lamadon et al. (2022) and Berger et al. (2022).

We apply the model using data from Germany, which are uniquely suited for the purpose. In particular, we use the Sample of Integrated Employment Biographies (SIAB), which follows workers over their entire labour market careers for the years 1975–2010 and provides a consistent and fine-grained set of 120 occupations over this period. We estimate the supply elasticities using occupations' employment sizes and workers' transition flows over 1975–1984, in five-year rolling windows. These display substantial heterogeneity: Own-price elasticities vary by a factor of ten between the most elastic (e.g., Nursery teachers, Other occupations attending on guests) and the most inelastic (Physicians and pharmacists, Bank and building society specialists) occupations. A large part of this is how dispersedly they source employees. Lower employment elasticities are also related to occupations' certification requirements and regulations (taken from Vicari, 2014),

a larger share of university graduates, and higher average age.

Turning to the cross-price elasticities, we find that these are distributed approximately log-normally. As such, although most elasticities are close to zero, there exists a right tail of very similar occupation pairs, often within broader groups (such as Nursery teachers and Social work teachers, or Carpenters and Concrete workers), that lead to high elasticities of employment in one with respect to wage changes of the other. Overall, the cross-price elasticities are strongly correlated with task distances between occupations, measured as in [Gathmann & Schönberg \(2010\)](#); [Cortes & Gallipoli \(2018\)](#). Our empirical measure, however, improves on task distance by having a cardinal quantitative interpretation.

We then use the estimated elasticities to examine wage and employment changes over 1985–2010. To explore mechanisms and aid intuition, we first apply the model on the supply side of the labour market only. We begin by documenting a striking relationship between occupations’ own-price elasticity and ex-post outcomes: as would be expected, more elastic occupations display significantly higher employment growth per unit of wage growth than do less elastic occupations. We then examine the full effect of labour supply heterogeneities on employment in a simple regression specification. Both own-occupation and, particularly, cross-occupation effects are important in explaining the observed patterns of employment changes. Using model R-squared as a simple metric, we find that the explanatory power for employment changes is 33% higher than in standard specifications with homogeneous labour supplies only. By relaxing a key restriction in this regression, we also implement a simple test of the model, which is clearly passed.

Of particular note, these results highlight the importance of allowing for cross-occupation effects in this type of analysis. Because substitutable occupations experience similar wage shocks, omitting cross effects gives a misleading impression of the effect of wages on occupational employment. Specifically, the simple relationships analysed by e.g. [Autor et al. \(2008\)](#); [Mishel et al. \(2013\)](#); [Hsieh et al. \(2019\)](#); [Böhm et al. \(2024\)](#) *understate* the ceteris-paribus response of employment to sectoral wage changes by over 50%. This omitted variable result relates to the similar point made by [Borusyak et al. \(2022\)](#) on the responsiveness to wage shocks of migrants’ location.

To analyse labour market equilibrium, we add the demand side to the model using CES aggregation of occupational outputs. In terms of the theory, we find that the effect of shocks on both sides of the market can be expressed in compact form, featuring a single additional matrix which captures how shocks to *either* demand or supply dissipate across the labour market heterogeneously. Importantly, in terms of empirics, the model also points directly to a strategy to isolate demand shocks with instrumental variables.

Following the literature on routine-biased technical change (see e.g., [Autor et al., 2003](#), among many others), we base our instruments on occupations' average task content in the late 1970s and early 1980s. We then interact this with the predicted effects that it has depending on the different supply elasticities. These instruments are strong and, as we show in detail, yield similar conclusions to those from the pure supply-side analysis.

We use the equilibrium model to extract the effects of supply heterogeneity from underlying shocks in decomposition and counterfactual analyses. In terms of the shocks, we show that those on the demand side have been substantially more important than supply shocks over the period we study. This feature largely explains why our analysis of the supply side provides insight on its own. Quantitatively, the effect of labour supply heterogeneity in response to demand shocks is equally important for changing occupational wages and employment as are the supply shocks by themselves.<sup>3</sup> Spillovers resulting from the interaction between cross-price elasticities and demand shocks again play a critical role in these changes, leading to heterogeneous outcomes for specific occupations and reducing the effective *level* of occupational labour supply in the economy.

This paper contributes to the analysis of occupational changes. A large body of research has studied whether and what kinds of demand shocks have worked on the occupation and task structures, and what effects this has had on wages and employment (notably job polarisation).<sup>4</sup> We advance this literature by highlighting that a fundamental catalyst of such changes is the flexibility of labour supply to react to them. These results inform a broader debate about how the labour market will generate the jobs of the future. [Autor et al. \(2023\)](#) discuss how institutions and policies may be designed to (re-)train workers in the skills that are needed. [Autor et al. \(2022\)](#) show how new occupations and job types emerge from labour-augmenting and automating innovations. We complement this agenda by studying the ability to shift employment among the existing set of occupations and skills. While our empirical application is oriented around changes to technology, the framework could equally be applied to other demand-side changes.

Our theory extends standard models of sector choice by allowing for variation in the costs to transition between occupation pairs. [Cortes & Gallipoli \(2018\)](#) is a notable precursor. We show that this leads to heterogeneity of labour supply elasticities being identified directly from job flow data.<sup>5</sup> We then highlight the role of the substitutability between the sectors that workers choose from as driving these elasticities. In this sense, and with the

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<sup>3</sup>In particular, on top of demand shocks, supply heterogeneity and supply shocks each explain about 20% of the variation in occupational employment.

<sup>4</sup>See, e.g., [Spitz-Oener \(2006\)](#); [Autor et al. \(2008\)](#); [Acemoglu & Autor \(2011\)](#); [Autor & Dorn \(2013\)](#); [Autor et al. \(2013\)](#); [Goos et al. \(2014\)](#); [Deming \(2017\)](#); [Bárány & Siegel \(2018\)](#) in addition to the papers cited above.

<sup>5</sup>Alternatively, e.g., [Bhalotra et al. \(2022\)](#) exploit the full set of women and men's employment and wages across broad occupation task groups for equilibrium identification.

resulting importance of cross-occupation effects, the analysis complements research that focuses on employer size to generate heterogeneity in own-wage labour supply elasticities or market power (Berger et al., 2022; Jarosch et al., 2019).

More generally, we complement a micro-economic research agenda on the labour-supply-side substitutability between occupations. A series of studies have provided advice to job seekers about which alternative but related occupations to their previous employment they should search in (e.g., Belot et al., 2019, 2022; Altmann et al., 2022). Gathmann & Schönberg (2010) analyse the importance of task distance and Eckardt (2023) the specificity of training for the costs of switching occupations. Borusyak et al. (2022) highlight the econometric issues that arise in migration regressions when not taking into account the correlation of shocks to workers' current and substitutable region-industries. We formalise the mechanisms that may underpin such relationships between occupations or sectors, and then study their role for more aggregate wage and employment outcomes.

The remaining sections of the paper are as follows. In Section 2, we present a static partial equilibrium model with perfect information that provides a tractable framework for labour mobility decisions under frictions. In Section 3, we discuss the data and describe the components of the estimated own- and cross-price elasticities of occupations' labour supply. Section 4 presents our estimates of own- and cross-occupation effects. In Section 5, we add the demand side to the model and study labour market equilibrium. Section 6 uses the equilibrium model to extract the effects of supply heterogeneity from demand and supply shocks in decomposition and counterfactual analyses. In Section 7, we extend the model to account for non-employment transitions and explore the robustness of our results by estimating the model separately by sub-period and employing an alternative measure for occupational wage growth. Section 8 concludes.

## 2 The Model of Labour Supply

We adopt a random utility model of worker preferences that characterises occupation-specific labour supply functions. This builds on Cortes & Gallipoli (2018) and Hsieh et al. (2019), who adapt the environment in Eaton & Kortum (2002) to occupational choices, and Card et al. (2018) who study the selection of workers into firms. In this section, we present a static partial equilibrium model with perfect information, providing a tractable framework for labour mobility decisions under frictions. Labour demand and market equilibrium are modelled in Section 5.

## 2.1 Environment

There is a continuum of workers  $\omega \in \Omega$  and a finite set of  $N$  occupations. The number of employers in each occupation is large, such that labour demand is competitive and there is no strategic wage setting. Every worker is initially and predeterminedly assigned to an occupation  $i$ . Workers subsequently choose occupations to maximise their utility, which can be interpreted as a total lifetime payoff and is occupation-combination as well as individual-specific. It includes wages as pecuniary benefits, a specific cost of switching between occupations  $i$  and  $j$ , and an idiosyncratic preference for working in occupation  $j$ .

The indirect utility of worker  $\omega$  with initial occupation  $i$  choosing occupation  $j$  is given by:

$$u_{ij}(\omega) = \theta p_j + a_{ij} + \varepsilon_j(\omega) \quad (1)$$

where  $\theta p_j$  is the general pecuniary payoff to occupation  $j$ . The component  $p_j$  can be interpreted as the log occupational price or wage rate offered to all workers per unit of their skill (we will later simplify our language and refer to this as ‘price’) and  $\theta$  as their pecuniary preference or ‘wage elasticity’ parameter.

The occupation–combination-specific term  $a_{ij}$  summarises potential pecuniary and non-pecuniary costs of selecting occupation  $j$  for individuals initially assigned to occupation  $i$ . These can include lower payoffs as switchers may need to learn new tasks in  $j$  or institutional barriers. [Gathmann & Schönberg \(2010\)](#) and [Cortes & Gallipoli \(2018\)](#) analyse these costs explicitly – we further discuss this in Section 3 – while we let them flexibly affect the labour supply functions that we are after.

The final summand  $\varepsilon_j(\omega)$  is an idiosyncratic preference shock for working in occupation  $j$ , which may, for example, include non-pecuniary match components with occupation-specific amenities or types of coworkers. We assume  $\varepsilon_j(\omega)$  is independently drawn from a type I extreme value (i.e., Gumbel) distribution.<sup>6</sup> Draws, including for the current occupation, occur at the beginning of the period. Based on realised shocks, switching costs, and log occupational prices, workers decide whether to stay in their occupation or switch to a different one.

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<sup>6</sup>Gumbel location  $\mu$  and scale  $\delta$  are general because equation (1) can always be recast as  $u_{ij}(\omega) = \frac{\theta}{\delta} p_j + \frac{a_{ij}}{\delta} + \frac{\varepsilon_j(\omega) - \mu}{\delta}$ , yielding the same choice probabilities (see [Card et al., 2018](#)). In that sense,  $\theta$  can be thought of as scaling the importance of wages relative to idiosyncratic shocks.

## 2.2 Occupational Choice and Price Elasticities

By standard arguments (McFadden, 1973), the assumptions on eq. (1) imply that workers' occupational choice probabilities are of the form:

$$\pi_{ij}(\mathbf{p}) = \frac{\exp(\theta p_j + a_{ij})}{\sum_{k=1}^N \exp(\theta p_k + a_{ik})}, \quad (2)$$

where  $\mathbf{p}$  is the vector of  $N$  log occupational prices. We follow the convention that, by the law of large numbers,  $\pi_{ij}$  is the fraction of workers switching from occupation  $i$  to  $j$ . Choice probabilities are occupation–combination-specific and they may involve staying in the current occupation ( $i = j$ ). Intuitively, eq. (2) says the more attractive occupation  $j$  is relative to all other occupations, and the lower the cost of switching to it from  $i$ , the higher will be the fraction of workers who will move to that occupation. Since they are aggregated over idiosyncratic shocks, the probabilities are not individual-specific and we can omit the index  $\omega$  from now on.

Let  $\tau_i$  denote the share of the working population originating in occupation  $i$ , such that  $\sum_i \tau_i = 1$ . One can think of  $\{\tau_i\}$  as the stationary distribution of employment in a baseline period. Further, let  $E_j(\mathbf{p})$  be the fraction ending up working in occupation  $j$  as a function of log occupational prices. This implies

$$\begin{aligned} E_j(\mathbf{p}) &= \sum_i \tau_i \pi_{ij}(\mathbf{p}) \\ &= \tau_j \text{ if } \mathbf{p} = \mathbf{p}^* \end{aligned} \quad (3)$$

with  $\mathbf{p}^*$  the vector of baseline log occupational prices. From now, we simplify our language by using 'prices' to mean log occupational prices as described in eq. (1).

### 2.2.1 Effect of Individual Price Changes

Our interest centres on (own- and cross-occupation) price elasticities, that is, the elasticity of occupation  $j$ 's employment with respect to any occupation  $k$ 's price (including  $k = j$ ). Writing  $e_j \equiv \ln E_j(\mathbf{p})$ , and differentiating eq. (3), we obtain:

**Remark 1 (Elasticities and Job Flows)** *The short-term partial derivative of occupation  $j$ 's log employment share with respect to  $k$ 's log price is equal to:*

$$\frac{\partial e_j(\mathbf{p})}{\partial p_k} = \theta d_{jk} \quad (4)$$



with

$$d_{jk} = \begin{cases} \frac{\sum_i \tau_i (\pi_{ij}(1-\pi_{ij}))}{\tau_j} & \text{if } j = k \\ -\frac{\sum_i \tau_i (\pi_{ij}\pi_{ik})}{\tau_j} & \text{otherwise} \end{cases} \quad (5)$$

Appendix A.1 contains the derivation.

Equation (4) shows how these price elasticities can be computed using transition probabilities (as we discuss in the next section, the transition probabilities have direct analogues in the data as job flows), baseline employment shares, and an unobserved pecuniary parameter  $\theta$ . We return to the estimation of  $\theta$  in Section 4. We now focus our attention on eq. (5).

Element  $d_{jk}$  in eq. (5) can be thought of as a constituent of an  $N \times N$  matrix of price elasticities, which we also refer to as ‘elasticity matrix’ or ‘matrix  $D$ ’ throughout the paper. With a slight abuse of notation, we thus refer to elements  $d_{jj}$  and  $d_{jk}$  as own- and cross-price elasticities, respectively.<sup>7</sup> To gauge the empirical content of Remark 1 further, we derive alternative formulations of these elasticities more explicitly in terms of moments of job flows. This provides further intuition on what determines the elasticities as well as metrics to compare to other related measures used in the literature.

To do this, we define some additional terms. First, and as standard, let  $\mathbb{E}_\tau x \equiv \sum \tau_i x_i$  be the average of vector elements  $x_i$  weighted by the stationary employment distribution  $\{\tau_i\}$ . Then define  $\tilde{\pi}_{iq} \equiv \frac{\pi_{iq}}{\tau_q}$ , such that  $\tilde{\pi}_{iq}$  gives normalised job flows, with  $\mathbb{E}_\tau \tilde{\pi}_{iq} = 1$ . Normalising the transition probabilities in this way yields moments that are invariant to occupation size. In this spirit, and in parallel, let  $Cov_\tau(x, y) \equiv \sum \tau_i (x_i - \mathbb{E}_\tau x)(y_i - \mathbb{E}_\tau y)$ . This leads us to the following result:

**Remark 2 (Individual Cross-Price Elasticities)** For all  $j \neq k$ , the off-diagonal elements of matrix  $D$  can be expressed as:

$$-d_{jk} = \underbrace{\tau_k}_{\text{occupational importance}} \times \underbrace{Cov_\tau(\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})}_{\text{occupational similarity}} + \underbrace{\tau_k}_{\text{price index}} \quad (6)$$

where we examine the negative of  $d_{jk}$ , rather than  $d_{jk}$  itself, so that we can interpret higher elasticities by larger positive numbers. Appendix A.1 contains the derivation.

Expression (6) above consists of two additive components. First is a substitutability component  $\tau_k Cov_\tau(\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})$ . It consists of an ‘occupational-similarity’ term that is symmetric between  $j$  and  $k$ , is invariant to the fineness of the occupational classification, and captures the pure similarity of occupation in-flows: If  $Cov_\tau(\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k}) > 0$ , then occupa-

<sup>7</sup>Strictly speaking, these elements should be multiplied by  $\theta$  as shown in eq. (4).

tions  $j$  and  $k$  are ‘competing’ for workers and the cross-price elasticity (i.e., the responsiveness of employment in occupation  $j$  to changes in the price of occupation  $k$ ) will be higher. This occupational similarity term is then weighted by an ‘occupational-importance’ term  $\tau_k$  that depends on the size of the occupation of the price change: Price increases in a smaller competing occupation will have smaller percentage ripple effects than price increases in a larger occupation. Second is an occupation-specific intercept which captures occupation  $k$ ’s contribution to a price index and which, in terms of variability across occupations, turns out to be quantitatively relatively unimportant.

Likewise, we can reformulate the on-diagonal elements of the elasticity matrix  $D$ , which capture the own-price elasticities. This leads us to the following result:

**Remark 3 (Individual Own-Price Elasticities)** *For all  $j = k$ , the on-diagonal elements of  $D$  can be expressed as:*

$$d_{jj} = \underbrace{\sum_{k \neq j} \tau_k \text{Cov}_\tau (\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})}_{\text{aggregate substitutability}} + \underbrace{1}_{\text{direct}} - \underbrace{\tau_j}_{\text{price index}} = \underbrace{-\tau_j \text{Var}_\tau (\tilde{\pi}_{.,j})}_{\text{job-flow dispersion}} + \underbrace{1}_{\text{direct}} - \underbrace{\tau_j}_{\text{price index}} \quad (7)$$

where  $\text{Var}_\tau (x) \equiv \sum \tau_i (x_i - \mathbb{E}_\tau x)^2$ . Appendix A.1 contains the derivation.

Expression (7) captures the effect of an isolated change in occupation  $j$ ’s own price and has a similar structure to expression (6), though in this case it can be constructively formulated in two ways, each of which provides informative interpretations. The first formulation includes an ‘aggregate substitutability’ term, that sums substitutability components from all other occupations. This term captures the fact that a unit increase in the price of occupation  $j$  is equivalent to an equal and opposite price decline in all other occupations. It is in this sense that the own-price elasticity captures aggregate substitutability with other occupations.

In the second formulation, on the right-hand side of expression (7), the term  $\tau_j \text{Var}_\tau (\tilde{\pi}_{.,j})$  can be interpreted as a ‘job-flow dispersion’ term, reflecting how dispersed or concentrated are the inflows to occupation  $j$ : Sectors hiring from a diversity of sources (in this case, a *small*  $\text{Var}_\tau (\tilde{\pi}_{.,j})$ ) are more elastic. Following this line of thought, it is useful to consider that inflows are typically concentrated if the diagonal element of the transition matrix is close to 1 (meaning everyone remains in the current occupation) and the off-diagonal elements are close to 0. In this case,  $\text{Var}_\tau (\tilde{\pi}_{.,j})$  is large, the job-flow dispersion component is more negative, and  $d_{jj}$  is lower, indicating a lower own-price elasticity. Finally, in both formulations are ‘direct’ and price-index effects. As in the discussion following Remark 2, these terms contribute to the *level* of the elasticity, but little to the observed

variability.

Remarks 2 and 3 show that we can express the price elasticities in terms of simple moments of the distribution of job flows. Before moving on, it is worth commenting that in eq. (6) we conceptually separate  $Cov_{\tau}(\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})$  from  $\tau_k$  in the first summand, while in eq. (7) we interpret  $\tau_j Var_{\tau}(\tilde{\pi}_{.,j})$  jointly. We formulate the expressions in this way because it is  $Cov_{\tau}(\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})$  and  $\tau_j Var_{\tau}(\tilde{\pi}_{.,j})$  (rather than  $Var_{\tau}(\tilde{\pi}_{.,j})$ ) which are invariant to the fineness of the occupational classification. We discuss this point further in Appendix A.1 using both empirical evidence and theoretical justification.

### 2.2.2 Effect of Multiple Price Changes

We now generalise the formulation given in eq. (4). The response of the vector of employment shares to a change in the vector of prices can be approximated by:

$$\Delta \mathbf{e} \approx \frac{\nabla \mathbf{e}}{\nabla \mathbf{p}} \Delta \mathbf{p} = \theta D \Delta \mathbf{p} \quad (8)$$

with  $\Delta \mathbf{e}$  representing the change of the  $N \times 1$  vector of log employment shares,  $\{e_j\}$ , and  $\frac{\nabla \mathbf{e}}{\nabla \mathbf{p}}$  the  $N \times N$  matrix of partial derivatives  $\frac{\partial e_j(\mathbf{p})}{\partial p_k} \forall j, k$ . Given some demand-side shock and ensuing shock to prices, which we discuss below, the change to employment shares can be approximated by eq. (8). This approximation is exact for marginal changes in prices.

Equation (8) shows how the model traces out a supply curve vector,  $\mathbf{e}(\mathbf{p})$ , of log employment shares. With a view to our empirical application, we rewrite the inner product of elasticity matrix  $D$  with the vector of price changes as follows:

$$\begin{aligned} \Delta e_j &\approx \theta \mathbf{d}_j \Delta \mathbf{p} \\ &= \theta \left( \underbrace{d_{jj} \Delta p_j}_{\text{own-occupation effect}} + \underbrace{\sum_{k \neq j} d_{jk} \Delta p_k}_{\text{total cross-occupation effect}} \right), \end{aligned} \quad (9)$$

where  $\mathbf{d}_j$  is the  $j$ th row of matrix  $D$ , and, in the bottom line, we separate the effects of on-diagonal elements in  $D$  from those of all off-diagonal elements. To summarise the intuition, the own-occupation effect in eq. (9) represents the part of occupations' employment changes that are due to their own price changing. The total cross-occupation effect captures the effect of heterogeneity in price changes across all other occupations: Intuitively, large price changes in occupations that are very substitutable with  $j$  (i.e.,  $d_{jk} \ll 0$ ) will have potentially important spillovers on  $j$ 's employment share. We provide additional

formal details in Appendix [A.2](#).

The thought experiment we imagine is that the economy is hit by a sudden change in the technology of final goods production, which shifts demands for the different occupations' labour inputs either to the right (an increase) or to the left (a decrease).<sup>8</sup> This leads to a new set of equilibrium prices  $\{p_j\}$  and quantities  $\{e_j\}$  in all occupations. In the absence of supply shocks (eq. (9)), these price changes are sufficient statistics for the implied changes in demand – we consider this case in Section 4. In the presence of supply shocks ( $\Delta \mathbf{e} \approx \theta D \Delta \mathbf{p} + \Delta \mathbf{s}$ ), the equilibrium model presented in Section 5 provides an identification framework which can be implemented with appropriate instruments.

### 3 Data and the Elasticity Matrix

This section presents our data sources. We then describe the components of the estimated own- and cross-price elasticities of occupations' labour supply, also relating them to other established measures in the literature.

#### 3.1 Data Sources

Our first objective is to analyse the elasticity components and to estimate the labour supply curves given by eq. (9). To take the model to the data, we use the Sample of Integrated Labour Market Biographies (SIAB, [Frodermann et al., 2021](#)), a 2% sample of administrative social security records in Germany since 1975. The SIAB data contains complete employment histories and wage information for more than one million employees. This dataset is representative of all individuals covered by the social insurance system, roughly 80% of the German workforce. It excludes self-employed, civil servants, and individuals performing military service.

The SIAB data have been used in various prior studies of the labour market and are well-suited for our purpose. First, the panel dimension allows us to measure worker flows over long frequencies. The administrative nature ensures that we observe the exact date of a job change and the wage associated with each job. Second, occupation codes are consistently coded from 1975 to 2010 ( $N = 120$  occupations). Since employers are legally required to report the kind of job their employees perform, miscoding of occupations is less likely than in the case of survey-based data collection. Finally, the wage information

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<sup>8</sup>The instrumental variables strategy in Section 5 will exploit occupations' initial task contents at the beginning of our analysis period as proxies for subsequent demand shocks. More generally, forces of occupational demand may include, among others, task-biased technological change and automation (e.g., [Acemoglu & Autor, 2011](#); [Acemoglu & Restrepo, 2022](#)), international trade and offshoring ([Autor et al., 2013](#); [Goos et al., 2014](#)), transformation of the industry structure ([Bárány & Siegel, 2018](#)), changes in consumption patterns ([Autor & Dorn, 2013](#); [Mazzolari & Ragusa, 2013](#)), or social skills content ([Deming, 2017](#)).

is highly reliable. The SIAB is based on process data used to calculate retirement pensions and unemployment insurance benefits, so misreporting is subject to severe penalties.

We restrict the main sample of analysis to men aged 25–59 who are working full-time (excluding apprentices and always-foreigners) in West Germany.<sup>9</sup> We further drop spells of workers with missing information on occupation or wage, and wages below the limit for which social security contributions have to be paid.<sup>10</sup> Following [Böhm et al. \(2024\)](#), we transform the daily spell structure of the SIAB into a yearly panel by using the longest spell in a given year. Our final sample consists of approximately 600,000 unique individuals and 9 million individual  $\times$  year observations for the whole period 1975–2010.

Importantly, the SIAB data allows us to compute worker flows (sufficient statistics for the elements of  $D$ ), changes in occupational employment ( $\Delta e$ ), as well as changes in occupational prices ( $\Delta p$ ). For the latter, we follow the literature on this, which emphasises that raw wages need to be selection-corrected ([Cavaglia & Etheridge, 2020](#); [Böhm et al., 2024](#)), and use occupation stayers' (i.e., workers who do not switch occupation from one year to the next) wage changes as the main estimate of changes in occupational prices. We show the robustness of our results using an alternative price estimation procedure following [Cortes \(2016\)](#) that corrects for worker–occupation–spell fixed effects in Section 7. The SIAB data also provides us with other occupational characteristics (e.g., workers' mean age by occupation, the share of workers with university degree by occupation) that we use to relate to our elasticity measures.

To obtain task information in occupations, we use the Qualifications and Career Surveys (QCS, [Hall et al., 2012](#)). The QCS consist of cross-sectional surveys with 20,000–35,000 individuals in each wave. Respondents report on the tasks performed in their occupations, and we categorise them into analytical, routine, and manual tasks, assigning values based on response frequency. By averaging responses from pooled QCS data in 1979 and 1985/1986, we compute task intensities among those three categories by occupation, which we also use to construct a measure of task distance between occupations following [Gathmann & Schönberg \(2010\)](#) and [Cortes & Gallipoli \(2018\)](#). We study how these relate to our elasticity measures below. In Section 5, we use task measures to proxy for demand changes across occupations between 1985–2010. Finally, to obtain measures of occupational licensing, we use the indicators for standardised certification and degree of regulation developed by [Vicari \(2014\)](#).

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<sup>9</sup>Excluding East Germans allows us to define a consistent sample during the whole 1975–2010. We also remove women and individuals who are always foreigners as these groups have experienced some strong and potentially confounding changes during this period (rapidly rising education and employment rates, declining workplace discrimination, changing norms; see e.g. [Hsieh et al., 2019](#); [Boelmann et al., 2023](#)).

<sup>10</sup>In preparing the data, we impute censored wages above the upper earnings threshold for social security contributions ([Dustmann et al., 2009](#); [Card et al., 2013](#)) and correct for the wage break in 1983–1984 ([Fitzenberger, 1999](#); [Dustmann et al., 2009](#)). See Appendix B for all the details.

We report summary statistics for the 120 occupations in Appendix [Table B.1](#). This shows that cross-sectional variation of employment is substantial, with occupations at the 10th percentile shrinking by 1.8 log points annually (averaged over the period 1985–2010) while growing by 2.4 log points annually at the 90th percentile (see also [Figure 2](#) below). The annualised wage growth of occupation stayers is positive at 0.59 log points, again with considerable dispersion around this average. Similar variation is found for our alternative measure of occupational prices à la [Cortes \(2016\)](#). Using five-year sub-periods, we also show that there is large variation in employment and wage growth over time which is, for example, slower in the economically sluggish early 2000s. More details on the data, variable construction, and descriptive statistics are presented in Appendix [B](#).

### 3.2 The Elasticity Matrix

As shown in [Remark 1](#), a strength of the elasticity matrix implied by the theory is that it can be computed directly from baseline worker flows. We construct transition rates across all occupation pairs for individuals who are observed at the endpoints of five-year periods within 1975–1984. The flow of switchers from origin occupation  $i$  to destination occupation  $j$  (which includes staying in occupation  $i$ ) is defined as the number of individuals who are employed in occupation  $i$  in year  $t$  and employed in occupation  $j$  in year  $t + 5$ . Dividing each element by total flows from origin occupation  $i$  we obtain the transition probability matrix  $\Pi$ , which is of size  $120 \times 120$ , and element  $\pi_{ij}$  represents the empirical probability that a worker employed in origin occupation  $i$  switches to  $j$  in five years' time. The transition probability matrix also implies a steady state vector  $\tau$  of size  $120 \times 1$ , with element  $\tau_i$  representing occupation  $i$ 's size as a share of total employment. With that, we compute the elasticity matrix  $D$  following eq. (5).<sup>11</sup>

Panel A of [Table 1](#) reports occupations at different quantiles of the own-price elasticities  $d_{jj}$  (the full list for the 120 occupations is in Appendix [Table B.5](#)). These range from 0.07 among physicians and pharmacists to 0.80 among personnel in social, medical, and gastronomy service occupations. [Figure 1a](#) correlates the key component of own-price elasticities, 'aggregate substitutability', with education, age, task content, and occupational requirements.<sup>12</sup> For the latter, we use the indicators for standardised certification

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<sup>11</sup>The baseline period (1975–1984) sample consists of 252,309 individuals and 1,794,286 individual  $\times$  year observations. Our findings remain consistent whether we use two-year or ten-year period lengths for the flows. The resulting analysis period 1985–2010 is similar to [Card et al. \(2013\)](#) and [Böhm et al. \(2024\)](#). Appendix [Table B.3](#) summarises the transition probability matrix  $\Pi$  and the elasticity matrix  $D$ .

<sup>12</sup>As discussed in relation to [Remark 3](#), aggregate substitutability is the key component of own-price elasticities, dominating the price index component. Appendix [B.3](#) reports the variation in the two. As such, the relationship of the own-price elasticity with external characteristics is almost the same as that of its substitutability component (Appendix [Figure B.1](#)).

and degree of regulation developed by [Vicari \(2014\)](#).<sup>13</sup> [Figure 1a](#) shows that occupations with a higher degree share, more analytical tasks, and higher regulation and certification requirements are less substitutable and by extension less own-price elastic. Together, the table and figure also suggest that occupations which are more sensitive to wages are easier to enter and have less specialised workforces (consistent with [Cortes & Gallipoli, 2018](#)), and that occupational licensing can have significant negative effects on worker labour market flows ([Kleiner & Xu, 2024](#)).<sup>14</sup>

Panel B of [Table 1](#) shows cross-price elasticities ( $-d_{jk}$ ) between occupation pairs. The highest spillovers of price changes on employment are naturally among related occupations: of ‘home wardens, social work teachers’ on ‘nursery teachers, child nurses’; of ‘non-medical practitioners, masseurs, physiotherapists’ on ‘medical receptionists’; and of ‘office specialists’ on ‘stenographers, shorthand typists, data typists’. While quantitatively these top pairs are within the range of the own-price elasticities, cross-price elasticities fall off quickly from the top and become an order of magnitude smaller than any own-price elasticities even at the 90th percentile.

[Figure 1b](#) plots the occupational similarity component of the cross-price elasticities against occupational task distance as in [Gathmann & Schönberg \(2010\)](#) and [Cortes & Gallipoli \(2018\)](#). Because it abstracts from the role of occupational importance, ‘occupational similarity’ is the fitting comparison to task distance as both are symmetric and size-independent. Occupational similarity is also the main driver of variation in cross-price elasticities, which are strongly skewed and approximately log-normally distributed.<sup>15</sup> [Figure 1b](#) illustrates the corresponding skewness of occupational similarities and a negative (and significant) relationship with measured task distance. In other words, the figure shows that the higher the distance in task content between two occupations, the lower the cross-price elasticity (i.e., lower ‘substitutability’ of these occupations). However, we note that task distance is based only on the set of tasks reported in survey responses and it explains at most a subset of occupational similarity, which in contrast contains all information implied by realised worker flows. This last point is underscored by the fact that task distance is essentially an ordinal variable whereas the skewness of occupational similarity and cross-elasticities has a natural quantitative interpretation. Accordingly, Spearman’s rank coefficient provides a better fit in [Figure 1b](#) than standard linear correlation.

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<sup>13</sup>The degree of regulation indicates whether legal and administrative regulations exist which bind the access to and practice of the occupation, including the necessity of holding a specific title as proof of competence. The occupational certification further includes whether access to exercising the professional activity is linked to a standardised training credential. See [Appendix B](#) for further details.

<sup>14</sup>[Abraham & Kearney \(2020\)](#) review the employment and wage effects of occupational licensing. [Eckardt \(2023\)](#) studies the effect of training specificity for the costs of switching occupations in Germany.

<sup>15</sup>A detailed analysis is in [Appendix B.3](#), which depicts the log of cross-price elasticities against the normal distribution and decomposes its variation into occupational similarities versus other factors following [Remark 2](#). We also plot the cross-price elasticities against occupational task distance directly.

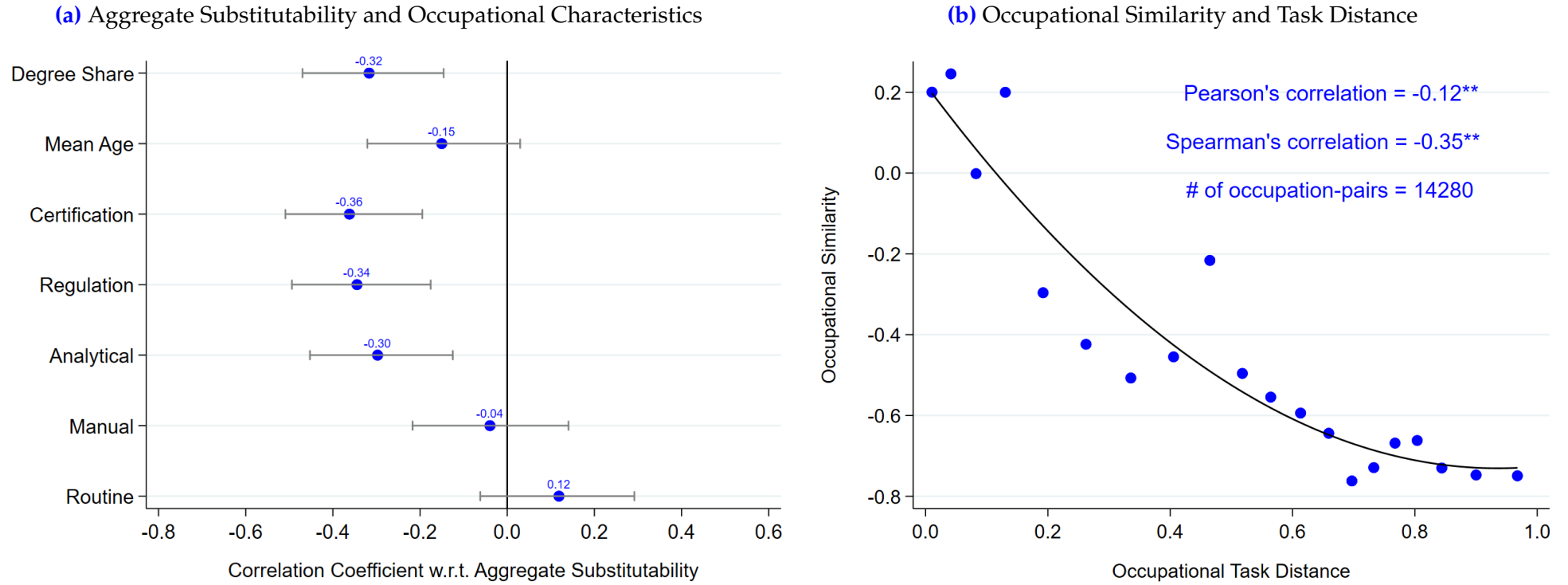
**Table 1:** Summary Statistics: Own- and Cross-Price Elasticities

<b>Panel A</b>	Own-price elasticity ( $d_{jj}$ )	Occupation
Minimum	0.074	Physicians, dentists, veterinary surgeons, pharmacists
10th percentile	0.294	Health or property insurance specialist
25th percentile	0.358	Members of parliament, association leaders, officials
50th percentile	0.430	Stucco workers, plasterers, rough casters, proofers
75th percentile	0.517	Sheet metal pressers, drawers, stampers, metal moulders
90th percentile	0.604	Salespersons
Third highest	0.740	Other attending on guests
Second highest	0.797	Medical receptionists
Maximum	0.798	Nursery teachers, child nurses
<b>Panel B</b>	Cross-price elasticity ( $-d_{jk}$ )	Occupation of price change ( $k$ ) → Occupation of employment change ( $j$ )
50th percentile	0.001	Paviours, road makers → Sheet metal workers
90th percentile	0.009	Miners, shaped brick/concrete block makers → Engine fitters
Fifth highest	0.144	Bricklayers, concrete workers → Carpenters, scaffolders
Fourth highest	0.182	Restaurant, inn, bar keepers, hotel and catering personnel → Other attending on guests
Third highest	0.185	Office specialists → Stenographers, shorthand typists, data typists
Second highest	0.253	Non-medical practitioners, masseurs, physiotherapists → Medical receptionists
Maximum	0.464	Home wardens, social work teachers → Nursery teachers, child nurses

Notes: Panel A shows statistics from a ranking of the 120 occupations of the 1988 Klassifikation der Berufe according to their own-price elasticity ( $d_{jj}$ ). Panel B comes from a ranking of the 14280 occupation pairs according to their cross-price elasticity. See text for more details.



**Figure 1:** Elasticity Components: Comparison with External Metrics



Notes: Panel (a) reports how the aggregate substitutability component of the own-price elasticity, namely  $\sum_{k \neq j} \tau_k Cov_{\tau}(\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})$ , correlates with skill requirements across 120 occupations. Occupational certification and regulations come from Vicari (2014). Task content (analytical, manual, and routine) are measured using BiBB, see Appendix B.2. Correlations weighted by initial employment in each occupation. Panel (b) shows the relationship (with a quadratic fit) between the occupational similarity component of the cross-price elasticity, namely  $Cov_{\tau}(\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})$ , and occupational task distance measured as in Cortes & Gallipoli (2018). Appendix Figure B.1 does the same plots for  $d_{jj}$  and  $-d_{jk}$  instead.

## 4 Estimates of Own- and Cross-Occupation Effects

This section presents our estimates of own- and cross-occupation effects. First, we study only bivariate relationships of occupations’ changing prices with their employment. Then we add the effects of other occupations’ price changes taking the respective own- and cross-price elasticities into account.

### 4.1 Heterogeneity of Own-Price Elasticities

Figure 2a plots occupations’ changes in employment – annualised over the period 1985-2010 – against our measure of changes in occupational prices, based on stayers’ wage growth. These wage growth rates clearly line up with their employment growth, consistent with earlier work (Cavaglia & Etheridge, 2020; Böhm et al., 2024). However, there is a significant amount of variation in the movements of employment and wages across occupations. For example, the explicitly labelled occupation of ‘physicians and pharmacists’ has high occupational wage growth (over five log points per year) but rather small employment growth, while ‘assistants’ exhibit high employment but hardly any wage growth. ‘Data processors’ have both substantial employment and wage growth.

This paper’s hypothesis is that a significant part of such heterogeneity is due to differences in labour supply curves across occupations. To investigate this empirically, we first consider individual price changes in isolation and reduce equation (9) as follows:<sup>16</sup>

$$\Delta e_j(\mathbf{p}) \approx \underbrace{\theta d_{jj} \Delta p_j}_{\text{own-occupation effect}} \quad (10)$$

The hypothesis is that the effect of occupations’ own price changes on their employment should be governed by the heterogeneity in  $d_{jj}$ . In Figure 2b, we split occupations at the median of  $d_{jj}$  and draw two separate regression lines. The blue circles, including ‘physicians and pharmacists’, are the occupations ex-ante predicted to be relatively inelastic in terms of employment response with respect to changes in their own price, while the red circles, including ‘assistants’, are predicted to be relatively elastic.

Indeed, we find that the relationship between occupational employment and price changes is substantially flatter among the red than among the blue circles. That is, the employment response associated with a given price change is substantially stronger among the above-median  $d_{jj}$  (high predicted elasticity) than among the below-median  $d_{jj}$  (low elasticity) occupations. The differences on the regression slopes are not only strongly sig-

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<sup>16</sup>That is, we focus on the partial derivative of own prices on employment ( $\frac{\partial e_j(\mathbf{p})}{\partial p_j} = \theta d_{jj}$ ) from Remark 1.

nificant ( $p$ -value  $< 0.01$ ), but also economically meaningful. As shown in the plot labels, a 1% increase in wages is on average associated with a  $\frac{1}{0.270} \approx 3.7\%$  increase of employment for the group with high predicted elasticities, but only a  $\frac{1}{0.605} \approx 1.7\%$  employment increase for the low-elasticity group. Appendix [Figure C.1](#) alternatively splits occupations into  $d_{jj}$  quartiles. The resulting four regression lines are visibly ranked by predicted labour supply elasticity, with the lowest  $d_{jj}$  quartile exhibiting the steepest relation of employment vs prices, the highest  $d_{jj}$  quartile exhibiting the flattest relationship, and the middle quartiles ranked in between.

## 4.2 Full Own- and Cross-Effects Implementation. Estimating $\theta$

The analysis above showed that even a simplified version of our model helps explain whether occupational changes are characterised by relatively larger shifts in employment or wages. The full model presented in [Section 2](#) is however equally characterised by spillovers that work *across all* occupations.

We take our model to data fully by developing eq. (9) as follows:

$$\begin{aligned} \Delta e_j &\approx \theta \left( d_{jj} \Delta p_j + \sum_{k \neq j} d_{jk} \Delta p_k \right) \\ &= \underbrace{\theta \bar{d}_{diag} \Delta p_j}_{\text{fixed relationship of price with employment}} + \underbrace{\theta (d_{jj} - \bar{d}_{diag}) \Delta p_j}_{\text{heterogeneity of own-occupation effect}} + \underbrace{\theta \sum_{k \neq j} d_{jk} \Delta p_k}_{\text{total cross-occupation effect}} \end{aligned} \quad (11)$$

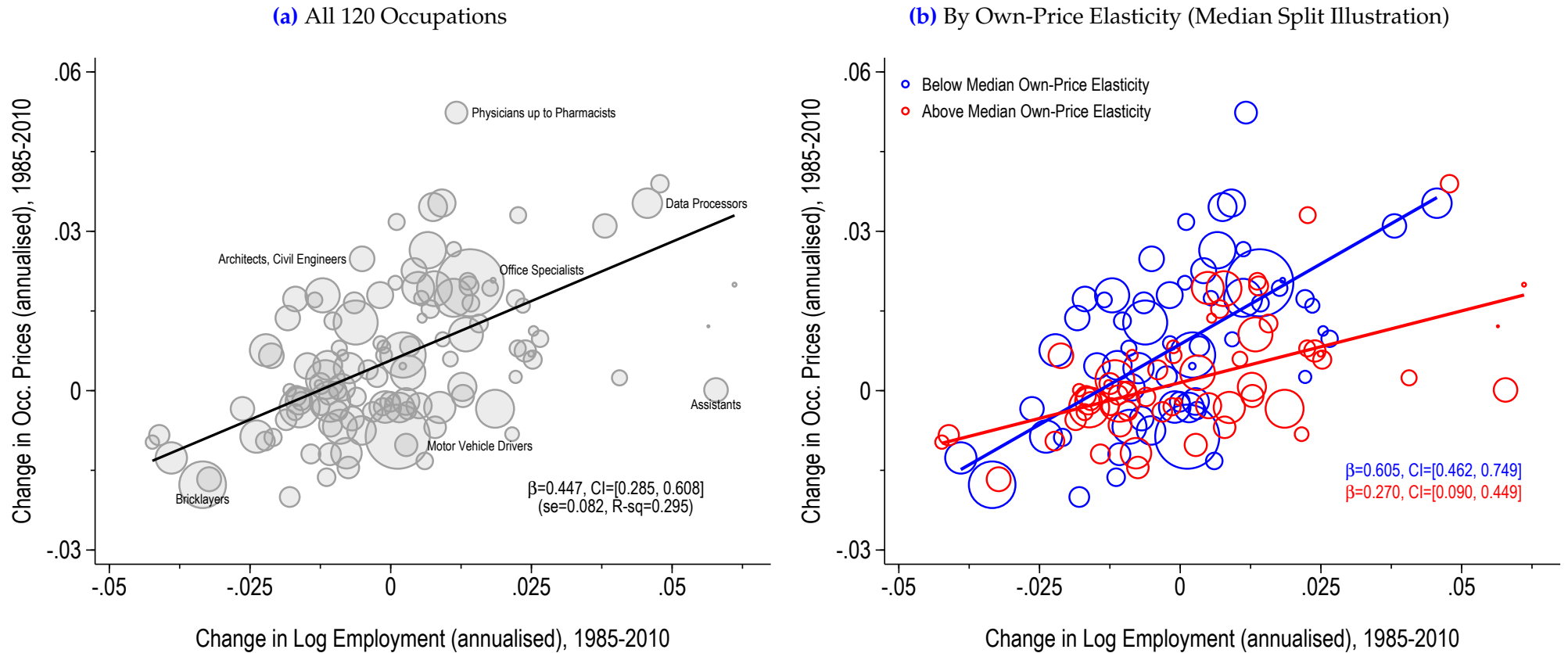
The top line of equation (11) repeats that displayed in eq. (9), and includes own- and cross-occupation effects. As in the previous section, it is instructive to further split the own-occupation effect into a fixed relationship that one would obtain when regressing employment onto price changes ([Figure 2a](#)) and the additional effect of the pure heterogeneity in elasticities  $d_{jj}$  ([Figure 2b](#)). This is done in the last line of eq. (11), where  $\bar{d}_{diag}$  is the mean of matrix  $D$ 's main diagonal elements, and the heterogeneity is captured by  $d_{jj} - \bar{d}_{diag}$ .

Our baseline empirical specification extends eq. (11) in two additional respects:

$$\Delta e_j = \alpha + \theta_1 \bar{d}_{diag} \Delta p_j + \theta_2 (d_{jj} - \bar{d}_{diag}) \Delta p_j + \theta_3 \sum_{k \neq j} d_{jk} \Delta p_k + \varepsilon_j \quad (12)$$

This regression replaces the pecuniary preference parameter common to all effects in eq. (11) by some generic coefficients, which allows us to test the theoretical restriction that  $\theta_1 = \theta_2 = \theta_3 = \theta$ . Second, while the theory analysed a model of employment shares (employment levels in a static population), intercept  $\alpha$  now accounts for overall changes

**Figure 2:** Occupational Price and Employment Changes (1985–2010)



Notes: Panel (a) shows the line from an occupation-size weighted regression of price change on employment change. Panel (b) shows a split by occupations below (blue, inelastic) and above (red, elastic) the median own-price elasticity ( $d_{jj}$ ).  $\beta$  refers to the slope coefficient,  $CI$  stands for the 95% confidence interval,  $se$  refers to standard error, and  $R\text{-sq}$  stands for the R-squared of the regression. Marker size indicates the baseline employment (in 1985) in each occupation.

in log employment. The approximation error from eq. (11) is represented by  $\varepsilon_j$ .

Table 2 reports the estimates from different versions of regression (12). Observations are weighted by occupations' initial employment so that coefficients represent effects as faced by the typical worker.<sup>17</sup> Column (1) shows the regression of  $\Delta e_j$  onto  $\bar{d}_{diag}\Delta p_j$  only. As seen in Figure 2a and in prior work, this fixed relationship of employment with price changes results in a positive and significant slope parameter with an R-squared of 0.29. Column (2), which allows for heterogeneity in own-price elasticities  $d_{jj}$ , yields an additional positive and significant effect, consistent with the strong implications of Figure 2b.

**Table 2:** Determinants of Employment Changes: Own- and Cross-Effects (OLS)

	Dependent Variable: $\Delta e_j$				
	Unrestricted Model			Restricted Model	
	(1)	(2)	(3)	(4)	(5)
fixed relationship: $\bar{d}_{diag}\Delta p_j$	1.59 (0.30)	1.79 (0.31)	4.09 (0.89)	1.81 (0.32)	4.15 (0.70)
heterogeneous own effect: $(d_{jj} - \bar{d}_{diag})\Delta p_j$		1.25 (0.36)	4.07 (1.00)		
total cross effect: $\sum_{k \neq j} d_{jk}\Delta p_k$			4.02 (1.33)		
R-squared	0.295	0.314	0.394	0.310	0.394
Number of occupations	120	120	120	120	120

Notes: The table presents the estimates from different versions of eq. (12). Regressor in column (4) is  $d_{jj}\Delta p_j$ . In column (5), the regressor is  $\sum_k d_{jk}\Delta p_k$ , i.e., corresponding to the full model. All regressions include a constant. Observations weighted by occupation  $j$ 's initial employment size. Period 1985–2010. Standard errors in parentheses; all coefficients shown are significant at the 1% level.

Column (3) of Table 2 then adds the cross effects of price changes in other occupations that may be more or less substitutable. In line with theory, the coefficient on this is also positive and significant. This should be so, since  $d_{jk} < 0$  for  $k \neq j$  such that a positive regression coefficient implies that rising prices in other occupations  $k$  lead to a decline of employment in occupation  $j$ . As discussed above, a stronger implication of the theory is that coefficients  $\theta_1$ – $\theta_3$  should all capture the same pecuniary preference parameter. Although econometrically they are allowed to differ, estimated coefficients turn out almost identical across regressors. We examine the equality of coefficients more formally in columns (4) and (5). Consistent with  $\theta_1 = \theta_2 = \theta_3$  being fulfilled, the estimates do not change much when we run the restricted models (10) and (11).<sup>18</sup>

The estimated coefficients in columns (3) and (5) are all substantially larger than those

<sup>17</sup>Unweighted regressions and additional specifications are reported in Appendix Table C.1 and C.2.

<sup>18</sup>To be precise, column (4) estimates  $\Delta e_j = \alpha + \theta d_{jj}\Delta p_j + \varepsilon_j$  and (5) estimates  $\Delta e_j = \alpha + \theta \sum_k d_{jk}\Delta p_k + \varepsilon_j$ .

in the other columns (Wald test  $p$ -value  $< 0.01$ ). The reason for this is that highly cross-elastic occupations tended to experience similar price changes. That is, for  $-d_{jk}$  large,  $\Delta p_j$  and  $\Delta p_k$  tended to move together such that  $Cov(\Delta p_j, d_{jk}\Delta p_k) < 0$ . Adding this up for all  $k \neq j$ , the own-occupation and total cross-occupation effects are negatively correlated, and including the latter raises the coefficient on the former in our estimation.<sup>19</sup> [Borusyak et al. \(2022\)](#) find a related result in migration regressions across Brazilian region-industries. They highlight the omitted variables bias that results when not taking into account that shocks will often be correlated between workers' current and potentially substitutable employment options. In theirs as well as our case, estimated pecuniary parameters are indeed substantially larger in the full model which accounts for the fact that actual wage opportunities from moving across substitutable options are not that large.<sup>20</sup>

Simulations in [Borusyak et al. \(2022\)](#) show that migration responses can be underestimated by over half when not taking correlated shocks into account. We find that our pecuniary preference parameter more than doubles, to 4.15, once we include total cross-occupation effects. This number is broadly comparable to [Cortes & Gallipoli \(2018\)](#), who estimate  $\theta$  using US wage data and obtain estimates in the range of 2 to 8.87.<sup>21</sup> As another comparison, the literature on employer wage effects finds that the elasticity of labour supply to the firm is around 2–7 (e.g., see [Lamadon et al., 2022](#), and papers cited therein). Given that switching occupations is likely more costly than switching firms, it seems plausible that our implied own-elasticities fall into the lower end of this range (average  $\theta d_{jj} = 1.8$  as  $\bar{d}_{diag} = 0.43$ ). The novelty of our approach lies in the heterogeneity around the average for own-price (from  $0.07 \cdot 4.15 = 0.3$  to  $0.80 \cdot 4.15 = 3.3$ ) as well as cross-price elasticities (from essentially 0 to 1.9). This stems from the worker flows and substitutabilities between occupations that we model explicitly.<sup>22</sup>

A final noteworthy feature of [Table 2](#) is that the R-squared rises by 2 percentage points when including heterogeneous own effects and by another 8 percentage points when adding the total cross-occupation effects. This latter substantial increase, together with the change in the coefficients, indicates that cross-occupation effects are the critical components of the effective labour supply elasticities prevailing in the economy. We shall see this in further detail below. In particular, [Section 6](#) will solve for the full economic model, including all shocks to demand and supply, to quantify the overall contribution of labour

<sup>19</sup>For clarity, we are here considering  $j, k$  and  $d_{jk}$  as given and considering the covariance over random draws of price changes. See [Appendix C](#) for further discussion on this omitted variable bias.

<sup>20</sup>Naively, we can consider variation in wage opportunities *without* considering substitutabilities as the variance of  $d_{jj}\Delta p_j$ . This is twice the variance of  $\sum_{k=1}^N d_{jk}\Delta p_k$ , which additionally captures wage opportunities across close substitutes. We explore this issue more formally and in more detail in [Section 6](#).

<sup>21</sup>[Cortes & Gallipoli \(2018\)](#) set  $\theta = 1$  in what corresponds to eq. (1) but estimate it via the dispersion of  $\varepsilon_j(\omega)$ , which is equivalent (see also footnote 6).

<sup>22</sup>[Berger et al. \(2022\)](#) and [Jarosch et al. \(2019\)](#) model heterogeneity based on employer size differences (granularity). It is worth emphasizing that this feature is also contained in our elasticities.

supply heterogeneity to the occupational changes.

## 5 Labour Demand, Equilibrium, and IV Estimation

To study labour market equilibrium, we add occupations' labour demand to the model. We characterise the resulting system of equations for prices and quantities and study its reaction to shocks. We then implement a novel instrumental variables estimation strategy that exploits relative demand shocks across occupations interacted with their predicted differential effects according to the heterogeneity in labour supplies.

### 5.1 Labour Demand and Equilibrium

Having primarily addressed the supply side thus far, we proceed to close the model by specifying an explicit theory of occupational labour demand. We provide a discussion of the main issues here leaving details to Appendix D.

We consider an economy-wide constant elasticity of substitution (CES) production function

$$Y = A \left( \sum_j \beta_j E_j^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}} \text{ s.t. } \sum \beta_j = 1 \quad (13)$$

where  $\beta_j$  are the factor intensities of different occupation inputs and  $\sigma > 0$  is the elasticity of substitution between occupations in production. Parallel to Remark 1, which focused on supply, competitive behaviour results in labour demand elasticities of the form:

$$\frac{\partial e_j^d}{\partial p_k} = \sigma \begin{cases} -(1 - \tau_j) & \text{if } j = k \\ \tau_k & \text{otherwise} \end{cases} \quad (14)$$

In equation (14), own-elasticities of labour demand are negative but attenuated by an occupation's size. The latter is equivalent to the price index terms in Remarks 2 and 3. The cross-price elasticities are positive and, after occupation size adjustment, constant. These constant elasticities are a defining feature of CES aggregation but not too restrictive here, since what matters for labour supply are the realised price changes after any attenuation or amplification of demand shocks via the production structure. As long as proxies for demand shifters are empirically relevant to predict these relative price changes, we can analyse behaviour on the labour supply side.<sup>23</sup>

<sup>23</sup>Berger et al. (2022) and Lamadon et al. (2022) assume perfect substitutability of firms' outputs in final consumption. The equivalent  $\sigma \rightarrow \infty$  here would lead to  $\beta_j$ -shocks fully compensated by commensurate wage increases (see eq. (16) below) and supply shocks fully feeding through to employment (eq. (17)). Our estimates of the supply-side parameter  $\theta$  are not much affected even for very large  $\sigma$  (see Table D.2).

The full supply and demand model allows the characterisation of the equilibrium as a system of  $N$  simultaneous equations:

$$e_j(\mathbf{b}, \mathbf{s}) = e_j^s(\langle p(\mathbf{b}, \mathbf{s}) \rangle, \mathbf{s}) = e_j^d(\langle p(\mathbf{b}, \mathbf{s}) \rangle, \mathbf{b}) \quad (15)$$

where  $\mathbf{b}$  is the vector of relative productivities (i.e., demand shifters  $(\ln \frac{\beta_i}{1-\beta_i})$ ),  $\mathbf{s}$  is a vector of supply shifters, that, intuitively-speaking, move supply curves vertically in parallel,  $j$  indexes the occupation as before, and both supply ( $s$ ) and demand ( $d$ ) curves depend on the full set of prices.

Our focus is on the response of this system to shocks to the structural parameters, given by changes to  $(\ln \frac{\beta_j}{1-\beta_j})$  and  $\mathbf{s}$ . Appendix D shows that a linear approximation to the changes in prices and employment can be expressed as:

$$\Delta \mathbf{p} \approx V \Delta \mathbf{b} - \frac{1}{\sigma} V \Delta \mathbf{s} \quad (16)$$

and

$$\Delta \mathbf{e} \approx \theta D V \Delta \mathbf{b} + V \Delta \mathbf{s} \quad (17)$$

where  $V = (\frac{\theta}{\sigma} D + I)^{-1} (I - W)$  and  $W$  is the matrix of stacked occupation sizes with  $j, k$ th element  $\tau_k$ . Equations (16) and (17) mirror expressions from a standard model with homogeneous supply elasticities: given the structure of  $D$  and  $V$ , positive demand shocks increase both prices and employment, while positive supply shocks increase employment but reduce prices.

Given that the matrix  $V$  plays a central role in the solution of the equilibrium model, it is worth discussing some of its properties here. In terms of its mathematical features, it has rank  $N - 1$ , just like matrix  $D$ , and each row sums to 0 across columns. Additionally, just like matrix  $D$ , it has non-negative eigenvalues, which ensure, roughly speaking, that shocks move prices and employment in the expected direction.

In terms of economic properties, first note that  $V$  plays a parallel role here to that which matrix  $D$  plays in our analysis of the supply side of the market: it governs the dissipation of shocks across the economy. As in Section 3, we can summarise its effect most simply by examining its diagonal elements. Appendix Table D.1, which displays summary statistics for  $V$ , shows that the correlation of its diagonal with that of  $D$  is  $-0.96$ . Accordingly, for example, the diagonal elements of  $V$  tend to be *lower* for more elastic occupations. As implied by eq. (16), for these occupations, ceteris-paribus demand shocks



induce relatively muted changes to prices.<sup>24</sup>

The right-hand side of Appendix Table D.1 summarises relevant features of the matrix product  $DV$ , which similarly has rank  $N - 1$  with all non-negative eigenvalues. Most importantly, and as expected, its diagonal elements are *positively* correlated with those of  $D$  and *negatively* with those of  $V$ . Accordingly, while ceteris-paribus demand shocks cause a smaller change in prices for more elastic occupations, they induce a *larger* increase in employment implied by eq. (17).<sup>25</sup> The parallel effects to those just discussed can be traced through shocks to supply.

Finally, combining eq. (16) and eq. (17), we obtain our basic regression equation

$$\Delta \mathbf{e} \approx \theta D \Delta \mathbf{p} + \Delta \mathbf{s} \quad (18)$$

In the absence of supply shocks (i.e.  $\Delta \mathbf{s} = 0$ ), OLS is sufficient. The logic of requiring the IV is that supply shocks contribute to, and so are correlated with,  $\mathbf{d}_j \Delta \mathbf{p}$ .

## 5.2 Instrumental Variables Estimation

Suppose we have access to a variable, which we denote by  $r_j$ , that proxies demand shifters  $\Delta \ln \frac{\beta_j}{1-\beta_j}$  but is uncorrelated with supply shifters  $\Delta s_j$ . Equation (16) implies proportionality of the form

$$D \Delta \mathbf{p} \sim DV \mathbf{r} = D \left( \frac{\theta}{\sigma} D + I \right)^{-1} \check{\mathbf{r}} \quad (19)$$

where vector  $\check{\mathbf{r}} \equiv (I - W) \mathbf{r}$  is the weighted-demeaned version of  $\mathbf{r}$ . Equation (19) represents an IV first-stage relationship for the relevant regressor, the product of elasticities with price changes. Implementing this model requires having some information on the demand elasticity  $\sigma$ . We choose a calibration based on estimates from the literature. Based on a range of  $\sigma \in [1.81, 2.10]$  from Burstein et al. (2019) and our initial estimates of  $\theta$  from Table 2, we calibrate  $\frac{\theta}{\sigma} = 2.3$  as a benchmark. As we shall see below, the resulting estimate of  $\theta$  is consistent with this choice. Moreover, the robustness of our results to different

<sup>24</sup>Appendix Table D.1 also provides summary statistics of the elements of  $V$  off the diagonal. In contrast to  $D$ , many of these off-diagonal elements are positive. Intuitively, a positive shock to demand can create a relative scarcity in labour not only in the given sector but also in close substitute occupations. As indicated by eq. (16), this scarcity can then lead to an increase in prices in *both* occupations.

<sup>25</sup>In terms of off-diagonal elements, the Table D.1 shows that for matrix  $DV$  these are all negative. Following through the example just given in footnote 24, a positive demand shock has two opposing effects on close substitute occupations: first, as discussed above, a possible increase in prices draws workers in from the rest of the labour market; second, however, is the direct effect of the shock which pulls workers in from these close occupations to the occupation of the positive shock itself. Overall, the second effect dominates and, as given by eq. (17), this cross-effect always reduces employment.

values of  $\frac{\theta}{\sigma}$  is shown in Appendix [Table D.2](#).<sup>26</sup> More immediately, we turn to the vector  $\mathbf{r}$ .

Our instrument for relative productivity shocks is based on initial task content. As discussed in Section 3, we employ survey information that asks workers which tasks they carry out in their jobs to construct measures of analytical, routine, and manual task intensity across occupations in the late 1970s and early 1980s. Following the literature on routine-biased technical change (RBTC, [Autor et al., 2003](#)), several important papers have found that occupations intensive in analytical tasks grew quite strongly, whereas employment in routine-intensive occupations declined in the late 1980s and the 1990s (e.g., [Autor et al., 2008](#); [Acemoglu & Autor, 2011](#)). For Germany, [Böhm et al. \(2024\)](#) additionally show that the overall demand shift was negative for manual-intensive occupations; with employment, average wages, and skill prices declining after 1985.<sup>27</sup> We thus approximate occupation  $j$ 's (negative) demand shocks during 1985–2010 as

$$r_j = (\textit{routine}_j + \textit{manual}_j) - \textit{analytical}_j$$

The idea is that occupations initially scoring high on routine and manual relative to analytical tasks will decline during the sample period, in terms of wages and employment, compared to occupations that score low on our measure  $r_j$ .

### 5.2.1 Estimation Without Cross-Occupation Effects

Following the exposition in Section 4, we illustrate the IV estimation by first implementing the model removing cross-occupation effects. As in [Figure 2b](#) we capture the heterogeneity of own-occupation effects by splitting estimation by the median value of  $d_{jj}$ . In this case, the instrument  $DV\mathbf{r}$  within each sub-sample of 60 occupations reduces to a scalar multiple of the pure proxy vector  $\mathbf{r}$ .

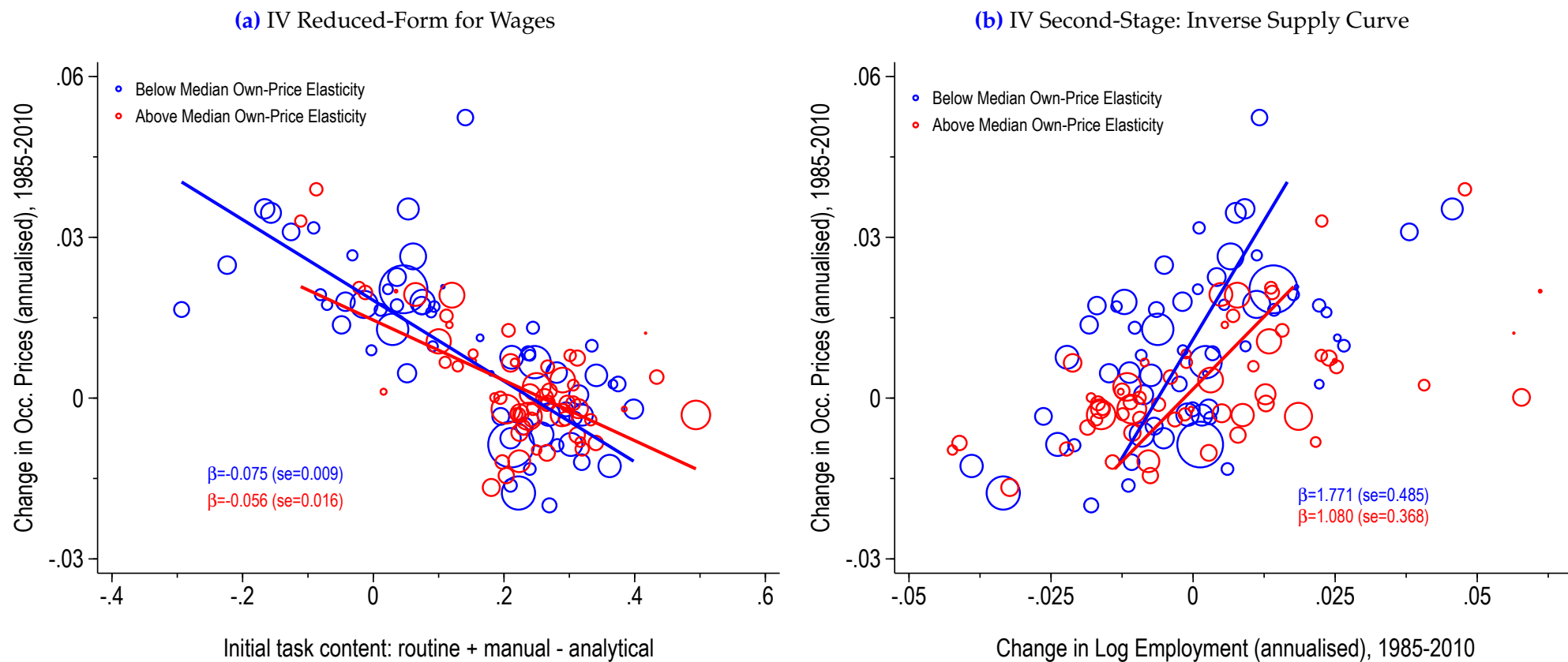
The relationship between  $r_j$  and  $\Delta p_j$  is displayed in [Figure 3a](#). Overall, it is clearly negative given the negative demand shocks that we proxy. We would also expect the regression line to be flatter among more elastic occupations, which should react to a demand shock relatively less in terms of wages and more in terms of employment. Although not significant at conventional levels, this difference is apparent. Similarly, Appendix [Figure D.1](#) displays the relationship between  $r_j$  and  $\Delta e_j$ , and consistently shows that the more

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<sup>26</sup>Relating relative wages to relative occupational inputs in US-CPS data, [Burstein et al. \(2019\)](#) estimate the elasticity of substitution between occupational inputs to be within the range  $\sigma \in [1.81, 2.10]$ . Given the initial estimate of  $\hat{\theta} = 4.15$ , our calibration implies a choice of  $\sigma$  at the bottom end of this range. As emphasized, Appendix [Table D.2](#) shows that our results are largely insensitive to reasonable changes in this parameter.

<sup>27</sup>[Böhm et al. \(2024\)](#) caution that the QCS questionnaires have some difficulty distinguishing between routine and manual job tasks. See also [Rohrbach-Schmidt & Tiemann \(2013\)](#) for details about classifying tasks in the German context.

**Figure 3:** Instrumental Variables Illustration: Median-Split by Own-Price Elasticity



Notes: Panel (a) shows reduced-form regressions of occupations' price changes on their initial task contents  $r_j$ . Panel (b) shows second-stage IV-2SLS regressions of occupations' price changes on predicted employment changes using initial task contents as the instrument. Colour codes and linear regression lines are split by occupations below (blue, inelastic) and above (red, elastic) the median own-price elasticity ( $d_{jj}$ ).  $\beta$  and  $se$  refer to the slope coefficient and standard error, respectively. Marker size indicates the baseline employment (in 1985) in each occupation.

elastic occupations present a slightly steeper slope.

Figure 3b then depicts the second stage in this simplified model. Again to parallel Figure 2b, and to keep prices on the vertical axis as standard, we display the *inverse* supply curve, with price changes as a function of changes to employment. In this case, the slopes are steeper than those in Figure 2b. This reflects that, in this case, removing shocks to supply also eliminates attenuation of the estimated regression line. What remains the same is that the relationship of wages with employment is substantially steeper among occupations ex-ante classified as inelastic compared to elastic occupations. These are the relative reactions in terms of employment for a given price change among more versus less elastic occupations. Figure 3 is therefore illustrative of the type of variation employed in our instrumental variables approach.

### 5.2.2 Full Model Estimation

Finally, expression (20) reports the results from the two-stage least squares regression, using (19) as first and (18) as second stage:

$$\begin{aligned}\Delta e_j &= \underset{(1.30)}{4.78} \mathbf{d}_j \Delta \mathbf{p} + \text{constant} + \text{error}_j \\ \mathbf{d}_j \Delta \mathbf{p} &= \underset{(0.0125)}{-0.046} \mathbf{d}_j V \mathbf{r} + \text{constant} + \text{error}_j\end{aligned}\tag{20}$$

We focus directly on the model with a single value of  $\theta$ . In contrast to the illustration of the IV shown in Figure 3b, the theoretical model here is specified in terms of the standard (rather than inverse) supply curve. The first stage relationship of occupations' task intensities on price changes, multiplied by elasticities  $\mathbf{d}_j$  reflecting their implied impact on employment, is negative as expected and displays an  $F$ -statistic of  $\left(\frac{-0.046}{0.0125}\right)^2 = 13.5$ . In the second stage, the estimated  $\theta$  parameter is 4.78, or about 15% higher than the OLS estimate of 4.15 from Table 2, and again statistically significant.

Standard intuition implies that, if price changes are correlated with supply shocks, then OLS should be attenuated and biased downwards. We see this here, but the IV estimate in (20) is still relatively similar to that from the OLS. As we discuss through a formal analysis in Appendix D.4, in this case two relevant and opposing forces are at play: i) demand shocks were positively correlated with supply shocks, ii) the variance of supply shocks was relatively small. The second factor would, on its own, lead to only a small attenuation of OLS estimates. And, in fact, this attenuation is partly offset by the first factor. We now turn to providing further insights into the full solution of the underlying supply and demand model.

## 6 Model-Based Decomposition and Counterfactuals

The previous section shows how to solve for the equilibrium of the full supply and demand model. We now use this to decompose the changes in employment and wages into contributions of different factors: shocks to occupational demand and supply as well as the heterogeneities in labour supply elasticities that we emphasise.

### 6.1 Construction of Counterfactuals

We use equations (16)–(17) to express the changes of prices and employment in terms of parameters and exogenous shocks as follows:<sup>28</sup>

$$\Delta \mathbf{p} = \left( \frac{\theta}{\sigma} D + I \right)^{-1} \Delta \mathbf{b} - \frac{1}{\sigma} \left( \frac{\theta}{\sigma} D + I \right)^{-1} \Delta \mathbf{s} \quad (21)$$

$$\Delta \mathbf{e} = \theta D \left( \frac{\theta}{\sigma} D + I \right)^{-1} \Delta \mathbf{b} + \left( \frac{\theta}{\sigma} D + I \right)^{-1} \Delta \mathbf{s} \quad (22)$$

The equilibrium solution treats equations (21) and (22) as equalities and – up to constants representing general wage and employment growth – reproduces the actual changes of  $\Delta \mathbf{p}$  and  $\Delta \mathbf{e}$  from the data. We manipulate these reduced-form expressions to study the role of labour supply heterogeneity versus occupation-specific shocks for the variation in wages and employment. We provide a summary here leaving details to Appendix E.1.

To do this, we replace  $D$  with its matrix equivalents from counterfactual environments with more homogeneous elasticities. Our first counterfactual, matrix  $D_{own}$ , considers the case that occupations’ aggregate (own-price) elasticities vary but their similarities with other occupations are homogeneous. For example, employment in service occupations may be responsive to price but suppose that flows of workers into services come equally from any other occupation according to its size. This is consistent with theoretical models often found in the literature on firms (e.g. Card et al., 2018; Lamadon et al., 2022; Berger et al., 2022), where the costs of entering employer  $j$  do not depend on the source employer  $i$  (that is,  $a_{ij} = a_j$  in eq. (1)). Main diagonal elements of  $D_{own}$  continue to be the actual own-price elasticities, whereas cross-price elasticities reduce to appropriate fractions of the on-diagonals.<sup>29</sup> We term this the model with ‘heterogeneous own-price elasticities’.

Another counterfactual imposes completely homogeneous labour supply elasticities. The main diagonal elements of matrix  $D_{hom}$  become an average  $\bar{d}_{diag}$  and cross-price elas-

<sup>28</sup>Equations (21) and (22) are obtained by inserting the solution for  $V$  into equations (16)–(17) and then using the fact that demand and supply shocks are weighted mean zero by construction (see Appendix D.2). Now, the backed-out shocks,  $\Delta \mathbf{b}$  and  $\Delta \mathbf{s}$ , are indeed contingent on the CES assumption (13).

<sup>29</sup>We use size-weighted  $d_{jk} = \frac{-\tau_k}{1-\tau_j} d_{jj} \forall k$ , which is more theory-consistent, but  $d_{jk} = \frac{-1}{N-1} d_{jj}$  fully homogeneous yields the same results as those shown below. See Appendix E.1 for details.

ties a constant fraction of it. This counterfactual is consistent with specifications in the empirical literature that regress occupations’ log employment changes on their log wage changes (e.g. Autor et al., 2008; Dustmann et al., 2009; Cavaglia & Etheridge, 2020; Böhm et al., 2024, or column (1) of Table 2). From eq. (18), it leads to a relationship of the form  $\Delta e_j = \text{constant} + \text{slope} \cdot \Delta p_j$ , where the slope is proportional to pecuniary preferences  $\theta$  and the constant is proportional to the average wage growth in the economy. We term this the ‘fully homogeneous’ model.

As an alternative to the counterfactual  $D$ -matrices, we turn off the classic simultaneous equations component. We do this by shutting down supply shocks, using  $\Delta \mathbf{s}_{off} = \mathbf{0}$  in equations (21)–(22), which allows us to assess the variation in wages and employment that these shocks account for.

## 6.2 Results

Throughout this section we use our baseline parameter estimates:  $\theta = 4.8$ ,  $\sigma = 2.10$ , and  $\frac{\theta}{\sigma} = 2.3$ .<sup>30</sup> We begin with a decomposition to uncover the drivers of overall employment changes. We do this by following eq. (22) and running regressions of observed employment changes on various components of the right-hand side. The first row in Table 3 shows that demand shocks in the fully homogeneous model (i.e.,  $\Delta \mathbf{s}$  replaced by  $\Delta \mathbf{s}_{off} = \mathbf{0}$  and  $D$  replaced by  $D_{hom}$ ) explain 64% of the variance of employment changes.<sup>31</sup> This is consistent with the literature on job polarisation (e.g. Acemoglu & Autor, 2011; Goos et al., 2014), where demand shocks are the main drivers of occupational changes. But it still leaves room for a substantial role of supply.

The second row of Table 3 adds supply shocks, still under  $D_{hom}$ , to create a new counterfactual employment change according to eq. (22) in the homogeneous model. This explains 86% of the observed employment changes in an R-squared sense, or roughly half of the remaining variance in  $\Delta \mathbf{e}$ . Similarly, adding heterogeneity of supply under  $\Delta \mathbf{s}_{off} = \mathbf{0}$ , and using full matrix  $D$  with the demand shocks in eq. (22), accounts for 85% of employment changes and again roughly half of the remaining variance.<sup>32</sup> Together, supply shocks and heterogeneity, by construction, explain the full variation in actual employ-

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<sup>30</sup>As discussed earlier, Appendix Table D.2 shows that  $\theta$  estimates are largely insensitive to the exact  $\frac{\theta}{\sigma}$ . The results below are also similar for the range of  $\theta$  and  $\sigma$  values in that table.

<sup>31</sup>Regarding the table labels, regressing  $\Delta \mathbf{e}$  on raw  $\Delta \mathbf{b}$  gives the same fit as regressing it on  $\theta D_{hom} V_{hom} \Delta \mathbf{b} = \text{constant} + \text{slope} \cdot \Delta \mathbf{b}$ , which is demand shocks’ implied employment impact from eq. (22).

<sup>32</sup>It is worth noting why the R-squared is higher when we regress employment changes on demand shocks than when we regress on observed price changes in Table 2. Intuitively, the error terms related to supply shocks in eq. (22), given by  $V \Delta \mathbf{s}$ , are substantially less dispersed than those in the OLS estimation of eq. (18),  $\Delta \mathbf{s}$ . In the latter, they are also negatively correlated with the regressor,  $\Delta \mathbf{p}$ , due to simultaneity, lowering the estimated contribution of prices.

ment changes (last row of Table 3).<sup>33</sup> They are thus both important, in addition to demand shocks and equally so, to account for the overall occupational employment changes observed over the past decades.

**Table 3:** Decomposition of Overall Employment Changes

	(1) R-sq. between data & model	(2) Remainder explained
Base $\Delta \mathbf{e}$ with $\Delta \mathbf{b}$	0.641	
Adding supply shocks	0.856	59.9%
Adding supply heterogeneity	0.849	57.9%
Full model	1.000	

*Notes:* This table decomposes the employment changes in our 120 occupations. The first row considers only demand shocks in the fully homogeneous model. The second row adds supply shocks. The third row alternatively adds supply heterogeneity. The final row considers the full model. Column (1) reports the regression R-squared between the data and model. Column (2) gives the percent of remainder explained by either the counterfactual with only supply shocks or with only heterogeneity.

We provide further insight into this result by constructing proper counterfactuals. Figure 4 displays results where, in keeping with the figures throughout the paper, we relate implied counterfactual price changes  $\Delta \mathbf{p}_{cf}$ , generated by eq. (21), to implied counterfactual employment changes  $\Delta \mathbf{e}_{cf}$  from eq. (22) across different scenarios. We start again with demand shocks in the fully homogeneous model. In this case, all occupational changes emanating from experienced demand shocks  $\Delta \mathbf{b}$  run perfectly along a single supply curve (panel a). We can see from this plot that the explicitly labelled ‘physicians and pharmacists’ as well as ‘data processors’ are among the occupations with the largest relative demand increases over time. ‘Bricklayers’ are among the occupations with the largest negative demand shocks.<sup>34</sup>

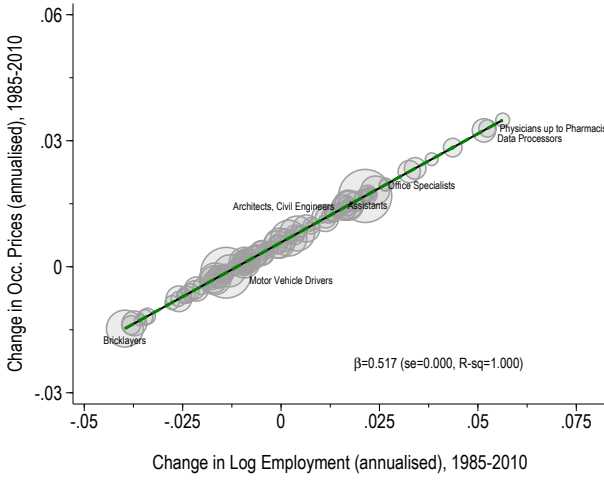
Panel b shows how supply shocks affect this counterfactual. Here we facilitate interpretation by retaining the regression line from panel a. Switching  $\Delta \mathbf{s}$  back on introduces attenuating variation around the price-employment relationship such that the R-squared in a regression of price on employment declines to 65%. The regression line moves *clockwise* and its slope reduces to 0.36, partly driven by positive demand *and* supply shocks in occupations such as ‘assistants’. Still, the regression slope remains strongly positive, which is due to the larger dispersion of demand shocks than of shocks to supply.

<sup>33</sup>The two standalone contributions sum to  $59.9\% + 57.9\% > 100\%$ , which implies a  $-18\%$  interaction effect. This is because eq. (22) is not purely additive.

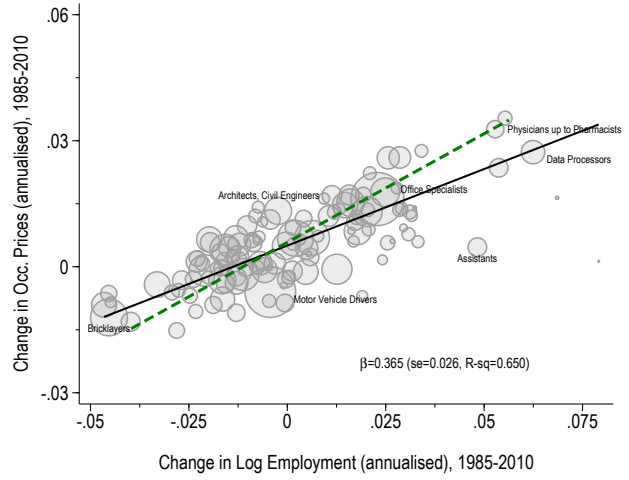
<sup>34</sup>It is worth noting here that the points in this plot include average real price and employment growth, both of which are positive over the period. Accordingly, occupations with no relative demand shock are located slightly above and to the right of the origin.

**Figure 4:** Counterfactual Changes of Prices and Employment

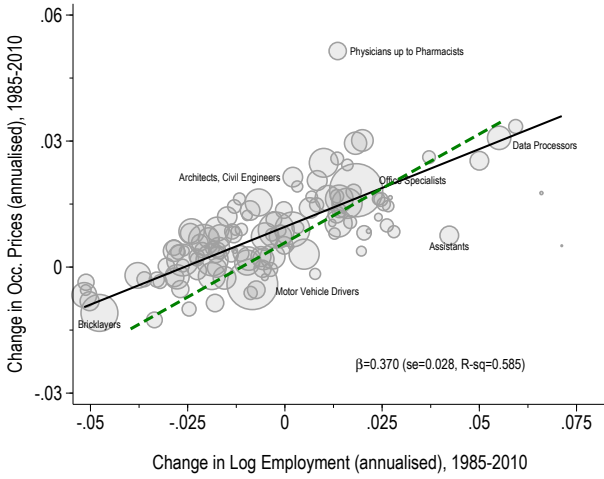
**(a)** Demand shocks only; Fully-homog. supply



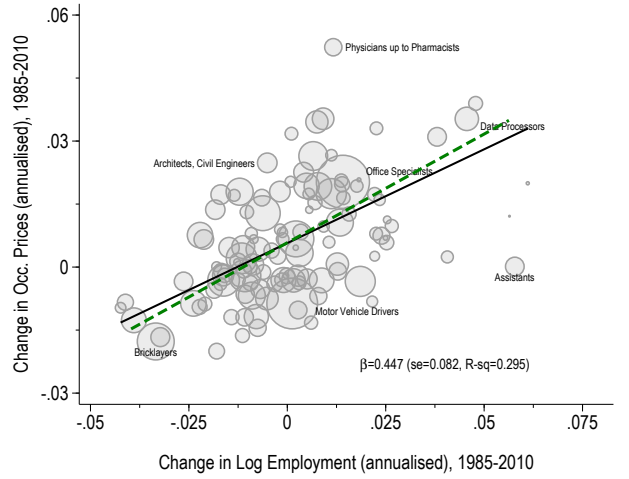
**(b)** ... with supply shocks



**(c)** ... with supply shocks; Het. own-price supply



**(d)** Both shocks; Fully heterogeneous supply



*Notes:* The figure shows occupational price and employment changes for different manipulations of the elasticity matrix  $D$  and  $\Delta s$ , as described in Section 6.1. In Panel 4a, both supply shocks and heterogeneity in  $D$  are switched off (i.e.  $\Delta s = \Delta s_{off} = 0$  and  $D_{hom}$ ), leaving only demand shocks. Panel 4b first introduces the supply shocks (i.e.  $\Delta s \neq 0$ ), then 4c adds own-elasticity heterogeneity (i.e.  $D_{own}$ ). Finally, Panel 4d shows the full model (actual data) by including also heterogeneous cross-elasticities (i.e. full matrix  $D$  is used). For the exact description of the counterfactuals see Section 6.1 and Appendix E.1. The OLS with slope coefficients, standard errors, and R-squared is shown for each panel. For ease of comparison, the regression line in Panel 4a is repeated as green-dashed in all panels. Marker size indicates the baseline employment (in 1985) in each occupation.

The remaining two panels of Figure 4 show how the movements of occupational prices and employment are affected by labour supply heterogeneity. Panel c first introduces heterogeneity of occupations' own-price elasticities, but retains homogeneity in cross-occupation elasticities (i.e., uses matrix  $D_{own}$  discussed above). A geometric interpretation of the transition from panel b to c is that each occupational point is translated along its own demand curve and according to its own aggregate labour supply elasticity. Inelastic occupations move *counterclockwise* around the centre: in a Northwest direction for those with positive demand shocks, Southeast for those with negative demand shocks, and with no effective change for those with no shock to demand. Symmetrically, occupations that



are more elastic than average move around the centre *clockwise*.

Panel **c** shows that the effect of allowing for this heterogeneity is, for the most part, small. This is consistent with the regression-based analyses of Sections 4–5. A strong exception is for ‘physicians and pharmacists’, which is very own-price inelastic (see again Table 1) and experienced a large positive demand shock. This makes its implied price increase much higher, and its employment increase lower, compared to panel **b** (or compared to, say, ‘data processors’, who exhibit an own-price elasticity of roughly average strength). In short, ‘physicians and pharmacists’ is the most notable occupation with an extreme own-elasticity (high or low) that also had an extreme demand shock.

Finally, panel **d** also includes heterogeneity in cross-occupation elasticities, and so reproduces the observed data. Compared to panel **c**, variation around the regression line increases substantially, such that the R-squared from a regression of price on employment reduces from 59% to 30%. As an illustration of this feature, displayed occupations such as ‘architects with civil engineers’ and ‘motor vehicle drivers’ move away from one another. In addition, the locus of points moves on average *counterclockwise* and the slope of the regression line increases from 0.37 to 0.45. These changes show the importance of allowing for cross-occupation elasticities to explain the data. As discussed previously, cross-occupation effects make occupations less price elastic. In effect, realised cross-price elasticities captured by the full matrix  $D$  are lower than those captured by matrix  $D_{own}$  or the fully homogeneous model, since ‘clusters’ of occupations, which within them are relatively elastic, are equally shocked. Meanwhile, substitutabilities between the (differently shocked) clusters are relatively low.<sup>35</sup>

The impact of including the total cross-occupation effect is a key difference of the exposition in Figure 4 compared to earlier Table 3. It is seen even more starkly in Appendix Figure E.1 where we introduce heterogeneous elasticities *before* introducing supply shocks. Without the background dispersion from these, the increase in the regression slope is highly obvious. We also display the impact of demand and supply shocks along the occupational wage distribution in Appendix Figure E.3–E.4. Among other things, these show that the lower effective labour supply elasticities have led to even larger between-occupation inequality than in a model without cross-occupation effects. For Figure 4, as was the case in the table, it is worth noting that, although changing the sequence with which we re-introduce model features makes them more or less salient graphically, it

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<sup>35</sup>An interesting exception to this is ‘assistants’, which moves further Southeast in panel **d** compared to panel **c**. For this occupation, close substitute occupations saw strong relative demand declines, and its positive shock was therefore accentuated, making working as an assistant even more attractive. Our model thus provides a novel explanation for the expansion of this occupation over this period: the large increase in the number of assistants was not only due to an increase in the number of individuals suited for this type of work (positive supply shock) but also due to a strong increase in demand, not in absolute terms but *relative* to occupations requiring similar skills.

does not change their quantitative importance markedly.

We finish this discussion by starting again at panel [a](#) and, from there, providing another assessment of the relative importance to dispersion in price and employment changes of supply shocks versus supply heterogeneity. Using changes in R-squared as a metric, we see that this is roughly equal. Panels [a](#) and [b](#) show that supply shocks cause a decline in the R-squared of 35 percentage points, while [b](#) and [d](#) show that supply heterogeneity accounts also for a decline of 35 points. Therefore, and consistent with [Table 3](#), the relative impacts of supply heterogeneity and shocks are similar in explaining occupational changes. Moreover, we have discussed that, within this overall important contribution, different aspects of heterogeneity are important for explaining idiosyncratic outcomes of particular occupations.

## 7 Extensions and Robustness

This section summarises findings from extensions and robustness checks of the main results in the paper. The model is extended to non-employment transitions in [7.1](#). We then discuss results when estimating in five-year sub-periods and finally, in [7.3](#), with an alternative method of estimating changes in occupational prices.

### 7.1 Accounting for Non-Employment Transitions

A driver of heterogeneity in occupational changes that we have omitted so far is the extensive margin of employment. This may be particularly important if young workers' entry and old workers' exit from the labour market affect specific occupations' growth differently. In the case of US routine occupations, this was shown by [Autor & Dorn \(2009\)](#). The secular decline of German unemployment from the mid-2000s may also be relevant here.

In line with eq. (1), we interpret indirect utility in  $M$  different non-employment states  $m \in \{N + 1, \dots, N + M\}$  as containing pecuniary payoffs, transition costs, and idiosyncratic components. While pecuniary payoffs  $p_m$  are unobserved, the empirical framework can be extended to control for switches to and from different non-employment states.<sup>36</sup>

We start by computing a new elasticity matrix that includes all transitions to and from non-employment states. Then consider equation (11) with  $N + M$  occupations, where  $M$

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<sup>36</sup>As noted above, regressions so far included a constant that captures employment growth from sources other than direct occupational transitions (e.g. due to the general growth of the working-age population). Now we allow for such contributions to vary by occupation.

refers to different non-employment sectors:

$$\Delta e_j \approx \theta \sum_{k=1}^{N+M} d_{jk} \Delta p_k = \theta \sum_{k=1}^N d_{jk} \Delta p_k + \sum_{m=N+1}^{N+M} (\theta \Delta p_m) d_{jm} \quad (23)$$

The first summation on the right-hand side represents our standard occupational own- and cross-occupation effects, while in the second summation, we explicitly group factors  $\theta \Delta p_m$  together. This is to indicate that  $d_{jm}$  are control variables for the occupation  $j$ 's elasticity to non-employment state  $m$ . The  $\theta \Delta p_m$  coefficient represents the combination of pecuniary preferences and changes in non-employment 'prices'. In principle,  $\Delta p_m$  could be identified from the coefficient on this control and the estimate of  $\theta$ .

Appendix F.1 shows the results from these estimations with  $M = 3$  different non-employment sectors: unemployment, out of the labour force (during the career and including part-time as well as employment with benefit receipt), and entry or exit due to newly joining the labour force at age 25–32 or retiring at age 52–59.<sup>37</sup> The R-squared is somewhat higher in these specifications as more of the heterogeneity in employment growth can be explained when allowing for occupations' different elasticities with respect to non-employment states. Other than that, the estimation results in the OLS and the IV turn out broadly similar to before. Findings also do not substantively change when further separating part-time work and work with benefit receipt from out of labour force, or when merging the three states into one single non-employment sector.

## 7.2 Analysis in Five-Year Sub-Periods

In the main analysis, we have studied changes of occupational prices and employment over the period 1985–2010. We now split this longer interval into five-year sub-periods (1985–1990, 1990–1995, 1995–2000, 2000–2005, and 2005–2010), to explore robustness and potential temporal heterogeneity.

The pooled panel sample containing 600 observations (120 occupations  $\times$  5 sub-periods) is used to estimate an extended version of (11):

$$\Delta e_{jt} = \alpha + \theta d_{jj} \Delta p_{jt} + \theta \sum_{k \neq j} d_{jk} \Delta p_{kt} + \delta_t (+\gamma_j) + \varepsilon_{jt} \quad (24)$$

where  $t$  refers to a five-year period, and the matrix of elasticities  $D$  can be obtained using the baseline period 1975–1984 as previously or using the lagged matrix from the preced-

<sup>37</sup>A limitation of the records from unemployment insurance is that we cannot observe the exact reasons for individuals entering or leaving the dataset (e.g. health shock, discouraged worker, emigration, self-employment, military service or becoming a civil servant). Outside the age range for labour market entry or retirement, these are all treated as out of the labour force for our purposes.

ing five-year period (e.g., for the period 1995–2000, the matrix of elasticity is computed using employment transitions over the period 1990–1995).<sup>38</sup> The period fixed effects ( $\delta_t$ ) capture unobserved time-specific shocks or trends that affect all occupations uniformly within each sub-period. A more demanding specification additionally includes occupation fixed effects ( $\gamma_j$ ), removing average occupational growth over 1985–2010 and identifying only from accelerations or decelerations in the respective sub-period.

The results are shown in Appendix F.2. Graphically, Figure F.1 plots prices against employment growth for the pooled sample of 600 occupation–sub-periods as well as separately for each sub-period, analogous to Figure 2b. The previous finding is strengthened in the sense that each regression slope for above-median own-price elastic occupations is flatter than any slope for below-median own-price inelastic occupations. OLS and IV estimation on the pooled data essentially reproduce the results obtained in Sections 4–5. In estimations with occupation fixed effects ( $\gamma_j$ ), which only use deviations of price changes from their 1985–2010 averages interacted with the supply elasticities, results are also broadly similar.<sup>39</sup> Overall, estimation in a series of shorter intervals shows that the role of occupational supply elasticities persists, with evidence that even acceleration or deceleration of price growth in different sub-periods is translated into employment growth according to these elasticities.

### 7.3 Alternative Occupational Price Estimation

The results so far use occupation stayers’ (i.e., workers who do not switch occupations from one year to the next) wage changes as the main estimate of changes in occupational prices. This accounts flexibly for the selection into occupations based on observable and unobservable individual characteristics. In this section, we use an alternative estimation for occupational prices that also controls for the occupation-specific effect of time-varying observable characteristics on wages.

In this approach, originally proposed by Cortes (2016), observed log wages for individual  $\omega$  in period  $t$  are modeled by

$$\ln w_t(\omega) = \sum_j Z_{jt}(\omega) \varphi_{jt} + \sum_j Z_{jt}(\omega) X_t(\omega) \zeta_j + \sum_j Z_{jt}(\omega) \kappa_j(\omega) + \mu_t(\omega) \quad (25)$$

where  $Z_{jt}(\omega)$  is an occupation selection indicator that equals one if individual  $\omega$  chooses occupation  $j$  at time  $t$ ,  $\varphi_{jt}$  are occupation–time fixed effects, and  $\kappa_j(\omega)$  are occupation–spell fixed effects for each individual. The model allows for time-varying observable skills (e.g.

<sup>38</sup>Consistent with the autocorrelation of matrix  $D$  over time (see Appendix Table B.3), results are similar whether we use the baseline or the lagged matrix.

<sup>39</sup>We can only do the OLS for this as the instrumental variable does not vary by period.

due to general human capital evolving over the life cycle) by including in the control variables  $X_t$  a set of dummies for five-year age bins interacted with occupation dummies.<sup>40</sup> Finally,  $\mu_t(\omega)$  reflects classical measurement error, which is orthogonal to  $Z_{jt}(\omega)$ . It may be interpreted as a temporary idiosyncratic shock that affects the wages of individual  $\omega$  in period  $t$  regardless of their occupation choice. The estimated occupation-year fixed effects ( $\varphi_{jt}$ ) are the parameters of interest, giving us a measure for changes (in our case, between 1985 and 2010) in occupational prices ( $\Delta p_j = \varphi_{j,2010} - \varphi_{j,1985}$ ).

The results using occupational prices à la Cortes (2016) are presented in Appendix F.3. The main figures of the paper are replicated using these alternative prices in Figure F.2. The main regression results, shown in Table F.3, including those when accounting for non-employment transitions, turn out very similar. Our findings hence remain consistent and robust to this alternative estimation for changes in occupational prices.

## 8 Conclusion

Shifts in the demand for occupations have led to large changes in employment and wages (e.g., Acemoglu & Autor, 2011; Goos et al., 2014). One important aspect that remains relatively unexplored is the responsiveness of labour supply (i.e., the ability of the workforce to react) to the changing the demand for jobs. In this paper, we study the role of the heterogeneity of occupational labour supply in explaining the variation of employment and wage growth between 1985 and 2010.

We propose a measure of occupation-specific labour supply elasticities, capturing the impact on employment of changes in the wage structure across occupations. These include wage changes in the occupation itself (own-price elasticities) and wage changes in other occupations (cross-price elasticities). We show how these price elasticities can be interpreted in terms of moments of the job flows and study how they relate to several occupational characteristics such as occupational licensing or task content. We implement our framework in administrative panel data from Germany with long-running occupation information. Findings show that the heterogeneity in labour supply elasticities matters and that, in particular, spillovers from correlated shocks across highly similar occupation pairs are important for the evolution of the occupation structure in Germany.

We close by highlighting two potential avenues of further study that our research opens up. First, the framework allows evaluating policies that may help raise occupational labour supply elasticities, e.g. as discussed in Autor et al. (2023) and potentially via changing occupational licensing (Kleiner & Xu, 2024) or educational contents (Eckardt,

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<sup>40</sup>The bins are for ages 25–29, 30–34, 35–39, 40–44, 45–49, 50–54, and 55–59.

2023). Our findings indicate that policies which enhance cross-price elasticities between relatively dissimilar occupations in terms of their likely shocks may have the largest beneficial impacts. Second, while this paper studies past occupational changes, the framework at hand can naturally be used for prediction. In particular, current job mobility flows together with forecasts of demand changes lead to distinct implications for occupational sourcing, employment, and wages from our model.<sup>41</sup> This could help project some of the structural changes and labour market inequality that we are likely to expect in the future.

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<sup>41</sup>Demand changes may, e.g., be due to enhanced automation or artificial intelligence (Felten et al., 2018; Eloundou et al., 2023; Autor, 2024). The German Federal Employment Agency provides a tool, ‘Job Futur-omat’ (Federal Employment Agency, 2023), that predicts how digital technology will change the tasks in each detailed occupation. Similar predictions are available by, e.g., the U.S. Bureau of Labor Statistics (2023).

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Appendix for:

# Heterogeneous Occupational Supply Elasticities and Changes in Labour Demand

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# A Formal Results on the Elasticity Matrix

This section further develops the model introduced in Section 2 of the paper, integrating additional aspects for a more comprehensive analysis. We begin by presenting formal derivations of the main remarks and a deeper exploration of their underlying intuition. We then derive another formal result on the full vector of price changes.

## A.1 Derivation of Formal Results: Remarks 1–3

We start by formally deriving Remarks 1–3.

### A.1.1 Remark 1 (Elasticities and Job Flows)

To simplify notation in the following, we define ‘choice index’  $\lambda(\mathbf{p}) \equiv \frac{1}{\sum_{k=1}^N \exp(\theta p_k + a_{ik})}$ , where  $\mathbf{p}$  represents the vector of log prices. The fraction of individuals working in sector  $j$  as a function of log prices, denoted by  $E_j(\mathbf{p})$ , can then be expressed as:

$$E_j(\mathbf{p}) = \sum_i \tau_i \lambda(\mathbf{p}) \exp(\theta p_j + a_{ij})$$

Recall that our interest centres on (own- and cross-occupation) price elasticities, the response of employment in occupation  $j$  to occupation  $k$ ’s log price change. Using the accounting identity presented in equation (3), we formally write this as:

$$\frac{\partial E_j(\mathbf{p})}{\partial p_k} = \sum_i \tau_i \left( \lambda(\mathbf{p}) \frac{\partial \exp(\theta p_j + a_{ij})}{\partial p_k} + \frac{\partial \lambda(\mathbf{p})}{\partial p_k} \exp(\theta p_j + a_{ij}) \right)$$

Computing the second element in the brackets,  $\frac{\partial \lambda(\mathbf{p})}{\partial p_k}$ , gives:

$$\begin{aligned} \frac{\partial \lambda(\mathbf{p})}{\partial p_k} &= -\frac{\theta \exp(\theta p_k + a_{ik})}{(\sum_s \exp(\theta p_s + a_{is}))^2} \\ &= -\theta \frac{1}{\sum_s \exp(\theta p_s + a_{is})} \frac{\exp(\theta p_k + a_{ik})}{\sum_s \exp(\theta p_s + a_{is})} \\ &= -\theta \lambda(\mathbf{p}) \pi_{ik}(\mathbf{p}) \end{aligned}$$

By combining these results, we derive the following expression:

$$\frac{\partial E_j(\mathbf{p})}{\partial p_k} = \begin{cases} \sum_i \tau_i \theta (\pi_{ij}(\mathbf{p}) (1 - \pi_{ij}(\mathbf{p}))) & \text{if } j = k \\ -\sum_i \tau_i \theta (\pi_{ij}(\mathbf{p}) \pi_{ik}(\mathbf{p})) & \text{otherwise} \end{cases}$$

Finally, writing  $e_j \equiv \ln E_j(\mathbf{p})$ , we obtain:

$$\begin{aligned} \frac{\partial e_j(\mathbf{p})}{\partial p_k} &= \frac{1}{E_j(\mathbf{p})} \frac{\partial E_j(\mathbf{p})}{\partial p_k} \\ &= \theta \begin{cases} \frac{\sum_i \tau_i (\pi_{ij}(\mathbf{p})(1-\pi_{ij}(\mathbf{p})))}{\sum_i \tau_i \pi_{ij}(\mathbf{p})} & \text{if } j = k \\ \frac{-\sum_i \tau_i (\pi_{ij}(\mathbf{p})\pi_{ik}(\mathbf{p}))}{\sum_i \tau_i \pi_{ij}(\mathbf{p})} & \text{otherwise} \end{cases} \end{aligned}$$

These are equations (4)–(5) in Section 2. It shows that the short-term partial derivative of occupation  $j$ 's log employment share with respect to  $k$ 's log price can be computed using (baseline) transition probabilities, and a pecuniary parameter  $\theta$ . We next discuss alternative formulations of the elasticities in terms of moments of job flows.

### A.1.2 Remark 2 (Individual Cross-Price Elasticities)

We have described the off-diagonal elements of the elasticity matrix  $D$  as:

$$d_{jk} = -\frac{1}{\tau_j} \sum_i \tau_i \pi_{ij} \pi_{ik}$$

where  $\pi_{ij}$ ,  $\pi_{ik}$  are elements of the transition matrix and  $\tau_i$  is the  $i$ th element of the associated stationary vector. To interpret this further, consider the weighted covariance between columns of the normalised transition matrix:

$$\begin{aligned} \text{Cov}_\tau(\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k}) &\equiv \sum_i \tau_i (\tilde{\pi}_{ij} - \mathbb{E}_\tau \tilde{\pi}_{.,j}) (\tilde{\pi}_{ik} - \mathbb{E}_\tau \tilde{\pi}_{.,k}) \\ &= \sum_i \tau_i (\tilde{\pi}_{ij} - 1) (\tilde{\pi}_{ik} - 1) \end{aligned}$$

where

$$\tilde{\pi}_{iq} \equiv \frac{\pi_{iq}}{\tau_q}$$

and the second line follows from the first because  $\sum_i \tau_i \tilde{\pi}_{iq} = \frac{1}{\tau_q} \sum_i \tau_i \pi_{iq} = \frac{\tau_q}{\tau_q} = 1$ .

Expanding this further:

$$\begin{aligned} \text{Cov}_\tau(\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k}) &= \sum_i \tau_i (\tilde{\pi}_{ij} - 1) (\tilde{\pi}_{ik} - 1) \\ &= \sum_i \tau_i \tilde{\pi}_{ij} \tilde{\pi}_{ik} - \sum_i \tau_i \tilde{\pi}_{ij} - \sum_i \tau_i \tilde{\pi}_{ik} + \sum_i \tau_i \\ &= \frac{1}{\tau_j \tau_k} \sum_i \tau_i \pi_{ij} \pi_{ik} - 1 - 1 + 1 \\ &= -\frac{1}{\tau_k} d_{jk} - 1 \end{aligned}$$

Rearranging gives equation (6).

### A.1.3 Remark 3 (Individual Own-Price Elasticities)

Turning to the on-diagonal elements of the elasticity matrix D. These are:

$$d_{jj} = \frac{1}{\tau_j} \sum_i \tau_i \pi_{ij} (1 - \pi_{ij})$$

Similar to the above, we can express this in terms of the weighted variance of normalised transition probabilities:

$$\begin{aligned} d_{jj} &= \frac{1}{\tau_j} \sum_i \tau_i \pi_{ij} - \frac{1}{\tau_j} \sum_i \tau_i \pi_{ij}^2 \\ &= 1 - \frac{1}{\tau_j} \sum_i \tau_i \pi_{ij}^2 \\ &= 1 - \frac{1}{\tau_j} \left( \text{Var}_\tau (\pi_{.,j}) + (\mathbb{E}_\tau \pi_{.,j})^2 \right) \\ &= 1 - \frac{1}{\tau_j} \left( \text{Var}_\tau (\pi_{.,j}) + \tau_j^2 \right) \\ &= 1 - \tau_j \left( 1 + \frac{1}{\tau_j^2} \text{Var}_\tau (\pi_{.,j}) \right) \\ &= 1 - \tau_j (1 + \text{Var}_\tau (\tilde{\pi}_{.,j})) \end{aligned} \tag{26}$$

Rearranging gives expression (7).

### A.1.4 Further Discussion on Remarks 1–3

We turn now to justifying our choices of normalisations. We first consider  $\text{Cov}_\tau (\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k}) = \sum_i \tau_i (\tilde{\pi}_{ij} - \mathbb{E}_\tau \tilde{\pi}_{.,j}) (\tilde{\pi}_{ik} - \mathbb{E}_\tau \tilde{\pi}_{.,k})$ . Because  $\mathbb{E}_\tau \tilde{\pi}_{.,j} = \mathbb{E}_\tau \tilde{\pi}_{.,k} = 1$ , we argue this term is invariant to occupation size. To show this empirically, we examine the distribution of this term for occupational classifications at various levels of coarseness. In particular, [Table A.1](#) reports the median across occupations for three levels of aggregation: 4 main groups as described below in [Appendix B](#), 10 occupation groups corresponding to one-digit categories of the 1988 *Klassifikation der Berufe*, and the 120 occupations considered in the analysis (see [Table B.5](#) for the full list).

We now consider the variance terms. We can also write  $d_{jj}$  as follows

$$d_{jj} = - \sum_{k \neq j} d_{jk}$$



$$\begin{aligned}
&= \sum_{k \neq j} \tau_k (1 + Cov_\tau (\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})) \\
&= \sum_{k \neq j} \tau_k + \sum_{k \neq j} \tau_k Cov_\tau (\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k}) \\
&= 1 - \tau_j + \sum_{k \neq j} \tau_k Cov_\tau (\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})
\end{aligned} \tag{27}$$

Equating equations (26) and (27) we see that

$$\begin{aligned}
Var_\tau (\tilde{\pi}_{.,j}) &= -\frac{1}{\tau_j} \sum_{k \neq j} \tau_k Cov_\tau (\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k}) \\
\implies \tau_j Var_\tau (\tilde{\pi}_{.,j}) &= -\sum_{k \neq j} \tau_k Cov_\tau (\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})
\end{aligned}$$

These expressions show two things. First, because  $Var_\tau (\tilde{\pi}_{.,j})$  is necessarily greater than zero, then  $Cov_\tau (\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})$  is below zero on average.<sup>42</sup> Second, if  $Cov_\tau (\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})$  is of order  $\mathcal{O}(1)$ , then  $\frac{1}{\tau_j} \sum_{k \neq j} \tau_k Cov_\tau (\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})$  is of order  $\mathcal{O}(N)$ . In contrast,  $\tau_j Var_\tau (\tilde{\pi}_{.,j}) = -\sum_{k \neq j} \tau_k Cov_\tau (\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})$  is a weighted average of the covariance terms, and so is of order  $\mathcal{O}(1)$ . To show this empirically, [Table A.1](#) also reports the median value across occupations for both measures of the variance, again for the three levels of occupational aggregation.

**Table A.1:** Median Values of Model Components Across Occupation Pairs

# Occs	$Cov(\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})$	$Var(\tilde{\pi}_{.,j})$	$\tau_j Var(\tilde{\pi}_{.,j})$
4	-0.76	2.20	0.54
10	-0.75	5.48	0.58
120	-0.78	126.91	0.57

*Notes:* Variances and covariance computed across sending occupations, given destination occupations  $j$  and  $k$ . Table then shows median values across these destination occupations. The occupations in the aggregation to four broad groups are (1) managers, professionals, and technicians, (2) sales and office workers, (3) production workers, operators, and craftsmen, and (4) workers in services and care occupations. In the ten broad groups, they are 1-digit level occupations as in, e.g. [Acemoglu & Autor \(2011\)](#); [Böhm et al. \(2024\)](#). For further details on occupations and their aggregations see [Section B.1](#).

<sup>42</sup>This also shows that  $\sum_k \tau_k Cov_\tau (\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k}) = 0$ .

## A.2 Remark 4: Vector of Price Changes

This section develops a further result on the aggregation of Remarks 2–3 for individual (own- and cross-price) elasticities. This formalises the effects of the full vector of price changes and provides a rigorous interpretation of overall employment changes in terms of distributions of worker flows.

**Remark 4 (Vector of Price Changes)** *Matrix  $D$  can be expressed as follows*

$$D = I - W - W \otimes C \quad (28)$$

where  $I$  is the identity matrix,  $W$  is the matrix of stationary employment shares with  $j, k$ th element  $\tau_k$ ,  $\otimes$  is the element-by-element product, and  $C$  is the symmetric matrix with  $j, k$ th element  $c_{jk} = \text{Cov}_\tau(\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})$ , which captures the ‘occupational-similarity’ between sectors  $j$  and  $k$ .

Accordingly, following a vector of price changes  $\Delta \mathbf{p}$ , then the change in the employment share in occupation  $j$  is given by

$$\begin{aligned} \Delta e_j &\approx \theta \mathbf{d}_j \Delta \mathbf{p} \\ &= \theta \left( \underbrace{\Delta p_j - \Delta \mathbb{E}_\tau p}_{\text{real price change}} + \underbrace{\text{Cov}_\tau(c_{.,j}, \Delta p_j - \Delta p.)}_{\text{occupational substitutability}} \right) \end{aligned} \quad (29)$$

$$= \theta \left( \underbrace{(1 - \tau_j - \tau_j c_{jj}) \Delta p_j}_{\text{own-occupation effect}} + \underbrace{\sum_{k \neq j} (-\tau_k - \tau_k c_{jk}) \Delta p_k}_{\text{total cross-occupation effect}} \right) \quad (30)$$

where  $\mathbb{E}_\tau p$  is the (weighted) average of prices across occupations and we drop a time subscript for ease of notation. Similarly,  $\text{Cov}_\tau(c_{.,j}, \Delta p_j - \Delta p.)$  captures the (weighted) covariance between the  $j$ -th column of  $C$ ,  $c_{.,j}$ , and the vector of relative price changes  $\Delta p_j - \Delta p.$ .  $\Delta p.$  denotes the vector of price changes across occupations.

Remark 4 complements the interpretations contained in Remarks 2–3. In the formulation in equation (29), the effect of a vector of price changes on a given occupation consists of two components. First is the direct effect of real price changes in that occupation itself, net of the change in the economy-wide price (wage) index. This term aggregates the ‘direct’ and ‘price index’ terms contained in equations (6) and (7). Second is the total effect of occupational substitutabilities: Employment growth is larger if price growth

is higher relative to more similar occupations. In fact, empirically, price changes are positively correlated across similar occupations, and so this last component tends to attenuate the direct effect of price changes. To see this, consider, for example, wage growth in occupations high in analytical tasks. Price growth in these occupations has been highest relative to routine and manual occupations, which saw the largest declines, but which are also dissimilar in terms of occupational flows. Therefore, for these analytical occupations, this last term is likely negative, offsetting the positive effect from the first two terms.

Equation (30) then builds on this formulation by relating it back to equation (9), which forms the basis of our empirical application. Equation (30) therefore expresses the effect of a vector of price changes in terms of two components which we can easily take to data, and which can be interpreted in terms of the joint distribution of these price changes with steady-state job flows.

**Derivation:** The expression

$$D = I - W - W \otimes C$$

follows directly from Remarks 2–3. The diagonal element  $c_{jj}$  of  $C$  is  $Var_{\tau}(\tilde{\pi}_{.,j})$ .

We therefore have that

$$\begin{aligned} \Delta e_j &= \theta \mathbf{d}_j \Delta \mathbf{p} \\ &= \theta \sum_k (i_{jk} - \tau_k - \tau_k c_{jk}) \Delta p_k \\ &= \theta \left( \sum_k i_{jk} \Delta p_k - \sum_k \tau_k \Delta p_k - \sum_k \tau_k c_{jk} \Delta p_k \right) \\ &= \theta \left( \Delta p_j - \Delta \mathbb{E}_{\tau} p - \sum_k \tau_k c_{jk} (\Delta p_k - \Delta p_j) \right) \\ &= \theta (\Delta p_j - \Delta \mathbb{E}_{\tau} p + Cov_{\tau}(c_{.,j}, \Delta p_j - \Delta p)) \end{aligned}$$

as given in the text. The fourth line follows from the third because  $\sum_k \tau_k c_{jk} = 0 \implies \sum_k \tau_k c_{jk} \Delta p_j = 0$ . The final line follows from the fourth because similarly  $\mathbb{E}_{\tau} c_{.,j} = 0$  and column vector  $c_{.,j} = c_{j.}$ , because  $C$  is symmetric.

## B Data Appendix

This section presents a detailed presentation of the data and supplementary descriptive statistics. We first discuss the SIAB data and outline the procedures for sample selection and wage imputation. We then review the data on tasks and occupational characteristics. Finally, we provide descriptive statistics to complement the analysis in Section 3.

### B.1 The SIAB Data

We use the Sample of Integrated Labour Market Biographies (*Stichprobe der Integrierten Arbeitsmarktbiographien*, [Frodermann et al., 2021](#)) for our analyses.<sup>43</sup> The SIAB is a 2% sample of the population of the Integrated Employment Biographies (IEB) provided by the Institute for Employment Research (*Institut für Arbeitsmarkt- und Berufsforschung – IAB*). It includes employees covered by social security, marginal part-time workers (after 1999), unemployment benefit recipients, individuals who are officially registered as job-seeking, and individuals who are participating in programs of active labour market policies. It is possible to track the employment status of a person exact to the day. The source of data regarding employment is the Employee History (*Beschäftigtenhistorik - BeH*) of the IAB. The BeH covers all white- and blue-collar workers as well as apprentices as long as they are not exempt from social security contributions. It excludes civil servants, self-employed people, regular students, and individuals performing military service.

The SIAB data contains an individual’s full employment history, including a consistent-over-time occupational classifier (up to 2010), the corresponding nominal daily wage, and socio-demographic variables such as age, gender, or level of education. Data are available in a spell structure, making it possible to observe the same person at several employers within a year. In a few cases, these spells overlap when workers have multiple employment contracts at a time. We transform the spell structure into a yearly panel by identifying the longest spell within a given year and deleting all the remaining spells (following [Böhm et al., 2024](#)).

#### B.1.1 Sample Selection and Variable Description

To work with a homogeneous sample throughout, the main sample is restricted to West German full-time male workers aged 25–59. Since the level and structure of wages differ substantially between East and West Germany, we drop from our sample all workers who were ever employed in East Germany. Our focus on full-time jobs is driven by the absence of data on hours worked. Excluding younger workers, we ensure the vast majority of our

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<sup>43</sup> Access to the data is subject to signing a contract with the Research Data Centre (FDZ) of the German Federal Employment Agency (BA) at the Institute for Employment Research (IAB).

sample will have concluded their formal education by the time they enter the sample. Besides, we stop relatively early (at 59) because early retirement programs were common in Germany, particularly in the late 1970s and the 1980s.

We further exclude workers with wages below the limit for which social security contributions have to be paid, mainly workers in marginal jobs (also known as mini-jobs). These jobs were not subject to social security taxation prior to 1999. After the first reform in 1999, the tax-free wage threshold was fixed during the period 1999 to 2003 at 325 euro per month. In 2003, the range of exempted earnings was expanded up to 400 euro, which was effective until 2012. The minimum threshold for mini-jobbers increased in 2013 from 400 to 450 euro per month. Approximately 10% of observations are affected by this restriction. We drop wage spells of workers whose last spell is in apprenticeship training as the first wage after apprenticeship is often a mixture between new wage and apprenticeship wage (this only affects 0.48% of the sample). We also drop all spells of workers who are always foreign workers (less than 5% of observations).<sup>44</sup> Finally, workers without information on their occupation or wages are dropped from the analysis.

**Occupation classification.** We use the 120 three-digit occupations from the SIAB's Scientific Use File as our main units of analysis. These occupations are consistently coded (from the detailed KldB 1988 classification system), available during the long period of 1975–2010, and listed in [Table B.5](#). After 2010, SIAB uses a new classification system, which results in a relatively sharp break of the occupation codes. In [Appendix Table A.1](#), we also consider occupations at the 1-digit level and aggregate them into four broad groups following the literature ([Acemoglu & Autor, 2011](#); [Böhm et al., 2024](#)). These are (1) managers, professionals, and technicians (Mgr-Prof-Tech), (2) sales and office workers (Sales-Office), (3) production workers, operators, and craftsmen (Prod-Oper-Crafts), and (4) workers in services and care occupations (Serv-Care).

**Wages.** The available wage variable is the employee's gross daily nominal wage in euro. It is calculated from the fixed-period wages reported by the employer and the duration of the original notification period in calendar days. Despite being accurately measured as the employer can be punished for incorrect reporting, two major drawbacks are of special relevance to our analysis. First, due to a cap on social security contributions, wages are right-censored. As is common in administrative data sources, earnings above the upper earnings limit for statutory pension insurance are only reported up to this limit. The upper earnings limit for statutory pension insurance differs from year to year as well as between East and West Germany, where the decisive factor is the location of the establish-

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<sup>44</sup>Workers who are classified as German at some point but foreign at another are not dropped from the sample.

ment. Second, the income components being subject to social security tax were extended in 1984. Prior to that, one-time payments such as bonuses were not included in the daily wage benefit measure. We further discuss how we deal with these two issues below. Finally, to ensure comparability across years, wages are deflated by the Consumer Price Index reported in the Federal Statistical Office of Germany, with 2010 as the base year.

### B.1.2 Imputation of Right-Censored Wages

The SIAB data is based on process data used to calculate retirement pensions and unemployment insurance benefits, implying the wage information is top-coded and only relevant up to the social security contribution ceiling. While this feature only affects approximately 8.5% of observations on average across years in our main sample (25–59 years old, full-time, excluding marginal workers), the proportion of censored observations differs across subgroups. By gender, top-coded wages amount to roughly 11% for men and 3.3% for women. Differences are also substantial by education groups. Whereas only 1.1% of the spells of individuals who enter the labour market without post-secondary education are affected by top-coding, the share of right-censored wages increases to 5.2%, 9.4%, and 30.8% for those who completed vocational education and training, an *Abitur*, and a university degree, respectively. The share of top-coded wages also increases over the life cycle. While censoring only affects less than 2% of observations for those aged 25–29, the fraction of top-coded wages rises to more than 11% for those older than 40.

To impute top-coded wages, we follow [Dustmann et al. \(2009\)](#) and [Card et al. \(2013\)](#).<sup>45</sup> We first define age-education cells based on seven age groups (with 5-year intervals; 25–29; 30–34; 35–39; 40–44; 45–49; 50–54; 55–59) and four education groups (as described above). Within each of these cells (and thereby allowing a different variance for each education and age group), we estimate Tobit wage equations separately by year, gender, and East-West Germany. We predict the upper tail of the wage distribution including controls for age (quadratic), tenure (quadratic), a part-time dummy, as well as interactions between age (quadratic) and the different education groups. To control for worker fixed effects, we construct the mean of an individual’s log wage in other years, the fraction of censored wages in other years, and a dummy variable if the person was only observed once in her life.<sup>46</sup> We use the predicted values  $X'\hat{\beta}$  from the Tobit regressions together with the estimated standard deviation  $\hat{\sigma}$  to impute the censored log wages  $y^c$  as follows:

$$y^c = X'\hat{\beta} + \hat{\sigma}\Phi^{-1}[k + u(1 - k)]$$

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<sup>45</sup>To ensure that all censored wages are covered in the imputation procedure, we mark all observations with wages four euro below the assessment ceiling as in [Dauth & Eppelsheimer \(2020\)](#).

<sup>46</sup>For those observed only once, the mean wage and mean censoring indicator are set to sample means.

where  $\Phi$  is the standard normal density function,  $u$  is a random draw from a uniform distribution ranging between zero and one,  $k = \Phi[(c - X'\hat{\beta})/\hat{\sigma}]$  and  $c$  is the censoring point, which differs by year and East-West Germany. See [Gartner \(2005\)](#) for further details.<sup>47</sup> In a very few cases ( $< 0.001\%$ ), imputed wages are exceedingly high. As a minor adjustment, we limit imputed wages to ten times the 99th percentile of the latent wage distribution.

### B.1.3 The Structural Wage Break 1983/1984

The income components being subject to the social security tax were extended in Germany in 1984 (for further details, see [Bender et al. \(1996\)](#) and [Steiner & Wagner \(1998\)](#)). Before 1984, one-time payments, such as bonuses, were not included in the daily wage benefit measure. Starting in 1984, these variable parts of the wage were included. We follow [Fitzenberger \(1999\)](#) and [Dustmann et al. \(2009\)](#) and deal with this structural break by correcting wages prior to 1984 upwards. The correction is based on the idea that higher quantiles appear to be more affected by the structural break than lower quantiles, as higher percentiles are likely to receive higher bonuses. To this end, we estimate locally weighted regressions, separately for men and women, of the wage ratio between 1982 and 1983 (i.e., before the break), and between 1983 and 1984 (i.e., after the break) on the wage percentiles in 1983 and 1984, respectively. The correction factor is then computed as the difference between the predicted, smoothed values from the two wage ratio regressions. In a way similar to that of [Dustmann et al. \(2009\)](#), to account for differential overall wage growth between the periods from 1982 to 1983 and from 1983 to 1984, we subtract from the correction factor the smoothed value of the wage ratio in 1983, averaged between the second and fortieth quantiles. Finally, wages prior to 1984 are corrected by multiplying them by 1 plus the correction factor. After this, some wages are corrected above the censoring limit. [Dustmann et al. \(2009\)](#) reset these wages back to the censoring limit and impute them in the same way they imputed wages that were above the limit anyway. Instead of doing that, here we follow [Böhm et al. \(2024\)](#) and do not reset wages back to the censoring limit if they were corrected above the limit but leave them at their break corrected values.

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<sup>47</sup>[Dustmann et al. \(2009\)](#) consider different imputation methods, such as restricting the variance to be the same across all education and age groups, or assuming the upper tail of the wage distribution follows a Pareto distribution. They conclude that the imputation method that assumes that the error term is normally distributed with a different variance by age and education works better than the other imputation methods. This method is also chosen in more recent papers such as [Cortes et al. \(2024\)](#) and [Böhm et al. \(2024\)](#).

## B.2 Data on Tasks and Occupational Characteristics

We use the Qualifications and Career Surveys (QCS, [Hall et al., 2012](#)), conducted by the Federal Institute for Vocational Education and Training (BiBB), to obtain information on tasks performed in occupations. The QCS, which have been previously used, e.g. by [Spitz-Oener \(2006\)](#); [Antonczyk et al. \(2009\)](#); [Gathmann & Schönberg \(2010\)](#), are representative cross-sectional surveys with 20,000–35,000 individuals in each wave who respond about the tasks required in their occupations. These include, for example, how often they repair objects, how often they perform fraction calculus, or how often they have to persuade co-workers. We classify questions as representing either analytical, interactive, routine, or manual tasks and assign a value of 0, 1/3, or 1, depending on whether the answer is ‘never’, ‘sometimes’, or ‘frequently’. We pool the QCS waves in 1979 and 1985/1986 to compute task intensities across occupations by averaging over all the responses. We use this information to study how task intensity relates to our price elasticity measures, and instrument demand changes across occupations over the period 1985-2010.

**Task distance.** To measure the distance between occupations in the task space (reflecting the degree of dissimilarity in the mix of tasks), we follow [Cortes & Gallipoli \(2018\)](#) and use the angular separation (correlation) of the observable vectors  $x_j$  and  $x_k$ .<sup>48</sup>

$$\text{AngSep}_{jk} = \frac{\sum_{a=1}^A (x_{aj} \cdot x_{ak})}{\left[ \sum_{a=1}^A (x_{aj})^2 \cdot \sum_{a=1}^A (x_{ak})^2 \right]^{\frac{1}{2}}} \quad (31)$$

where  $x_{aj}$  is the intensity of task dimension  $a$  in occupation  $j$  and  $A$  is the total number of dimensions being considered (analytical, routine, and manual). We transform this to a distance measure  $dist_{jk}$  that is increasing in dissimilarity:

$$dist_{jk} = \frac{1}{2}(1 - \text{AngSep}_{jk})$$

The measure varies between zero and one; it will be closer to zero the more two occupations overlap in their skill requirements. The mean task distance between occupations in our data is 0.5, with a standard deviation of 0.29. The most distant possible move is between an ‘economic and social scientist’ and a carpenter. Examples of pairs of occupations with low distance measures are between a sheet metal worker and a tile setter, or between a glass processor and a plastic processor.

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<sup>48</sup>The angular separation is the cosine angle between the occupations’ vectors in the task space.



**Occupational licensing.** To obtain measures of occupational licensing, we use the indicators for *standardised certification* requirements and degree of *regulation* developed by [Vicari \(2014\)](#). These indicators are based on BERUFENET, the online career information portal provided by the German Federal Employment Agency – a rich job title database similar to the US O\*NET. They are calculated by categorising very narrow occupations (8-digit) based on the presence or absence, under federal or state law, of standardised training certificates required for professional activities. This is done in three steps. First, each 8-digit occupation is assigned a value of 0 or 1 based on whether the access to the occupational activity is linked to standardised credentials. Second, each occupation is merged with the feature ‘regulation’, i.e. whether legal and administrative regulations exist for an occupation and whether a specific qualification is necessary to practice it. Finally, the indicator ‘standardised certification’ uses both pieces of information about the standardisation of the credentials and regulation. These 0-1 values are finally aggregated at the 3-digit occupational classification (i.e. the 120 occupations used in our analysis), weighted by the number of individuals employed in each occupation. Intuitively, the degree of regulation indicates whether legal and administrative regulations exist which bind the access to and practice of the occupation, including the necessity of holding a specific title as proof of competence. The occupational certification further includes whether access to exercising the professional activity is linked to a standardised training credential. These indicators are constructed as a metric value between 0 and 1, with the indicator increasing in the degree of certification and regulation.

### B.3 Descriptive Statistics

This section presents descriptive statistics to complement the analysis in Section 3.

[Table B.1](#) shows summary statistics for the 120 occupations. In the top panel, we see that variation of employment growth in the cross-section of occupations is substantial, with 10th percentile occupations shrinking at 1.8 log points annually (averaged over the period 1985–2010) and 90th percentile occupations growing at 2.4 log points, respectively. When weighting by initial size, the negative average employment growth partly stems from the fact that formerly large manufacturing- and craft-related occupations have shrunk over time.<sup>49</sup> Second, annualised occupational price growth, as given by our preferred measure (wage growth of stayers in the occupation), is positive at 0.59 log points, again with considerable variation around this average (-0.96 and +2.17 log points for occupations at the 10th and 90th percentile, respectively). Only slightly less variation is found for our alternative measure of occupational prices à la [Cortes \(2016\)](#).

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<sup>49</sup>The results of our main analyses do not substantively differ whether we weight occupations by their initial size or not.

The middle panel of [Table B.1](#) shows, among others, the distribution of occupational certification and regulation (coded between 0 and 1) and the shares of workers with university degrees. The bottom panel shows task intensities (analytical, routine, manual) across the 120 occupations. Consistent with earlier work ([Gathmann & Schönberg, 2010](#)), there exists substantial variation. For example, the median occupation is more than twice as routine-intensive as the occupation at the lowest decile. Task distance is normalised between zero and one, and best interpreted as a ranked ordinal variable (see its construction in the previous section). Still, the table reports e.g. distance at the 10th percentile (i.e. occupations using relatively similar task sets) and at the 90th percentile (occupations using rather different task sets).

**Table B.1:** Summary Statistics for the 120 Occupations.

	Mean	Weighted Mean	Std.Dev.	p10	p50	p90	Observ.
<b>Annualised Employment and Occupational Price Changes (1985-2010)</b>							
Log Employment	0.107	-0.123	1.921	-1.843	-0.065	2.369	120
Prices: Stayers' Wage Growth	0.586	0.516	1.354	-0.959	0.408	2.168	120
Prices: à la <a href="#">Cortes (2016)</a>	1.102	1.065	0.953	-0.009	0.949	2.308	120
<b>Other Occupational Characteristics</b>							
Initial Employment Size in 1985 (%)	0.833	1.763	0.883	0.213	0.543	1.639	120
Employment Size in 2010 (%)	0.833	1.789	1.030	0.193	0.501	1.738	120
Occupational Certification	0.712	0.751	0.258	0.290	0.810	0.970	120
Occupational Regulation	0.103	0.079	0.228	0	0	0.380	120
Share of University Degree (%)	0.135	0.117	0.232	0.006	0.018	0.463	120
Mean Workers' Age	40.55	40.92	1.68	38.59	40.46	42.35	120
<b>Task Intensity and Distance</b>							
Analytical	0.069	0.064	0.075	0.010	0.039	0.181	120
Manual	0.095	0.089	0.071	0.016	0.075	0.186	120
Routine	0.151	0.153	0.079	0.062	0.131	0.271	120
Task Distance	0.499	0.497	0.296	0.061	0.541	0.870	14280
Proxy for demand shocks $r$	0.177	0.178	0.149	-0.037	0.217	0.326	120

*Notes:* The table presents summary statistics for annualised employment and occupational price changes during 1985–2010, occupational characteristics (e.g., the share of workers with university degrees by occupation), and task content information (i.e., analytical, manual, routine, and task distance). The last row presents the summary statistics for our proxy of demand shocks  $r$  used in Section 5. The weighted mean is weighted by each occupation's employment share in 1985.

Table B.2 displays summary statistics for annualised employment and occupational price changes separately by each five-year sub-period from 1985 to 2010. We see substantial variation over time: e.g. average wage and employment growth was substantially faster in the pre-unification years 1985–1990 and turned negative in the economically sluggish early 2000s.

**Table B.2:** Summary Statistics. Annualised Employment and Occupational Price Changes by Sub-Periods

	Mean	Weighted Mean	Std.Dev.	p10	p50	p90	Autocorr. with 5-yr lag
<b>Panel A. 1985–1990</b>							
$\Delta e$ (Log empl. change)	2.59	2.28	2.57	−0.15	2.32	5.72	-
$\Delta p$ (Stayers' Wages)	2.10	2.08	1.44	0.40	1.85	4.07	-
$\Delta p$ (à la Cortes, 2016)	2.38	2.38	1.19	0.99	2.23	4.08	-
<b>Panel B. 1990–1995</b>							
$\Delta e$	0.05	0.13	2.51	−3.13	−0.25	3.62	0.56
$\Delta p$ (Stayers' Wages)	0.17	0.11	1.36	−1.33	−0.04	1.97	0.84
$\Delta p$ (à la Cortes, 2016)	0.58	0.50	1.09	−0.71	0.33	2.11	0.75
<b>Panel C. 1995–2000</b>							
$\Delta e$	−0.19	−0.24	2.67	−2.87	−0.46	2.71	0.46
$\Delta p$ (Stayers' Wages)	0.48	0.52	1.79	−1.57	0.25	2.56	0.83
$\Delta p$ (à la Cortes, 2016)	0.75	0.82	1.51	−0.97	0.56	2.50	0.75
<b>Panel D. 2000–2005</b>							
$\Delta e$	−1.64	−1.43	2.27	−4.49	−1.46	1.35	0.71
$\Delta p$ (Stayers' Wages)	−0.24	−0.17	1.32	−1.90	−0.24	1.51	0.84
$\Delta p$ (à la Cortes, 2016)	0.09	0.12	1.07	−1.15	0.01	1.54	0.82
<b>Panel E. 2005–2010</b>							
$\Delta e$	−0.27	−0.04	2.18	−3.07	−0.31	2.07	0.59
$\Delta p$ (Stayers' Wages)	0.42	0.61	1.38	−1.14	0.12	2.17	0.77
$\Delta p$ (à la Cortes, 2016)	0.57	0.76	1.25	−0.88	0.22	2.25	0.82

*Notes:* The table presents summary statistics for annualised employment and occupational price changes for different 5-year periods. The last column refers to the autocorrelation between that period and the preceding 5-year period, e.g. the autocorrelation of employment changes between 1990-1995 relative to employment changes in 1985-1990.

Table B.3 presents summary statistics for the transition probability matrix,  $\Pi$ , and the elasticity matrix,  $D$ . Diagonal elements (i.e., probabilities for staying and own-price elasticities) are on average substantially larger than off-diagonal elements (for switching occupations and cross-price elasticities). However, dispersions of off-diagonal elements are higher relative to their means and skewness is clearly substantial in these variables. As discussed in the main text, cross-elasticities at the top of the distribution are as high as

some of the own-elasticities, but thereafter fall off very rapidly in size. For example, the 99th percentile cross-elasticity (0.04 in [Table B.3](#)) is already somewhat lower than the minimum own-elasticity (0.07 in [Table 1](#)).

The persistence of elasticity components across time is also shown in [Table B.3](#). In particular, the matrix of elasticities is constructed for different five-year periods (1975–1980, . . . , 2000–2005, 2005–2010), and then the relation of the respective own-elasticities and cross-elasticities (the matrix elements) are separately studied across those periods. Autocorrelations turn out high, in the range of 0.75–0.90 even for the long time distances between the early and late periods. This is consistent with the high autocorrelation of occupational task contents reported in [Gathmann & Schönberg \(2010\)](#) and with the findings in [Section 7](#) when estimating our model pooled in these five-year sub-periods.

**Table B.3:** Summary Statistics. Elasticity Matrix and Transition Probability Matrix

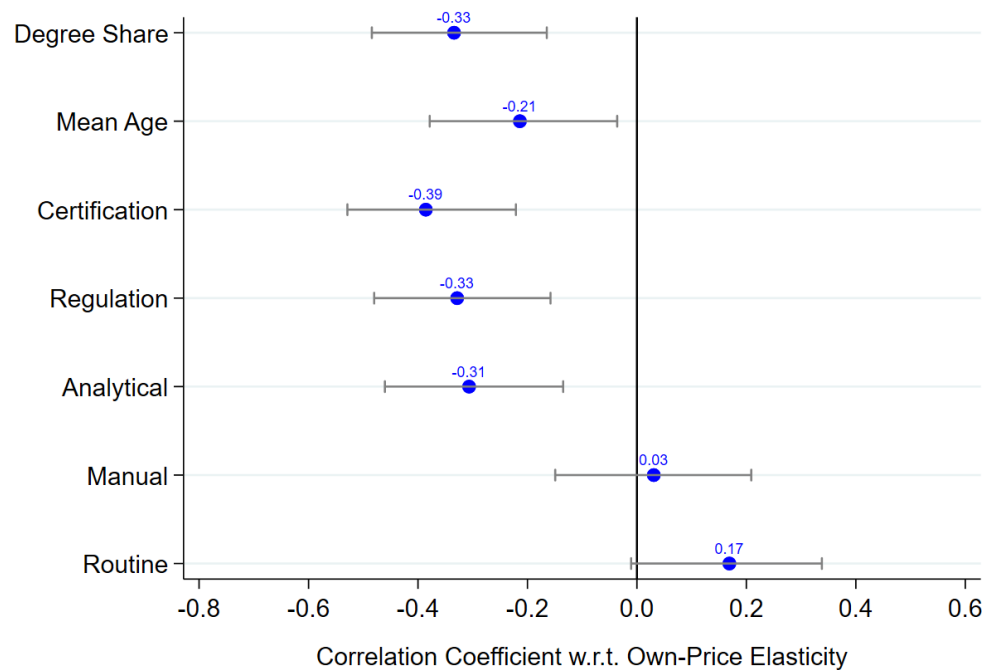
	Elasticity Matrix $D$		Transition Probability Matrix $\Pi$	
	Own-Price	Cross-Price	Diagonal	Off-Diagonal
	Elasticity ( $d_{jj}$ )	Elasticity ( $-d_{jk} \times 100$ )	Elements ( $\pi_{jj}$ )	Elements ( $\pi_{jk} \times 100$ )
Mean	0.434	0.364	0.746	0.214
Std. Dev.	0.128	0.939	0.090	0.660
Variance	0.016	0.882	0.008	0.436
Skewness	0.177	14.672	-0.722	17.449
Kurtosis	3.634	493.494	4.393	585.670
p10	0.294	0.007	0.627	0.000
p50	0.430	0.111	0.754	0.046
p90	0.604	0.867	0.839	0.516
p99	0.796	4.021	0.931	2.585
Average autocorr. 5-year	0.876	0.881	0.868	0.806
Autocorrelation 25-year	0.761	0.768	0.761	0.660
Number of Observations	120	14,280	120	14,280

*Notes:* The table presents summary statistics for the elasticity matrix  $D$  ([Remark 1](#)) and the transition probability matrix. The average (5-year period) autocorrelation is computed by averaging autocorrelations of reported variables between 1985–1990 and 1980–1985, 1990–1995 and 1985–1990, 1995–2000 and 1990–1995, and so on. The 25-year autocorrelation refers to the autocorrelation between the later period 2005–2010 and the earlier period 1980–1985.

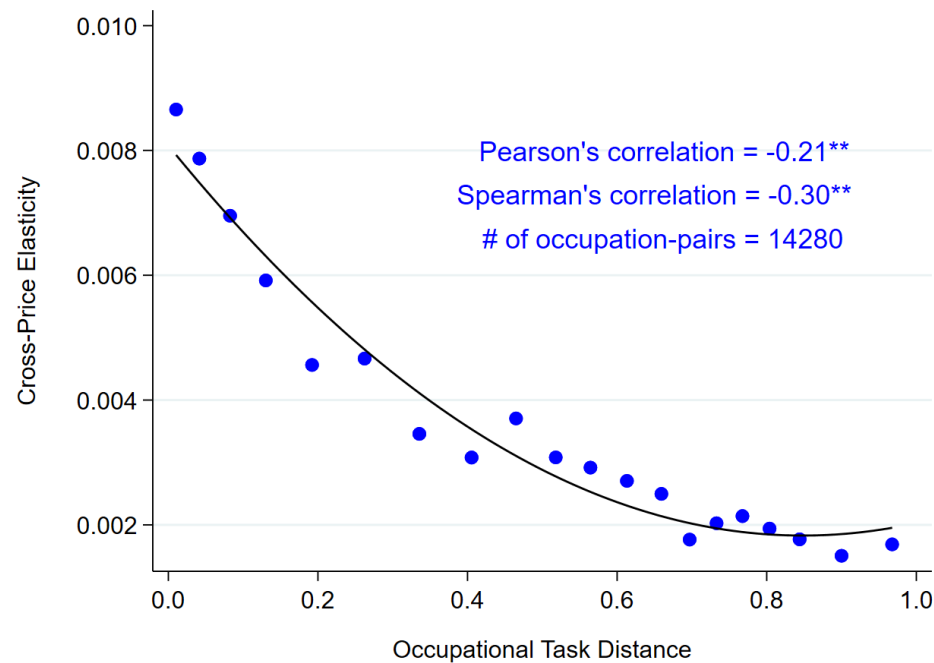
We show how own-price elasticities  $d_{jj}$  relate to several occupational characteristics in [Figure B.1a](#). These include the share of workers with university degrees, workers’ mean age, occupational certification and regulation as well as analytical, routine, and manual task intensities. Panel (b) of [Figure B.1](#) plots cross-price elasticities against occupational task distance.

**Figure B.1:** Own-Price and Cross-Price Elasticity: Comparison with External Metrics

**(a)** Own-Price Elasticity and Occupational Characteristics



**(b)** Cross-Price Elasticity and Task Distance



Notes: Panel (a) reports how own-price elasticity, namely  $d_{jj}$ , correlates with skill requirements across 120 occupations. Occupational certification and regulations come from [Vicari \(2014\)](#). Task content (analytical, manual, and routine) are measured using BiBB, see [Appendix B.2](#). Correlations weighted by initial employment in each occupation. Panel (b) shows the relationship (with a quadratic fit) between cross-price elasticity, namely  $-d_{jk}$ , and occupational task distance measured as in [Cortes & Gallipoli \(2018\)](#).

Table B.5 below offers the full list of the 120 occupations ranked by their respective own-price elasticities, together with their employment sizes in 1985 and 2010. The table also reports own-price elasticities when including transitions to and from three major non-employment states in the model. This is analysed in detail in Appendix F.1.

Finally, we decompose the variation of labour supply elasticities. The second column of Table B.3 shows that occupational cross-price elasticities are strongly skewed and with high kurtosis. Figure B.2 shows that they also distributed approximately *log*-normally.<sup>50</sup> Accordingly, we decompose the log of the cross-price elasticities using the expression in Remark 2 as follows:

$$\ln(-d_{jk}) = \ln(\tau_k) + \ln(\text{Cov}_\tau(\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k}) + 1)$$

Here, the variance of log differences in cross-price elasticities can be decomposed into variances of log differences in sector sizes and occupational similarities (plus one, to make them all positive). Table B.4 shows that in fact most of the dispersion of  $\ln(-d_{jk})$ , and hence the skewness in levels of  $d_{jk}$ , is driven by the dispersion of  $\ln(\text{Cov}_\tau(\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k}) + 1)$ , while the dispersion in log occupational sizes contributes less than 30%. Although not shown in Table B.4, but can be easily inferred, the covariance of log occupational size with the similarity term is negligible. Such covariance terms are often important in models of matching between worker and employer types, generating skewed wage distributions (e.g. [Sattinger, 1993](#)). Here, this interaction does not matter and cross-elasticities largely inherit their distribution from the occupational similarities.

Own-elasticities are distributed approximately normally in *levels*. In fact, here a formal test fails to reject normality based on the skewness and kurtosis reported in Table B.3 above.<sup>51</sup> Although we do not explore the reason for this feature rigorously here, we conjecture it is because own-price elasticities comprise the sum of many apparently independently-distributed terms, as Remark 3 indicates. In line with this feature, and with the first expression of Remark 3, we decompose this elasticity as:

$$d_{jj} = \underbrace{\sum_{k \neq j} \tau_k \text{Cov}_\tau(\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k})}_{\text{aggregate substitutability}} + \underbrace{1}_{\text{direct}} - \underbrace{\tau_j}_{\text{price index}}$$

As Table B.4 shows, and consistent with the discussion in the main text, the variation in aggregate substitutabilities is by far the dominant component of the variance of own-price

<sup>50</sup>A formal skewness-kurtosis test of normality of the logs is strongly rejected. This is not surprising, however, given the large number of observations and so the high precision of the test.

<sup>51</sup> $p$ -value on the skewness test is 0.40, with a  $p$ -value on the kurtosis test of 0.13. It should be remarked however, that this test is based on far fewer observations than that for the cross-price elasticities.

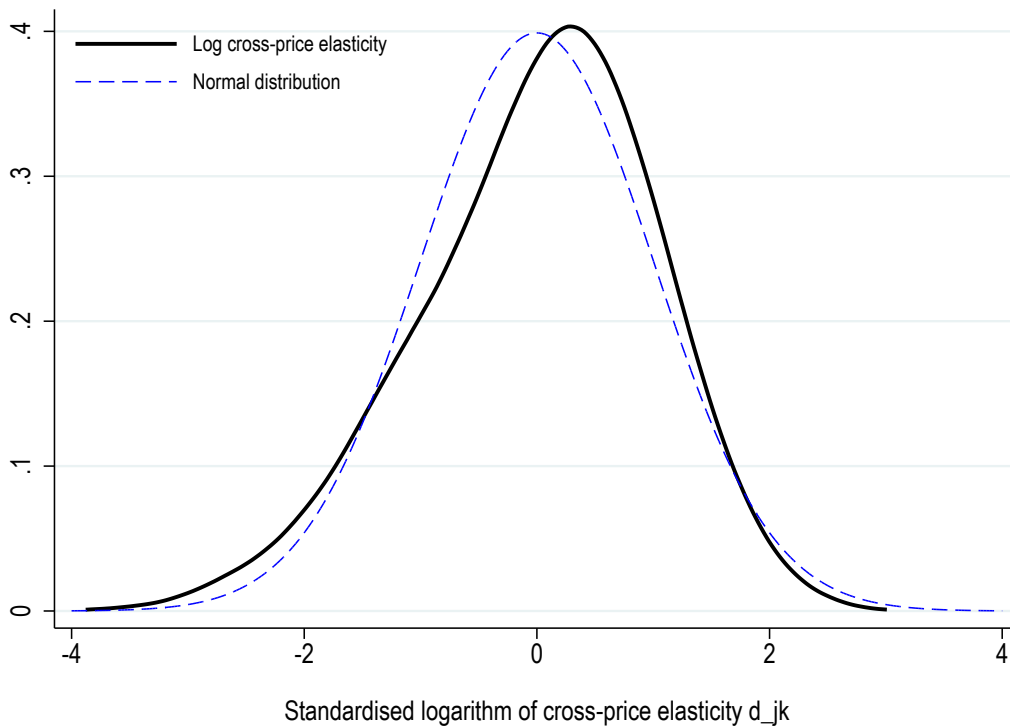
elasticities. Compared to this, the variation in occupation sizes and its covariance with aggregate substitutability are minuscule.

**Table B.4:** Summary Statistics. Elasticity Components

	Mean	Std. Dev.	Variance	Min	p10	p50	p90	Max	Skewness
<b>Own-Price Elasticity (<math>d_{jj}</math>)</b>									
Aggregate Substitutability	-0.558	0.126	0.0161	-0.918	-0.692	-0.565	-0.389	-0.202	0.131
Stationary Employment Size	0.008	0.012	0.0001	0.001	0.002	0.004	0.017	0.090	4.360
<b>Cross-Price Elasticity (<math>-d_{jk}</math>)</b>									
Occupational Similarity	-0.429	2.418	5.848	-0.999	-0.979	-0.779	0.203	129.849	36.912
<b>Log of components:</b>									
Cross-Price Elasticity		1.917	3.676						-0.479
Stationary Employment Size		1.072	1.150						-0.488
Occupational Similarity + 1		1.582	2.504						-0.259

*Notes:* The table presents summary statistics for the elasticity components of the own-price elasticity (as discussed in Remark 3) and cross-price elasticity (as discussed in relation to Remark 2). The number of observations is 120 for own-price elasticity and its components, while it is 14280 for cross-price elasticity and its components.

**Figure B.2:** Kernel Density of Log Cross-Price Elasticity



*Notes:* The figure shows the kernel density of the (standardised to have mean zero and standard deviation one) log of cross-price elasticity, superimposing a normal distribution. Bandwidth is 0.3.

**Table B.5.** All 120 Occupations Ranked by Diagonal Elements  $d_{jj}$ , and their Employment Size

Occupations (based on German KIDB 1988 Classification)	Own-Price Elasticity		% Share of Employment	
	$d_{jj}$	$d_{jj}^{NE}$	1985	2010
Physicians up to Pharmacists	0.07	0.27	0.65	0.81
Bank specialists up to building society specialists	0.13	0.18	1.79	1.98
Nurses, midwives	0.16	0.24	0.37	0.67
Dental technicians up to doll makers, model makers, taxidermists	0.18	0.31	0.32	0.24
Non-medical practitioners up to masseurs, physiotherapists and related occupations	0.19	0.27	0.13	0.22
Journalists up to librarians, archivists, museum specialists	0.20	0.28	0.28	0.35
Hairdressers up to other body care occupations	0.23	0.37	0.06	0.06
Architects, civil engineers	0.23	0.30	0.83	0.69
Soldiers, border guards, police officers up to judicial enforcers	0.27	0.36	0.38	0.51
Musicians up to scenery/sign painters	0.28	0.39	0.29	0.31
Foremen, master mechanics	0.29	0.37	1.39	0.75
Health insurance specialists (not social security) up to life, property insurance specialists	0.29	0.37	0.85	0.89
Chemical laboratory assistants up to photo laboratory assistants	0.30	0.33	0.26	0.25
Doormen, caretakers up to domestic and non-domestic servants	0.30	0.40	0.97	0.97
Type setters, compositors up to printers (flat, gravure)	0.31	0.35	0.75	0.36
Gardeners, garden workers up to forest workers, forest cultivators	0.31	0.40	1.18	1.15
Social workers, care workers up to religious care helpers	0.31	0.39	0.42	0.68
Carpenters	0.32	0.39	1.57	1.17
Tile setters up to screed, terrazzo layers	0.33	0.43	0.42	0.30
Nursing assistants	0.33	0.42	0.20	0.33
Mechanical, motor engineers	0.33	0.38	1.07	1.21
Electrical fitters, mechanics	0.33	0.38	2.78	2.76
Chemists, chemical engineers up to physicists, physics engineers, mathematicians	0.33	0.39	0.35	0.34
Bricklayers up to concrete workers	0.34	0.43	2.95	1.20
Home wardens, social work teachers	0.34	0.41	0.28	0.46
Music teachers, n.e.c up to other teachers	0.34	0.41	0.27	0.32
Electrical engineers	0.34	0.37	1.00	1.18
Entrepreneurs, managing directors, divisional managers	0.34	0.43	2.63	2.11
Data processing specialists	0.35	0.38	1.18	3.46
Members of Parliament, Ministers, elected officials up to association leaders, officials	0.36	0.46	0.33	0.48
Measurement technicians up to remnining manufacturing technicians	0.36	0.41	0.81	0.48
Painters, lacquerers (construction)	0.36	0.43	1.11	0.91
Office specialists	0.36	0.43	6.10	8.15
Dietary assistants, pharmaceutical assistants up to medical laboratory assistants	0.36	0.38	0.03	0.05
Chemical plant operatives	0.36	0.43	1.25	0.97
Navigating ships officers up to air transport occupations	0.37	0.45	0.39	0.28
Paper, cellulose makers up to other paper products makers	0.37	0.44	0.53	0.50
Artistic and audio, video occupations up to performers, professional sportsmen, auxiliary artistic occupations	0.37	0.44	0.27	0.25
Motor vehicle drivers	0.38	0.44	5.57	5.39
Toolmakers up to precious metal smiths	0.38	0.43	1.13	0.80
Cost accountants, valuers up to accountants	0.38	0.45	0.82	0.51
Railway engine drivers up to street attendants	0.39	0.47	0.77	0.61
Bakery goods makers up to confectioners (pastry)	0.39	0.46	0.41	0.41
Other technicians	0.39	0.45	1.96	2.43
Commercial agents, travellers up to mobile traders	0.39	0.45	1.58	1.10
Miners up to shaped brick/concrete block makers	0.40	0.47	1.33	0.47
Roofers	0.40	0.49	0.37	0.40
Survey engineers up to other engineers	0.40	0.46	0.75	1.82
Plumbers	0.40	0.46	1.35	1.23
Technical draughtspersons	0.40	0.45	0.60	0.48



**Table B.5—continued**

Occupations (based on German KIDB 1988 Classification)	Own-Price Elasticity		% Share of Employment	
	$d_{jj}$	$d_{jj}^{NE}$	1985	2010
Biological specialists up to physical and mathematical specialists	0.40	0.45	0.30	0.20
Mechanical engineering technicians	0.41	0.45	0.91	0.82
Butchers up to fish processing operatives	0.41	0.48	0.65	0.47
Turners	0.41	0.46	0.97	0.73
Generator machinists up to construction machine attendants	0.42	0.48	1.42	0.73
Goods examiners, sorters, n.e.c	0.42	0.49	0.90	0.58
Ceramics workers up to glass processors, glass fishers	0.42	0.49	0.40	0.22
Agricultural machinery repairers up to precision mechanics	0.42	0.46	0.53	0.54
Machine attendants, machinists' helpers up to machine setters (no further specification)	0.43	0.50	0.58	0.51
Stucco workers, plasterers, rough casters up to insulators, proofers	0.43	0.50	0.53	0.32
Metal grinders up to other metal-cutting occupations	0.43	0.49	0.50	0.35
Cooks up to ready-to-serve meals, fruit, vegetable preservers, preparers	0.43	0.54	0.62	1.05
Spinners, fibre preparers up to skin processing operatives	0.43	0.50	0.56	0.19
Motor vehicle repairers	0.43	0.48	1.63	1.65
Goods painters, lacquerers up to ceramics/glass painters	0.44	0.49	0.50	0.37
Chemical laboratory workers up to vulcanisers	0.44	0.51	0.41	0.30
Cutters up to textile finishers	0.44	0.52	0.24	0.08
Cashiers	0.44	0.51	0.10	0.07
Street cleaners, refuse disposers up to machinery, container cleaners and related occupations	0.44	0.51	0.63	0.72
Drillers up to borers	0.44	0.50	0.59	0.41
Iron, metal producers, melters up to semi-finished product fettlers and other mould casting occupations	0.45	0.52	0.96	0.60
Electrical engineering technicians up to building technicians	0.45	0.48	1.39	1.47
Wine coopers up to sugar, sweets, ice-cream makers	0.45	0.52	0.46	0.37
Room equippers up to other wood and sports equipment makers	0.45	0.51	0.39	0.27
Plant fitters, maintenance fitters up to steel structure fitters, metal shipbuilders	0.45	0.51	2.18	1.36
Carpenters up to scaffolders	0.46	0.53	0.63	0.49
Post masters up to telephonists	0.46	0.57	0.30	0.36
Forwarding business dealers	0.46	0.51	0.42	0.47
Engine fitters	0.47	0.50	2.04	1.43
Farmers up to animal keepers and related occupations	0.47	0.55	0.49	0.42
Welders, oxy-acetylene cutters	0.47	0.52	0.72	0.51
Telecommunications mechanics, craftsmen up to radio, sound equipment mechanics	0.47	0.52	0.82	0.45
Steel smiths up to pipe, tubing fitters	0.47	0.53	0.58	0.34
Wood preparers up to basket and wicker products makers	0.48	0.56	0.48	0.26
Office auxiliary workers	0.49	0.57	0.34	0.31
Sheet metal workers	0.49	0.55	0.40	0.36
Wholesale and retail trade buyers, buyers	0.51	0.55	1.65	1.88
Factory guards, detectives up to watchmen, custodians	0.51	0.59	0.67	0.67
Special printers, screeners up to printer's assistants	0.51	0.56	0.35	0.21
Sheet metal pressers, drawers, stampers up to other metal moulders (non-cutting deformation)	0.51	0.56	0.53	0.32
Paviours up to road makers	0.52	0.59	0.49	0.32
Tourism specialists up to cash collectors, cashiers, ticket sellers, inspectors	0.53	0.59	0.49	0.65
Tracklayers up to other civil engineering workers	0.53	0.61	0.78	0.32
Metal polishers up to metal bonders and other metal connectors	0.53	0.58	0.44	0.28
Management consultants, organisers up to chartered accountants, tax advisers	0.53	0.58	0.41	1.29
Transportation equipment drivers	0.53	0.58	0.52	0.45
Warehouse managers, warehousemen	0.54	0.61	2.21	1.58
Housekeeping managers up to employees by household cheque procedure	0.54	0.63	0.05	0.08
University teachers, lecturers at higher technical schools up to technical, vocational, factory instructors	0.54	0.60	0.38	0.50
Economic and social scientists, statisticians up to scientists	0.56	0.62	0.35	0.57
Stowers, furniture packers up to stores/transport workers	0.56	0.64	1.95	2.91

**Table B.5—continued**

Occupations (based on German KIDB 1988 Classification)	Own-Price Elasticity		% Share of Employment	
	$d_{jj}$	$d_{jj}^{NE}$	1985	2010
Stenographers, shorthand-typists, typists up to data typists	0.56	0.61	0.11	0.12
Other mechanics up to watch-, clockmakers	0.56	0.59	0.45	0.79
Electrical appliance fitters	0.57	0.59	0.43	0.60
Plastics processors	0.57	0.62	0.67	0.86
Packagers, goods receivers, despatchers	0.57	0.64	0.86	0.92
Locksmiths, not specified up to sheet metal, plastics fitters	0.59	0.63	1.32	1.54
Salespersons	0.60	0.65	1.57	2.06
Laundry workers, pressers up to textile cleaners, dyers, and dry cleaners	0.60	0.66	0.06	0.06
Building labourer, general up to other building labourers, building assistants	0.61	0.70	1.26	0.97
Electrical appliance, electrical parts assemblers	0.62	0.66	0.22	0.20
Other assemblers	0.63	0.68	0.31	0.81
Household cleaners up to glass, building cleaners	0.63	0.73	0.26	0.41
Publishing house dealers, booksellers up to service-station attendants	0.63	0.67	0.17	0.13
Restaurant, inn, bar keepers, hotel proprietors, catering trade dealers up to waiters, stewards	0.64	0.71	0.35	0.58
Metal workers (no further specification)	0.67	0.71	1.07	1.38
Assistants (no further specification)	0.71	0.75	0.75	3.00
Other attending on guests	0.74	0.80	0.21	0.12
Medical receptionists	0.80	0.83	0.01	0.02
Nursery teachers, child nurses	0.80	0.79	0.02	0.09

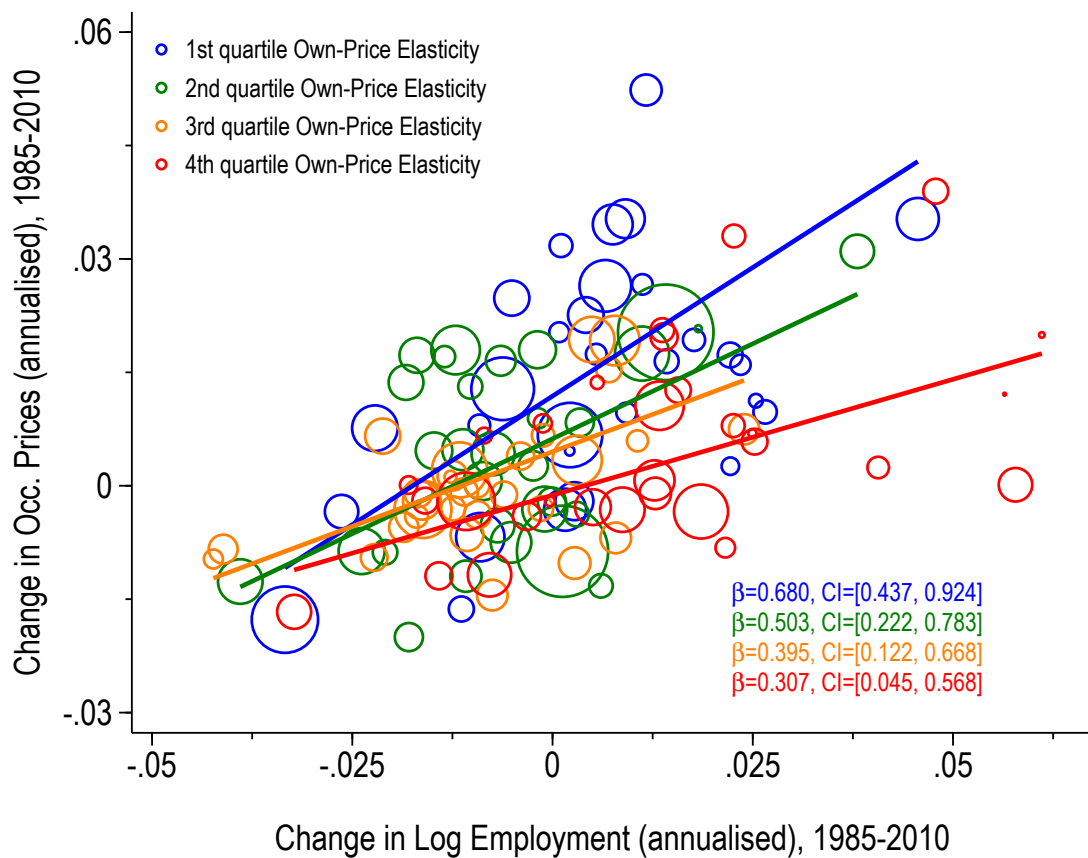
*Notes:* The table provides diagonal elements of the elasticity matrix  $D$ , not accounting (column (1), our baseline specification) and accounting for non-employment (columns (2), an extension of our model discussed in detail in Appendix F.1). Columns (3)–(4) report the occupation’s percentage share of employment in 1985 and 2010, respectively.

## C Empirical Results on the Labour Supply Model

This section provides tables and figures to complement the estimation results.

Figure 2b in the main text splits occupations at the median of  $d_{jj}$  and draws two separate regression lines. Figure C.1 below alternatively splits occupations into  $d_{jj}$  quartiles. The resulting four regression lines are visibly ranked by predicted labour supply elasticity, with the lowest  $d_{jj}$  quartile (in blue colour) exhibiting the steepest relation of employment vs prices, the highest  $d_{jj}$  quartile (in red colour) exhibiting the flattest relationship, and the middle quartiles (in green and orange) ranked in between.

**Figure C.1:** Occupational Price and Employment Changes by Own-Price Elasticity  $d_{jj}$  Quartiles



*Notes:* The figure shows the lines from an occupation-size weighted regression of price change on employment change, split by occupations in the lowest (blue), second (green), third (orange), and highest (red) quartile of own-price elasticity  $d_{jj}$ .  $\beta$  refers to the slope coefficient, and *CI* stands for the 95% confidence interval. Marker size indicates the baseline employment (in 1985) in each occupation.

Table C.1 considers the case in which own-occupation effects are not further split into a fixed relationship and the additional effect of the heterogeneity in elasticities  $d_{jj}$ . That is, it directly implements an unrestricted and a restricted version of eq. (9). Note that the coefficient in column (2) of the table is negative because of omitted variable bias (OVB).

In the short regression only on cross-effects of column (2),  $\Delta e_j = \theta_2 \sum_{k \neq j} d_{jk} \Delta p_k + \varepsilon_j$ , this leads to an OVB for  $\theta_2$  of  $\theta_1 \frac{Cov(d_{jj} \Delta p_j, \sum_{k \neq j} d_{jk} \Delta p_k)}{Var(\sum_{k \neq j} d_{jk} \Delta p_k)}$ . Considering these covariances as taken over random draws of price changes, for given  $j, k$  and  $d_{jk}$ , the numerator in this expression can be rewritten as  $d_{jj} \sum_{k \neq j} d_{jk} Cov(\Delta p_j, \Delta p_k)$ . Since  $d_{jk}$  is large negative for highly substitutable occupations, and close to zero for occupations that are further apart, and because prices for substitutable occupations tended to move in the same direction, then  $d_{jj} \sum_{k \neq j} d_{jk} Cov(\Delta p_j, \Delta p_k) \ll 0$ , which signs the OVB.

Finally, [Table C.2](#) shows unweighted regressions where each occupation is treated as one equally-weighted observation in the estimation.

**Table C.1:** Determinants of Employment Changes: Own- and Cross-Effects (OLS)

		Dependent Variable: $\Delta e_j$			
		(1)	(2)	(3)	(4)
own effect:	$d_{jj} \Delta p_j$	1.81 (0.32)		4.10 (0.88)	4.15 (0.70)
total cross effect:	$\sum_{k \neq j} d_{jk} \Delta p_k$		-2.14 (0.59)	4.03 (1.29)	
R-squared		0.310	0.163	0.394	0.394
Number of occupations		120	120	120	120

*Notes:* The table presents the unweighted estimates from different versions of eq. (9). Regressor in column (4) is  $\sum_k d_{jk} \Delta p_k$ , i.e., corresponding to the full model and as in the main text. All regressions include a constant. Observations weighted by occupation  $j$ 's initial employment size. Period 1985–2010. Standard errors in parentheses; all coefficients shown are significant at the 1% level.

**Table C.2:** Determinants of Employment Changes. Unweighted (OLS)

		Dependent Variable: $\Delta e_j$				
		Unrestricted Model			Restricted Model	
		(1)	(2)	(3)	(4)	(5)
fixed relationship:	$\bar{d}_{diag} \Delta p_j$	1.70 (0.27)	1.93 (0.26)	3.82 (0.69)	1.93 (0.27)	4.18 (0.54)
heterogeneous own effect:	$(d_{jj} - \bar{d}_{diag}) \Delta p_j$		1.94 (0.63)	4.27 (1.01)		
total cross effect:	$\sum_{k \neq j} d_{jk} \Delta p_k$			3.32 (1.11)		
R-squared		0.264	0.318	0.377	0.318	0.366
Number of occupations		119	119	119	119	119

*Notes:* The table presents the unweighted estimates from different versions of eq. (12). Regressor in column (4) is  $d_{jj} \Delta p_j$ . In column (5), the regressor is  $\sum_k d_{jk} \Delta p_k$ , i.e., corresponding to the full model. All regressions include a constant. Observations equally weighted; number of observations is 119 because the tiny occupation 'Medical Receptionists' has been dropped. Period 1985–2010. Standard errors in parentheses; all coefficients shown are significant at the 1% level.

## D Labour Demand, Equilibrium, and Estimation Strategy

This section extends the model by incorporating occupational labour demand. In what follows, we present the main features of the demand and supply sides, characterise equilibrium, and discuss its practical implementation.

### D.1 Labour Demand and Equilibrium

We consider an economy-wide constant elasticity of substitution (CES) production technology

$$Y = A \left( \sum_i \beta_i E_i^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}} \quad \text{s.t.} \quad \sum \beta_i = 1$$

where  $i$  is for occupation,  $E$  for employment,  $\beta_i$  are the factor intensities of different occupation inputs and  $\sigma > 0$  is the elasticity of substitution across occupations.

The first order conditions yield, for all  $i$ ,

$$\beta_i E_i^{-\frac{1}{\sigma}} A \left( \sum_i \beta_i E_i^{\frac{\sigma-1}{\sigma}} \right)^{\frac{\sigma}{\sigma-1}-1} = p_i$$

where  $p_i$  is the wage (the price of labour) level for occupation  $i$  and the price of the output good is normalised to 1.

To begin, consider demands relative to occupation  $N$ :

$$\begin{aligned} \tilde{E}_i &\equiv \ln \frac{E_i}{E_N} = \ln \left( \frac{\beta_i p_N}{\beta_N p_i} \right)^\sigma \\ &= \ln \left( \beta_{-i} \frac{\beta_i}{1 - \beta_i} \frac{1}{\tilde{p}_i} \right)^\sigma \end{aligned}$$

where  $\tilde{p}_i \equiv \frac{p_i}{p_N}$  and  $\beta_{-i} \equiv \frac{1 - \beta_i}{\beta_N} = \frac{\sum_{j \neq i} \beta_j}{\beta_N}$ . In what follows, we will consider incremental changes to  $\ln \frac{\beta_i}{1 - \beta_i}$  with proportionate off-setting changes to  $\beta_k$  for  $k \neq j$ .

It is worth noting that  $\frac{d \ln \frac{\beta_i}{\beta_N}}{d \ln \frac{\beta_i}{1 - \beta_i}} = \frac{d \ln \beta_{-i} \frac{\beta_i}{1 - \beta_i}}{d \ln \frac{\beta_i}{1 - \beta_i}} = 1$ . On the other hand,  $\frac{d \ln \frac{\beta_i}{\beta_N}}{d \ln \frac{\beta_j}{1 - \beta_j}} = 0$  because proportional changes to  $\beta_i$  and  $\beta_N$  are equal and offsetting. In more compact notation, we can therefore write

$$\tilde{E}_i^d(\tilde{p}_i(\mathbf{b}, \mathbf{s}), \tilde{\beta}_i) = \ln \left( \tilde{\beta}_i \frac{1}{\tilde{p}_i} \right)^\sigma \quad (32)$$

where  $\tilde{p}_i$  is the log of  $\tilde{p}_i$ ,  $\mathbf{b}$  is the  $(N - 1)$  vector of relative productivities (i.e., demand shifters  $\left( \ln \frac{\beta_j}{1 - \beta_j} \right)$ ),  $\mathbf{s}$  is a vector of supply shifters that do not directly affect demand,

and  $\tilde{\beta}_i = \frac{\beta_i}{\beta_N}$ . Note that relative demand for employment in occupation  $i$  depends on the relative price in that occupation *only*.

In fact, we are interested in log employment shares  $e_i = \ln \frac{E_i}{\sum_j E_j} = \ln \frac{E_i}{E}$ . In this case, demands depend on productivities and prices of other occupations. We will be interested in perturbations around the steady state, so in keeping with the rest of the paper, we will denote steady-state share of occupation  $i$  by  $\tau_i$ . This gives a demand curve  $e_i^d(\langle \tilde{p}(\mathbf{b}, \mathbf{s}) \rangle, \mathbf{b})$ , which is a function of all prices and demand shifters.

To calculate derivatives, first note that, around the steady state:

$$\frac{\partial e_j^d}{\partial p_i} \Big|_{p_{k \neq i}} = -\frac{\tau_i}{1 - \tau_i} \frac{\partial e_i^d}{\partial p_i} \Big|_{p_{k \neq i}}$$

i.e. given a change to  $p_i$ , and holding fixed all other prices (made explicit by the notation  $|_{p_{k \neq i}}$ ), then adding up ensures this identity, because all other occupations are equally proportionately offset.<sup>52</sup> Therefore, we have that:

$$\begin{aligned} \frac{\partial e_i^d}{\partial p_i} &= \frac{\partial \ln \frac{E_i}{E_N}}{\partial p_i} + \frac{\partial \ln \frac{E_N}{E}}{\partial p_i} \\ &= \frac{\partial \ln \frac{E_i}{E_N}}{\partial p_i} + \frac{\partial e_N^d}{\partial p_i} \\ &= -\sigma - \frac{\tau_i}{1 - \tau_i} \frac{\partial e_i^d}{\partial p_i} \\ \implies \frac{\partial e_i^d}{\partial p_i} &= -(1 - \tau_i) \sigma \end{aligned}$$

This also implies that for  $j \neq i$ :

$$\begin{aligned} \frac{\partial e_i^d}{\partial p_j} &= -\frac{\tau_j}{1 - \tau_j} \frac{\partial e_j^d}{\partial p_j} \\ &= \tau_j \sigma \end{aligned}$$

Together, these are result (14) in the main text. A similar logic implies that  $\frac{\partial e_i^d}{\partial \ln \frac{\beta_j}{1 - \beta_j}}$  follows a similar structure.

We therefore have a demand function  $e_i^d(\langle p(\mathbf{b}, \mathbf{s}) \rangle, \mathbf{b})$  with partial derivatives for

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<sup>52</sup>Note that adding up requires  $\sum_k \frac{\partial e_k^d}{\partial p_i} E_k = 0$ , which implies  $\frac{\partial e_i^d}{\partial p_i} E_i + \sum_{k \neq i} \frac{\partial e_k^d}{\partial p_i} E_k = 0$ . Noting that a property of CES demands given by eq. (32) are that  $\frac{\partial e_k^d}{\partial p_i} = \frac{\partial e_l^d}{\partial p_i} \equiv \frac{\partial e_{-i}^d}{\partial p_i}$  for  $k, l \neq i$ , then we have that  $\frac{\partial e_i^d}{\partial p_i} E_i + \frac{\partial e_{-i}^d}{\partial p_i} \sum_{k \neq i} E_k = 0 \implies \frac{\partial e_i^d}{\partial p_i} e_i + \frac{\partial e_{-i}^d}{\partial p_i} \sum_{k \neq i} e_k = 0$ . Rearranging and using  $\tau_i$  give the result.

prices given by elements of the matrix  $\sigma(W - I)$ , with rank  $N - 1$ , where  $I$  is the identity matrix, and  $W$  is the matrix of employment shares, as defined in Appendix A.2. The matrix of derivatives with respect to demand shifters is given by  $\sigma(I - W)$ , equally of rank  $N - 1$ .

### D.1.1 Labour Supply

As extensively discussed in the main text, we have that  $\frac{\partial e_j^s}{\partial p_k} = \theta d_{jk}$ . The matrix of supply derivatives is therefore given by  $\theta D$ , similarly of rank  $N - 1$ .

We have some flexibility in defining the effect of supply shifters, as long as they satisfy adding up, i.e. that  $\sum_i \frac{\partial e_i^s}{\partial s_j} \tau_i = 0$ . We can satisfy this by letting  $\frac{\partial e_i^s}{\partial s_j} \equiv -\tau_j$  for  $i \neq j$  and  $\frac{\partial e_j^s}{\partial s_j} \equiv 1 - \tau_j$ . Then  $\sum_i \frac{\partial e_i^s}{\partial s_j} \tau_i = (1 - \tau_j) \tau_j - \sum_{i \neq j} \tau_j \tau_i = \tau_j (1 - \tau_j - \sum_{i \neq j} \tau_i) = 0$ . The matrix of derivatives with respect to supply shifters is therefore given by  $I - W$ .

### D.1.2 Equilibrium Characterisation

Similarly to before, we can write

$$e_i(\mathbf{b}, \mathbf{s}) = e_i^s(\langle p(\mathbf{b}, \mathbf{s}) \rangle, \mathbf{s}) = e_i^d(\langle p(\mathbf{b}, \mathbf{s}) \rangle, \mathbf{b}) \quad (33)$$

where both supply and demand curves depend on the full system of prices.

In what follows, for ease of exposition, it is useful to define the following matrices for gradients of equilibrium quantities  $\{E_j\}$  and prices  $\{p_j\}$ .

Notation	Typical element
$\Xi$	$\frac{de_i}{d\left(\ln \frac{\beta_j}{1-\beta_j}\right)}$
$\Gamma$	$\frac{de_i}{ds_j}$
$V$	$\frac{dp_i}{d\left(\ln \frac{\beta_j}{1-\beta_j}\right)}$
$S$	$\frac{dp_i}{ds_j}$

### Solving for Price Gradients using $e_i^s(\cdot) = e_i^d(\cdot)$

Differentiating  $e_i^s(\cdot) = e_i^d(\cdot)$  from eq. (33) with respect to  $\ln \frac{\beta_j}{1-\beta_j}$  we obtain:

$$\sum_k \frac{\partial e_i^s}{\partial p_k} \frac{\partial p_k}{\partial \left(\ln \frac{\beta_j}{1-\beta_j}\right)} = \sum_k \frac{\partial e_i^d}{\partial p_k} \frac{\partial p_k}{\partial \left(\ln \frac{\beta_j}{1-\beta_j}\right)} + \frac{\partial e_i^d}{\partial \ln \frac{\beta_j}{1-\beta_j}} \quad (34)$$

Expressing this in matrix notation gives

$$\begin{aligned}\theta DV &= \sigma(W - I)V + \sigma(I - W) \\ \implies (\theta D + \sigma(I - W))V &= \sigma(I - W)\end{aligned}\quad (35)$$

where  $V$  is a matrix with  $i, j$ th element  $\frac{\partial p_i}{\partial \left(\ln \frac{\beta_j}{1-\beta_j}\right)}$  that we wish to solve.

At this point, we notice that  $(\theta D + \sigma(I - W))$  has rank  $N - 1$ . However, we can also notice that  $(I - W)$  is the de-meaning operator, such that for vector  $x$ , then  $(I - W)x = x - 1_N \sum_i \tau_i x_i$ , where  $1_N$  is a column vector of ones. Therefore, we can solve eq. (35) as long as we make the appropriate normalisation. Specifically, we define price gradients such that  $\sum_i \tau_i \frac{\partial p_i}{\partial \left(\ln \frac{\beta_j}{1-\beta_j}\right)} = 0$ , i.e., the weighted price gradient is 0.

Recall that this normalisation is without loss of generality because the model is invariant to additive shifts in prices. In this case, we can solve for  $V$  as

$$V = \left(\frac{\theta}{\sigma}D + I\right)^{-1} (I - W) \quad (36)$$

which in fact guarantees the normalisation by construction.

Next, we consider gradients with respect to supply shifters. Differentiating with respect to  $s_j$  we obtain:

$$\begin{aligned}\sum_k \frac{\partial e_i^s}{\partial p_k} \frac{\partial p_k}{\partial s_j} + \frac{\partial e_i^s}{\partial s_j} &= \sum_k \frac{\partial e_i^d}{\partial p_k} \frac{\partial p_k}{\partial s_j} \\ \implies \theta DS + I - W &= \sigma(W - I)S \\ \implies (\theta D + \sigma(I - W))S &= -(I - W)\end{aligned}$$

Similarly to above, we can solve for  $S$  using a normalisation of price gradients with respect to a supply shock. That is, setting  $\sum_i \tau_i \frac{\partial p_i}{\partial s_j} = 0$  and again without loss of generality, we obtain:

$$\begin{aligned}S &= -(\theta D + \sigma I)^{-1} (I - W) \\ &= -\frac{1}{\sigma}V\end{aligned}\quad (37)$$



**Solving for Quantity Gradients using  $e_i(\cdot) = e_i^d(\cdot)$  and  $e_i(\cdot) = e_i^s(\cdot)$**

Differentiating the identity  $e_i(\mathbf{b}, \mathbf{s}) = e_i^d(\langle p(\mathbf{b}, \mathbf{s}) \rangle, \mathbf{b})$  w.r.t.  $s_j$  we get

$$\begin{aligned} \frac{\partial e_i}{\partial s_j} &= \sum_k \frac{\partial e_i^d}{\partial p_k} \frac{\partial p_k}{\partial s_j} \\ \implies \Gamma &= -\sigma(I - W)S = -\sigma S = V \end{aligned}$$

and then differentiating the identity  $e_i(\mathbf{b}, \mathbf{s}) = e_i^s(\langle p(\mathbf{b}, \mathbf{s}) \rangle, \mathbf{b})$  w.r.t.  $\ln \frac{\beta_j}{1-\beta_j}$  we get

$$\frac{de_i}{d\left(\ln \frac{\beta_j}{1-\beta_j}\right)} = \sum_k \frac{\partial e_i^s}{\partial p_k} \frac{\partial p_k}{\partial \left(\ln \frac{\beta_j}{1-\beta_j}\right)}$$

which provides the matrix equation

$$\Xi = \theta DV$$

### D.1.3 Observed Changes

Let  $\Delta \mathbf{e}$  be the vector of observed changes in labour shares, with  $i$ th element,  $\Delta e_i$ . Similarly let  $\Delta \mathbf{b}$  be the vector of productivity (or demand) shifts,  $\Delta \mathbf{s}$  the vector of supply shifts, and  $\Delta \mathbf{p}$  be the change in prices. Then we have that

$$\begin{aligned} \Delta \mathbf{p} &\approx V\Delta \mathbf{b} + S\Delta \mathbf{s} \\ &= V\Delta \mathbf{b} - \frac{1}{\sigma}V\Delta \mathbf{s} \end{aligned} \tag{38}$$

and

$$\begin{aligned} \Delta \mathbf{e} &\approx \Xi\Delta \mathbf{b} + \Gamma\Delta \mathbf{s} \\ &= \theta DV\Delta \mathbf{b} - \sigma S\Delta \mathbf{s} \\ &= \theta DV\Delta \mathbf{b} + V\Delta \mathbf{s} \end{aligned} \tag{39}$$

These expressions, corresponding to eq. (16) and eq. (17) in the main text, describe changes to labour shares and prices in terms of demand and supply shocks, price elasticities, and model parameters  $\theta$  and  $\sigma$ .

## D.2 Estimation and Extraction of Shocks

### D.2.1 Estimation Strategy

Expressions (38) and (39) also inform the regression framework. From eq. (38), note that  $\theta D\Delta\mathbf{p} = \theta DV\Delta\mathbf{b} + \theta DS\Delta\mathbf{s}$ . Using this to substitute  $\Delta\mathbf{b}$  out of eq. (39) yields:

$$\begin{aligned}
 \implies \Delta\mathbf{e} &\approx \theta D\Delta\mathbf{p} - \theta DS\Delta\mathbf{s} - \sigma S\Delta\mathbf{s} \\
 &= \theta D\Delta\mathbf{p} - (\theta D + \sigma) S\Delta\mathbf{s} \\
 &= \theta D\Delta\mathbf{p} - (-(I - W)) \Delta\mathbf{s} \\
 &= \theta D\Delta\mathbf{p} + \Delta\mathbf{s}
 \end{aligned} \tag{40}$$

where the last line follows from the penultimate line because the vector of supply shocks is defined to be suitably normalised.

Equation (40) is our basic regression equation (eq. (18) in the main text), extending eq. (9) to include supply shocks. The logic of requiring the IV is that, given that  $\Delta\mathbf{s}$  is not observed, then an OLS regression of  $\Delta e_j$  on  $\mathbf{d}_j\Delta\mathbf{p}$  will not work, because  $\mathbf{d}_j\Delta\mathbf{p}$  is correlated with these shocks.

Suppose we have a variable, which we denote  $r_j$ , that is correlated with  $\Delta b_j \equiv \ln \frac{\beta_j}{1-\beta_j}$  but not with  $\Delta s_j$ . In matrix notation:

$$\Delta\mathbf{b} = \kappa \mathbf{1}_N + \lambda \mathbf{r} + \bar{\eta}$$

where  $\kappa$  and  $\lambda$  are scalars,  $\mathbf{1}_N$  is a vector of ones and  $\bar{\eta}$  is a vector of shocks.

Then, from eq. (38):

$$\begin{aligned}
 \Delta\mathbf{p} &\approx V\Delta\mathbf{b} + S\Delta\mathbf{s} \\
 \implies \Delta\mathbf{p} &\approx \lambda V\mathbf{r} + \bar{\epsilon} + S\Delta\mathbf{s} \\
 \implies D\Delta\mathbf{p} &\approx \lambda DV\mathbf{r} + D\bar{\epsilon} + DS\Delta\mathbf{s} \\
 &= \lambda D \left( \frac{\theta}{\sigma} D + I \right)^{-1} (I - W) \mathbf{r} + D\bar{\epsilon} + DS\Delta\mathbf{s} \\
 &= \lambda D \left( \frac{\theta}{\sigma} D + I \right)^{-1} \tilde{\mathbf{r}} + D\bar{\epsilon} + DS\Delta\mathbf{s}
 \end{aligned}$$

where the second line follows from the first because, if  $v_{ij}$  is the  $i, j$ th element of  $V$ , then  $\sum_j v_{ij} = 0$ . Vector  $\tilde{\mathbf{r}}$  is the employment-share-weighted-demeaned version of  $\mathbf{r}$  and finally,  $\bar{\epsilon} \equiv V\bar{\eta}$ . This is relationship (19) in the main text.

In terms of regressing  $\Delta e_j$  on the vector of price changes, this implies that an appropri-

ate instrument for  $\mathbf{d}_j \Delta \mathbf{p}$  is  $\mathbf{d}_j V \mathbf{r}$ .

We assume  $\frac{\theta}{\sigma} = 2.3$  throughout the paper. In [Table D.2](#), we show the robustness of our results to different values of  $\frac{\theta}{\sigma}$ .

### D.2.2 Backing Out the Shocks

In [Section 6](#), we use the model solution to construct counterfactuals. Here we show how to obtain the supply and demand shocks for this.

From [\(40\)](#), we immediately see that

$$\Delta \mathbf{s} \approx \Delta \mathbf{e} - \theta D \Delta \mathbf{p} \quad (41)$$

Similarly, from [\(38\)](#)

$$\begin{aligned} \Delta \mathbf{p} &\approx V \Delta \mathbf{b} + S \Delta \mathbf{s} \\ \implies \sigma (I - W) \Delta \mathbf{p} &\approx \sigma (I - W) V \Delta \mathbf{b} + \sigma (I - W) S \Delta \mathbf{s} \end{aligned}$$

Summing with [\(39\)](#) this implies that

$$\begin{aligned} \Delta \mathbf{e} + \sigma (I - W) \Delta \mathbf{p} &\approx (\sigma (I - W) V + \theta D V) \Delta \mathbf{b} \\ &= (\sigma (I - W) + \theta D) V \Delta \mathbf{b} \\ &= \sigma (I - W) \Delta \mathbf{b} \end{aligned}$$

where the last line follows from [equation \(35\)](#). Rearranging gives:

$$(I - W) \Delta \mathbf{b} \approx \frac{1}{\sigma} \Delta \mathbf{e} + (I - W) \Delta \mathbf{p}$$

Given the definition of the  $b_j = \ln \frac{\beta_j}{1 - \beta_j}$  as logs of relative demands, their (marginal) changes have mean of zero when weighted by employment shares. So we can write

$$\Delta \mathbf{b} \approx \frac{1}{\sigma} \Delta \mathbf{e} + (I - W) \Delta \mathbf{p} \quad (42)$$

without loss of generality. [Equations \(41\)–\(42\)](#) can be used to construct the shock vectors. Note that in [\(42\)](#) the term  $(I - W)$  is retained to de-mean any given vector of price changes. This term is not required in [\(41\)](#) because the  $D$  matrix de-means the vector automatically. Additionally,  $\Delta \mathbf{e}$  is (weighted) mean zero by construction.

### D.3 Empirical Results on the Equilibrium Model

In this section, we present empirical results from the equilibrium estimation.

Table D.1 presents summary statistics on the matrices  $V$  and  $DV$  that govern the dissipation of shocks to wages and employment in equations (16) and (17).<sup>53</sup> Parallel to the elasticity matrix in Table B.3, diagonal elements of  $V$  and  $DV$  (i.e., own-effects of shocks) are on average substantially larger than off-diagonal elements (cross-effects from shocks in other occupations) while, relative to the mean, standard deviations in the off-diagonal elements are higher. Off-diagonals in  $DV$  inherit some of the high skewness of  $D$ , whereas off-diagonals in  $V$  are not particularly skewed compared to the on-diagonals.

**Table D.1:** Summary Statistics. Matrices  $V$  and  $DV$

	Matrix $V$		Matrix $DV$	
	Diagonal Elements	Off-Diagonal Elements ( $\times 100$ )	Diagonal Elements	Off-Diagonal Elements ( $\times 100$ )
Mean	0.508	-0.427	0.210	-0.177
Std. Dev.	0.079	0.916	0.035	0.319
Variance	0.006	0.839	0.001	0.102
Skewness	1.203	-1.482	-1.090	-7.490
Kurtosis	5.881	54.605	5.565	113.507
p1	0.357	-5.326	0.099	-1.510
p10	0.418	-1.096	0.174	-0.397
p50	0.501	-0.226	0.215	-0.082
p90	0.587	0.016	0.249	-0.017
p99	0.746	1.109	0.279	-0.001
Correlation with $D$	-0.959	-0.246	0.968	0.935
Correlation with $V$			-0.989	0.016
Number of Observations	120	14,280	120	14,280

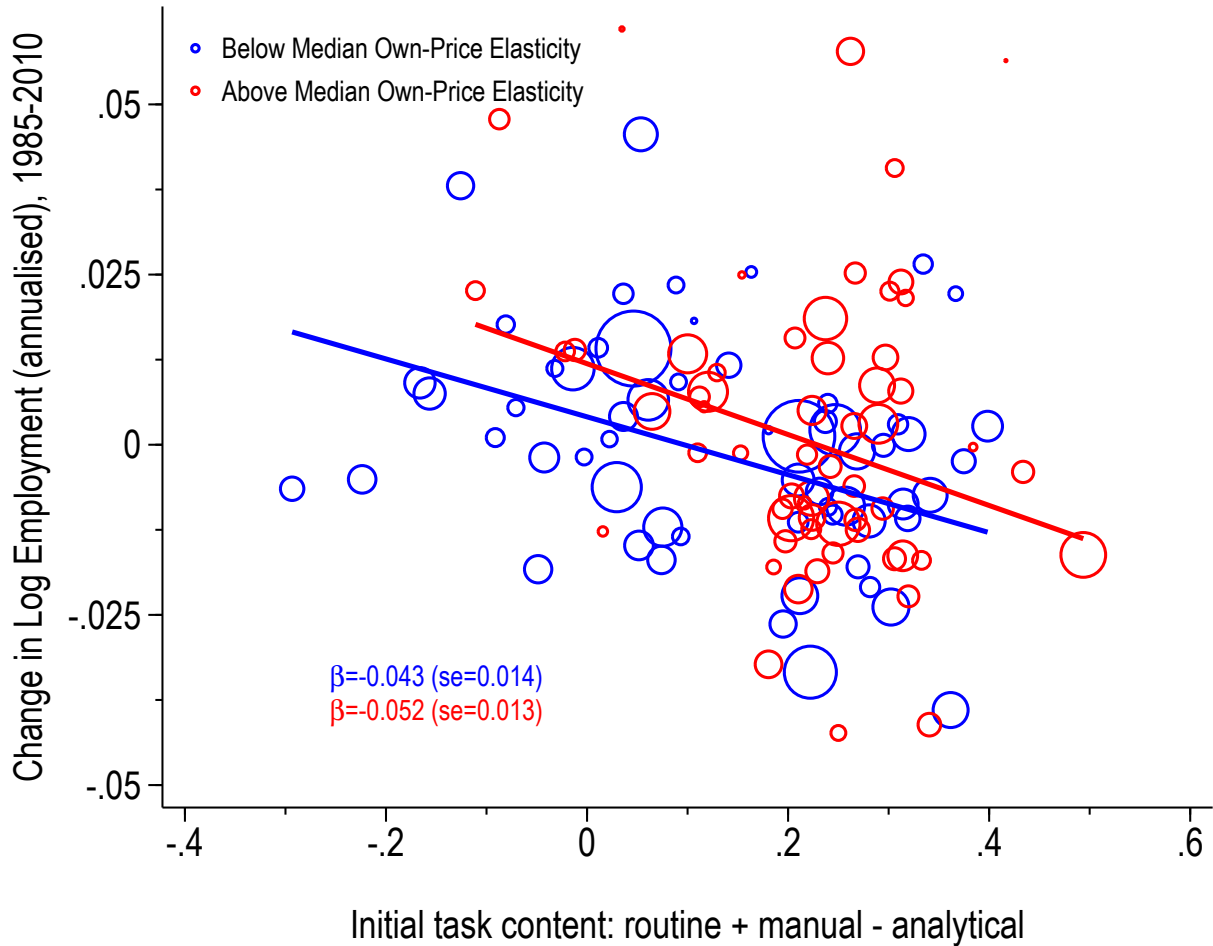
Notes: The table presents summary statistics for the matrices  $V = \left(\frac{\theta}{\sigma}D + I\right)^{-1}(I - W)$  and  $DV$ , where we use the equilibrium solution for  $\frac{\theta}{\sigma}$ . See also the discussion in the text.

Interestingly, in contrast to matrix  $D$  and as discussed in the main text, off-diagonal elements in  $V$  can have opposite signs. This reflects that demand shocks in a given sector may have positive effects on prices in close substitute occupations while they have negative effects in more distant occupations. Table D.1 also reports that, overall, matrix elements from  $D$  are negatively correlated with those in  $V$  but positively with those in  $DV$ . This indicates that, ceteris paribus, larger own-price elasticities are associated with lower

<sup>53</sup>We use  $\theta$  and  $\sigma$  from the equilibrium solution to the model. Table D.2 below shows that different calibrations of  $\sigma$  hardly change estimated  $\theta$ . Qualitative conclusions from Table D.1 also do not depend on the particular value of  $\frac{\theta}{\sigma}$  that is used.

price changes and higher employment changes in response to demand shocks. Larger cross-price elasticities (more negative  $d_{jk}$ ) tend to lead to more positive price responses and more negative employment responses from a demand shock in the respective other occupation.

**Figure D.1:** IV Reduced-Form for Employment



*Notes:* The figure shows reduced-form regressions of occupations' employment changes on their initial task contents  $r_j$ . Colour codes and linear regression lines are split by occupations below (blue, inelastic) and above (red, elastic) the median own-price elasticity ( $d_{jj}$ ).  $\beta$  and  $se$  refer to the slope coefficient and standard error, respectively. Marker size indicates the baseline employment (in 1985) in each occupation.

**Table D.2:** Structural IV: Different Values of  $\frac{\theta}{\sigma}$

	$\frac{\theta}{\sigma} = 0.001$	$\frac{\theta}{\sigma} = 0.1$	$\frac{\theta}{\sigma} = 1$	$\frac{\theta}{\sigma} = 1.5$	$\frac{\theta}{\sigma} = 2$	$\frac{\theta}{\sigma} = 2.3$	$\frac{\theta}{\sigma} = 2.5$	$\frac{\theta}{\sigma} = 3$	$\frac{\theta}{\sigma} = 4$
IV estimate for $\theta$	5.20	5.19	4.95	4.87	4.81	4.78	4.76	4.72	4.66
Implied $\sigma$	5200	519	4.95	3.25	2.41	2.08	1.90	1.57	1.17

*Notes:* The table shows the robustness of our IV estimate to different values of  $\frac{\theta}{\sigma}$ . The second row reports the implied  $\sigma$ . The case highlighted in blue ( $\frac{\theta}{\sigma} = 2.3$ ) is the benchmark used throughout the paper.

## D.4 OLS versus IV Estimates

We wish to estimate eq. (18), which is reproduced here for convenience:

$$\Delta \mathbf{e} \approx \theta D \Delta \mathbf{p} + \Delta \mathbf{s}$$

Allowing for a regression constant, we stack parameters into vector  $\beta = [\alpha \ \theta]'$  and regressors into  $N \times 2$  matrix  $X = [1_N \ D \Delta \mathbf{p}]$ , where  $1_N$  is a vector of ones. The OLS estimate of  $\beta$  is then

$$\hat{\beta}_{OLS} = (X'X)^{-1}X'\Delta \mathbf{e} = \beta + (X'X)^{-1}X'\Delta \mathbf{s}.$$

From (16) and (17), we note that

$$D \Delta \mathbf{p} = DV(\Delta \mathbf{b} - \frac{1}{\sigma} \Delta \mathbf{s})$$

and in the data the relevant covariances and variances are quite similar with  $Cov(\Delta b_j, \Delta s_j) = 0.000101$  and  $\frac{1}{\sigma} Var(\Delta s_j) = 0.000128$ , respectively. It turns out that also the weighting matrix  $DV$  does not change this near-equivalence such that  $(D \Delta \mathbf{p})' \Delta \mathbf{s} = \Delta \mathbf{b}' V' D' \mathbf{s} - \frac{1}{\sigma} \Delta \mathbf{s}' V' D' \mathbf{s}$  is only slightly negative (close to zero). Since  $\Delta \mathbf{s}$  is size-weighted mean zero, also  $1_N' \Delta \mathbf{s} \approx 0$  such that

$$(X'X)^{-1}X'\Delta \mathbf{s} \approx [0 \ 0]'$$

That is, there happens to be little bias in the OLS estimate.

Therefore, we get from this that

$$\hat{\theta}_{OLS} \approx \theta$$

where, by construction, true  $\theta$  is identified in (20) from the instrumental variables strategy under the relevant IV assumptions. Put differently,  $\hat{\theta}_{OLS} - \theta = 4.15 - 4.78 = -0.63$ , which is negative but small relative to the absolute value of  $\theta$ .

## E Model-Based Decomposition and Counterfactuals

This section develops the counterfactual elasticity matrices introduced in Section 6.1, relating them to the theory and empirics used in prior literature. We then report additional empirical results on the model solution and counterfactual analyses in Section 6.2.

### E.1 Counterfactual Elasticities

#### E.1.1 Heterogeneous Own-Price Elasticities Only

The counterfactual matrix  $D_{own}$  considers the case that occupations' aggregate (own-price) elasticities vary but their similarities with other occupations are homogeneous. In particular, we have that  $Cov_{\tau}(\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k}) = c \in [-1, 0]$  in eq. (6) and  $Var_{\tau}(\tilde{\pi}_{.,j}) = -\frac{1-\tau_j}{\tau_j}c$  in eq. (7). The main diagonal elements of  $D_{own}$  are the actual own-price elasticities, whereas cross-price elasticities reduce to size-weighted fractions of the on-diagonals  $\frac{-\tau_k}{1-\tau_j}d_{jj}$ .<sup>54</sup>

A specific version of this counterfactual with  $c = 0$  can be derived from setups commonly used in the literature on firms, even if their focus is on studying heterogeneity of (own-price) labour supply elasticities facing employers. Consistent with, among many others, Card et al. (2018); Lamadon et al. (2022); Berger et al. (2022), one could take a simpler version of individuals' indirect utility eq. (1) as follows:<sup>55</sup>

$$u_j(\omega) = \theta p_j + a_j + \varepsilon_j(\omega), \quad (43)$$

Note that, in this case, switching costs  $a_j$  do not depend on the source employer  $i$ .

We derive the versions of Remarks 1–3, which result from eq. (43), by noting that the choice probability  $\pi_j = \frac{\exp(\theta p_j + a_j)}{\sum_{k=1}^N \exp(\theta p_k + a_k)}$  also no longer depends on sending occupation  $i$ . For occupation sizes, we obtain:

$$\begin{aligned} E_j(\mathbf{p}) &= \sum_i \tau_i \pi_j = \pi_j \\ &= \tau_j \quad \text{if } \mathbf{p} = \mathbf{p}^* \end{aligned}$$

since  $\sum_i \tau_i = 1$  in the first line and then  $\pi_j = \tau_j$  in baseline stationary equilibrium.

From this, we obtain  $\tilde{\pi}_{i,j} = \frac{\pi_j}{\tau_j} = 1$  for all  $i, j$  and  $Cov_{\tau}(\tilde{\pi}_{.,j}, \tilde{\pi}_{.,k}) = Var_{\tau}(\tilde{\pi}_{.,j}) = 0$ . Without combination-specific access costs, occupations are just all equally substitutable

<sup>54</sup>Forcing fully homogeneous cross-elasticities (i.e.,  $\frac{-d_{jj}}{N-1}$ ) yields very similar empirical results to those shown below. In both cases,  $D_{own}$  is still a valid elasticity matrix, since  $d_{jj} = -\sum_{k \neq j} d_{kj}$ .

<sup>55</sup>In Berger et al. (2022) or Lamadon et al. (2022), the substitutability between employers within a market is fixed by what corresponds to our parameter  $\theta$ . Across predefined markets (region-industries) is an extra substitutability parameter, which leads to a nested CES or logit structure. In contrast, we allow for flexibly heterogeneous occupational similarities as governed by job flows in the data.

from a labour supply perspective. Remarks 2 and 3 then lead to

$$d_{jk} = \begin{cases} 1 - \tau_j & \text{if } j = k \\ -\tau_k & \text{otherwise} \end{cases}$$

which is the result corresponding to Remark 1. The economic model with  $a_{ij} = a_j$  thus generates a version of our matrix with homogeneous occupational similarities  $D_{own}$ , and with  $c = 0$  as mentioned above.

### E.1.2 Fully Homogeneous Labour Supplies

The second counterfactual imposes completely homogeneous labour supply elasticities. The main diagonal elements of matrix  $D_{hom}$  become  $\bar{d}_{diag} = \sum_j \tau_j d_{jj}$  and cross-price elasticities a constant fraction of it  $\frac{-\bar{d}_{diag}}{N-1}$ .<sup>56</sup> This counterfactual is consistent with specifications in the empirical literature that regress occupations' log employment changes on their log wage changes (e.g. Autor et al., 2008; Dustmann et al., 2009; Cavaglia & Etheridge, 2020; Böhm et al., 2024, or column (1) of Table 2). This is formalized in terms of counterfactuals as follows:

$$\begin{aligned} \Delta e_j &= \theta \sum_{k=1}^N d_{jk} \Delta p_k \\ \Rightarrow \Delta e_{j,cf} &= \tilde{\theta} \Delta p_j - \tilde{\theta} \left( \frac{1}{N} \sum_{k=1}^N \Delta p_k \right) \end{aligned}$$

where counterfactual employment changes in the second line are obtained by replacing  $d_{jk}$  by  $\frac{-\bar{d}_{diag}}{N-1}$ . The first  $\tilde{\theta} \equiv \frac{N}{N-1} \bar{d}_{diag} \theta$  is a single slope parameter on the price change and the second term becomes a regression constant that reflects average wage growth in the economy. In the equilibrium model (18), there is additionally an error term  $\Delta s_j$ , which reflects supply shocks. Alternatively, as in the main text, we can normalise  $\Delta \mathbf{p}$  to have a mean of zero without loss of generality, in which case  $\Delta e_{j,cf} = \tilde{\theta} \Delta p_j$ .

The economic model would generate a specific version of  $D_{hom}$  with  $\bar{d}_{diag} = \frac{N-1}{N}$  and  $\tilde{\theta} = \theta$  if, in addition to similarities, all occupation sizes are also the same. That is, when  $\theta p_j + a_j = \text{const.}$  in eq. (43).

## E.2 Results

This section complements the decomposition and counterfactual analyses in Section 6.

Figure E.1 shows the impact of including labour supply heterogeneity in a counterfactual with no supply shocks ( $\Delta \mathbf{s}_{off} = \mathbf{0}$ ). Figure E.1a, same as Figure 4a, starts by considering the case with only demand shocks in the fully homogeneous model (i.e.  $D_{hom}$ ). In

<sup>56</sup>Empirical results below do not change if we size-weight the cross-price elasticities as  $\frac{-\tau_k}{(1-\tau_j)} \bar{d}_{diag}$ .



this case, all occupational changes induced by demand shocks  $\Delta \mathbf{b}$  run perfectly along a single supply curve. [Figure E.1b](#) then introduces both own- and cross-occupation effects keeping  $\Delta \mathbf{s}_{off} = 0$ . Relative to [E.1a](#), variation around the regression line increases, such that the R-squared reduces to 69%. The locus of points moves on average *counterclockwise* and the slope of the regression line increases from 0.52 to 0.85. These changes show the importance of allowing for supply heterogeneity (and especially cross-occupation effects, which effectively reduce elasticities) to explain the data.

[Figure E.2](#) plots the distribution of demand and supply shocks by occupation, exhibiting a generally positive correlation between the two (0.23). It shows that, e.g., occupations such as ‘assistants’ or ‘data processors’ experienced positive demand and supply shocks, while occupations like ‘bricklayers’ suffered negative demand and supply shocks. Another interesting example is the occupation ‘physicians, pharmacists’, which experienced a (large) positive demand shock but no supply shock.

[Figure E.3](#) and [Figure E.4](#) display employment and wage changes along the occupational wage distribution (in the initial year 1985), for the full model and the fully homogeneous (counterfactual) model, respectively. We highlight some key points:

First, our period of analysis is characterised by an increase in wage inequality and employment polarisation. This is represented in [Figure E.3](#) by the dashed black line, which reproduces estimates from the raw data. This evidence is consistent with [Dustmann et al. \(2009\)](#), among others. Similar to them, we find that for occupations in the upper half of the wage distribution, employment and wage changes are positively correlated, while they are negatively correlated for occupations in the lower half.

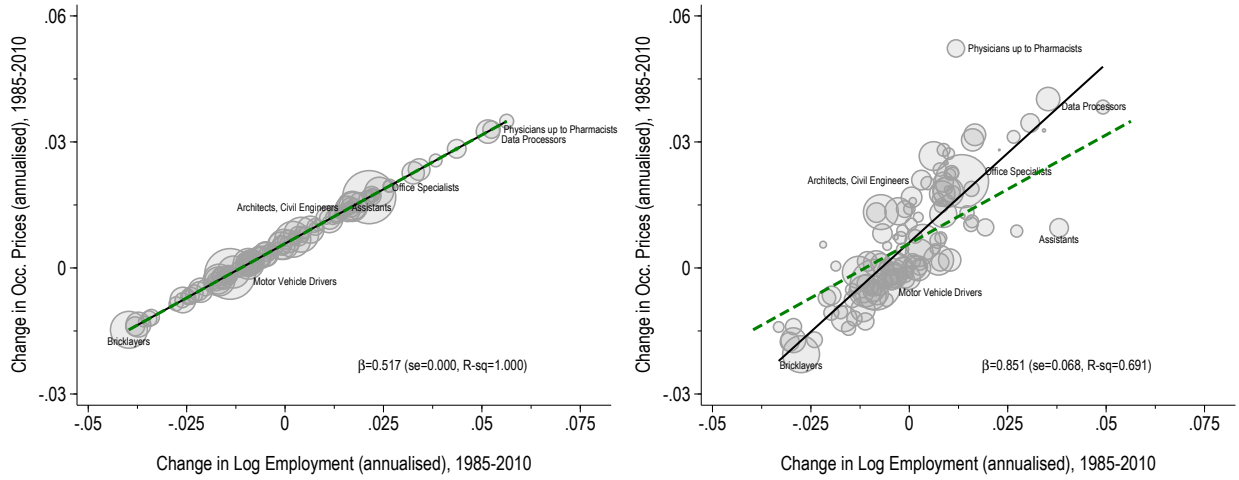
Second, a key strength of our framework is that it allows us to decompose the contribution of demand and supply shocks to the observed wage and employment changes. This decomposition, which follows from equations (16) and (17) in Section 5, reveals the distinct roles played by demand and supply shocks. Demand shocks, depicted in grey, emerge as the primary drivers behind both wage and employment changes. They are, however, more important in explaining wage changes than in explaining employment changes. For the latter, as we extensively discuss in Section 6.2 and [Table 3](#), supply shocks and supply heterogeneity also play a role.

Finally, and related to the last point, switching off supply heterogeneity and considering counterfactual outcomes from the fully homogeneous model (i.e. comparing [Figure E.4](#) to [E.3](#)) result in smaller wage changes and larger employment changes across occupations. The intuition for this is, as we discuss in the main text, that heterogeneous cross-effects make occupations less price elastic. As such, realised labour supply elasticities captured by the full model are lower than those captured in the homogeneous model.

**Figure E.1:** Counterfactual Changes of Prices and Employment (II)

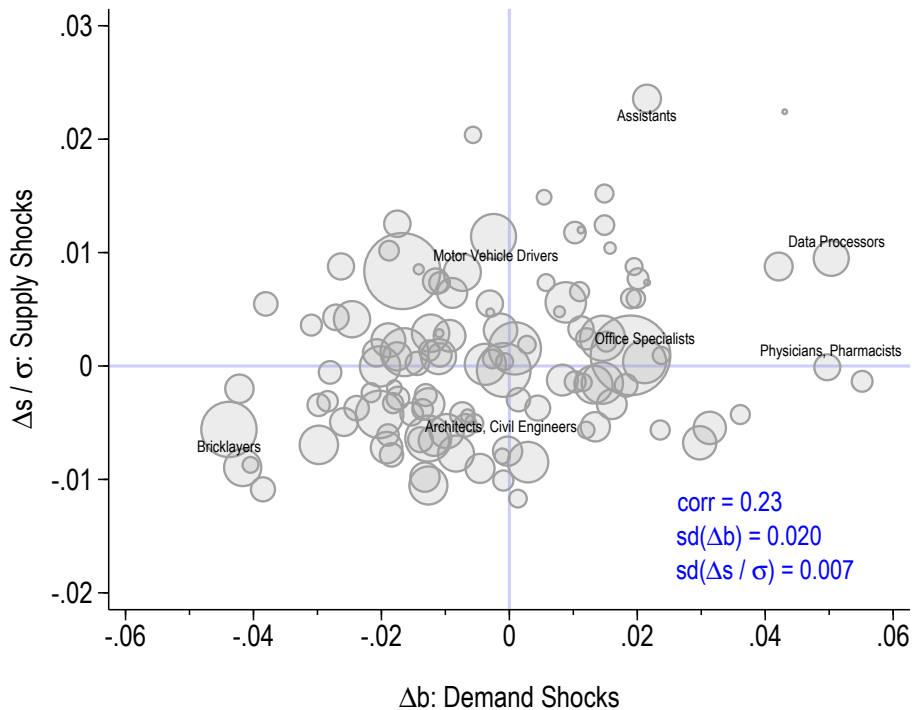
**(a)** Demand shocks only; Fully-homog. supply

**(b)** ... Fully heterogeneous supply



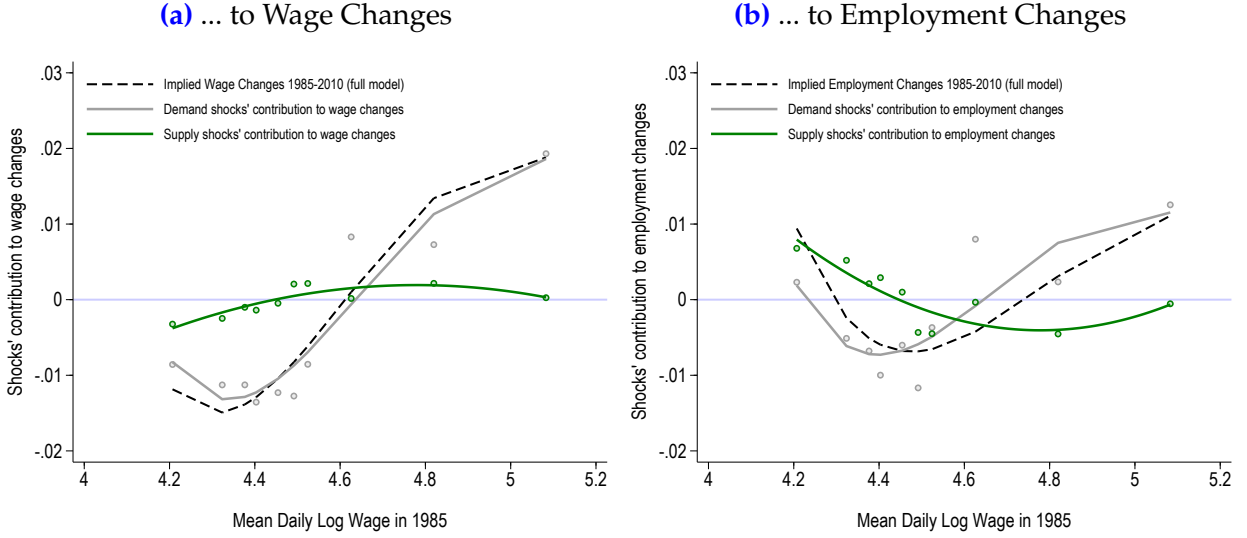
Notes: The figure shows occupational price and employment changes for different manipulations of  $\Delta s$  and the elasticity matrix  $D$ . In E.1a, both supply shocks and heterogeneity in  $D$  are switched off (i.e.  $\Delta s = \Delta s_{off} = 0$  and  $D_{hom}$ ), leaving only demand shocks. E.1b introduces heterogeneous own- and cross-price elasticities (i.e., full matrix  $D$  is used). For the exact description of the counterfactuals, see Section 6. The OLS with slope coefficients, standard errors, and R-squared is shown for each panel. The regression line in E.1a is repeated as green-dashed in both panels. Marker size indicates the baseline employment (in 1985) in each occupation.

**Figure E.2:** Distribution of Demand and Supply Shocks by Occupation



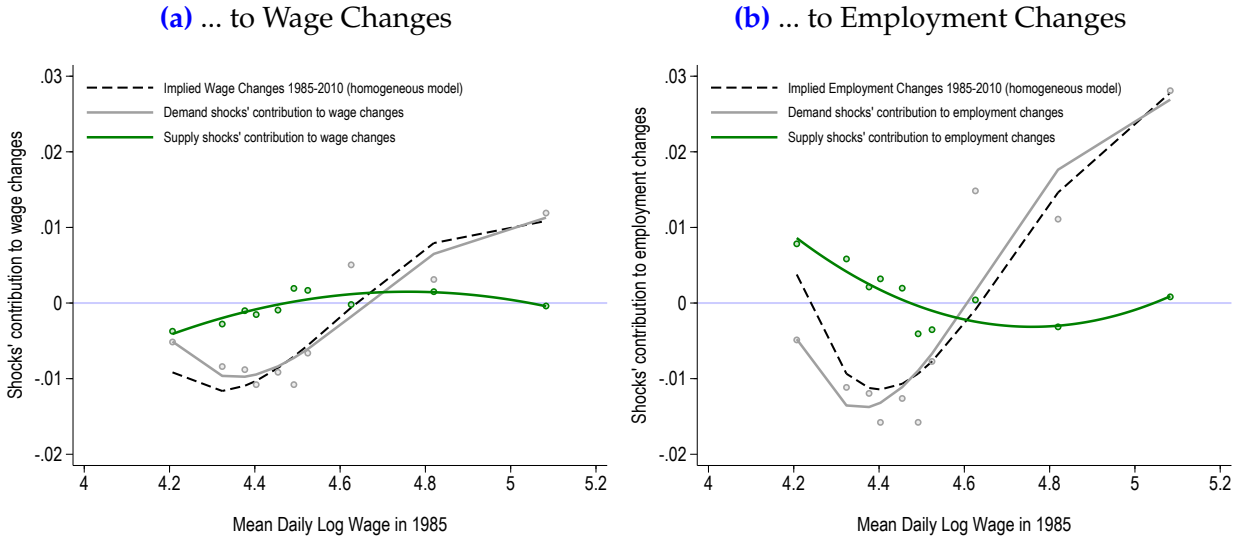
Notes: The figure shows the distribution of demand and supply shocks by occupation. Marker size indicates the baseline employment (in 1985) in each occupation. The standard deviations and correlation of demand and supply shocks are reported in the figure.

**Figure E.3: Contribution of Demand and Supply Shocks (Full Model)**



Notes: The left panel E.3a shows the contributions to price changes of demand and supply shocks across the wage distribution for the full model. These are given by  $V\Delta\mathbf{b}$  and  $-\frac{1}{\sigma}V\Delta\mathbf{s}$ , as in eq. (16). The right panel E.3b shows the contributions to employment changes of demand and supply shocks across the wage distribution for the full model. These are given by  $\theta DV\Delta\mathbf{b}$  and  $V\Delta\mathbf{s}$ , as in eq. (17). For supply, a quadratic is used for the smoothed fit. For demand, a fractional cubic is used.

**Figure E.4: Contribution of Demand and Supply Shocks (Fully Homogeneous Model)**



Notes: The left panel E.3a shows the contributions to price changes of demand and supply shocks across the wage distribution for the fully homogeneous model. These are given by  $V_{hom}\Delta\mathbf{b}$  and  $-\frac{1}{\sigma}V_{hom}\Delta\mathbf{s}$ , parallel to eq. (16) and where  $V_{hom} = \left(\frac{\theta}{\sigma}D_{hom} + I\right)^{-1}(I - W)$ . The right panel E.3b shows the contributions to employment changes of demand and supply shocks. These are given by  $\theta D_{hom}V_{hom}\Delta\mathbf{b}$  and  $V_{hom}\Delta\mathbf{s}$ , parallel to eq. (17). For supply, a quadratic is used for the smoothed fit. For demand, a fractional cubic is used.

## F Extensions and Robustness: Supplementary Material

In this section, we present details on the extensions and robustness checks of the main findings. We first extend the model to incorporate non-employment transitions. Second, we study changes in occupational prices and employment by five-year sub-period. Lastly, we introduce an alternative method for estimating changes in occupational prices.

### F.1 Accounting for Non-Employment Transitions

A driver of heterogeneity in occupational growth that we omit in the main analysis is the extensive margin of employment. This may be particularly important if young workers' entry and old workers' exit from the labour market affect specific occupations' growth (see [Autor & Dorn \(2009\)](#) for US routine occupations). The secular decline of German unemployment from the mid-2000s may also be relevant in this respect.

In line with eq. (1), we interpret indirect utility in  $M$  different non-employment states  $m \in \{N + 1, \dots, N + M\}$  as containing pecuniary payoffs, transition costs, and idiosyncratic components. While pecuniary payoffs  $p_m$  are unobserved, the empirical framework can be extended to control switches to and from different non-employment states.

We start by computing a new elasticity matrix that includes all transitions to and from non-employment states. We can then extend eq. (11) to  $N + M$  occupations, with  $M$  referring to different non-employment sectors:

$$\Delta e_j \approx \theta \sum_{k=1}^{N+M} d_{jk} \Delta p_k = \theta \sum_{k=1}^N d_{jk} \Delta p_k + \sum_{m=N+1}^{N+M} (\theta \Delta p_m) d_{jm} \quad (44)$$

The first summation on the right-hand side represents our standard (own- and cross-occupation) effects, while in the second summation, we explicitly group factors  $\theta \Delta p_m$  together. This is to indicate that here we treat  $d_{jm}$  as control variables for occupation  $j$ 's elasticity with respect to non-employment state  $m$ . The  $\theta \Delta p_m$  coefficient on the respective control represents the combination of pecuniary preferences and changes in non-employment 'prices'.

In what follows, we show the results from these estimations with  $M = 3$  different non-employment sectors: unemployment, out of the labour force (during the career and including part-time as well as employment with benefit receipt), and entry or exit due to newly joining the labour force at age 25–32 or retiring at age 52–59. A limitation of the records from unemployment insurance is that we cannot observe the exact reasons for individuals entering or leaving the dataset (e.g. health shock, discouraged worker, emigration, self-employment, military service or becoming a civil servant). Outside the age

range for labour market entry or retirement, these are all treated as out of the labour force for our purposes. [Table B.5](#) in [Appendix B](#) shows the resulting own-elasticity elements. These tend to be slightly larger than  $d_{jk}$  in our baseline matrix  $D$ , reflecting a relevant amount of transitions in many occupations with non-employment sectors, but they are also clearly correlated.

[Table F.1](#) then reports the estimation results for eq. (44). The R-squared is higher than in the main text as more of the heterogeneity in employment growth can be explained when allowing for occupations' different elasticities with respect to non-employment states. Importantly, the estimated role of own- and cross-occupation effects turn out similar to the main results (both OLS and IV estimates). In unreported analyses, we verify that the main results do not change when further separating part-time work and work with benefit receipt from 'out of the labour force' ( $M = 4$ ), or when merging the three states into one single non-employment sector ( $M = 1$ ). We also verify that [Figure 2b](#) is essentially the same if we split occupations by own-price elasticity arising from the model with non-employment transitions.

**Table F.1:** Accounting for Non-Employment Transitions.  
Determinants of Employment Changes: Own- and Cross-Effects (OLS–IV)

		Dependent Variable: $\Delta e_j$		
		Unrestricted Model	Restricted Model	
		(1)	(2)	(3)
fixed relationship:	$\bar{d}_{diag}\Delta p_j$	3.70 (0.74)		
heterogeneous own effect:	$(d_{jj} - \bar{d}_{diag})\Delta p_j$	3.27 (0.99)	4.06 (0.68)	4.48 (1.24)
total cross effect:	$\sum_{k \neq j} d_{jk}\Delta p_k$	2.83 (1.19)		
R-squared		0.470	0.463	-
Number of occupations		120	120	120
Estimation method		OLS	OLS	IV
Non-employment controls		Yes	Yes	Yes
F-statistic 1st Stage		-	-	36

*Notes:* Specifications as in the main text [Sections 4–5](#) other than that regressions now control for occupations' elasticities  $d_{jm}$  with three different non-employment states indexed by  $m$ . These are: unemployment; out of the labour force (during the career and including part-time as well as employment with benefit receipt), and entry or exit due to newly joining the labour force at age 25–32 or retiring at age 52–59. The regressors in column (2) are the full  $\sum_k d_{jk}\Delta p_k = \mathbf{d}_j\Delta \mathbf{p}$  together with  $d_{j,N+m}$  for  $m \in \{1, 2, 3\}$ . In column (3), these are instrumented by  $\mathbf{d}_jV\mathbf{r}$  together with  $d_{j,N+m}$  (see eq. (20)).

## F.2 Analysis in Five-Year Sub-Periods

In the main analysis, we study changes in occupational prices and employment over the period 1985–2010. In this section, we split this longer interval into five-year sub-periods (1985–1990, 1990–1995, 1995–2000, 2000–2005, and 2005–2010), to explore robustness and potential temporal heterogeneity.

The pooled panel sample containing 600 observations (120 occupations  $\times$  5 sub-periods) is used to estimate an extended version of eq. (11):

$$\Delta e_{jt} = \alpha + \theta d_{jj} \Delta p_{jt} + \theta \sum_{k \neq j} d_{jk} \Delta p_{kt} + \delta_t (+\gamma_j) + \varepsilon_{jt} \quad (45)$$

where  $t$  refers to a five-year period, and the matrix of elasticities  $D$  can be obtained using the baseline period 1975–1984 as previously or using the lagged matrix from the preceding five-year period (e.g. for the period 1995–2000, the matrix of elasticity is computed using employment transitions over the period 1990–1995).<sup>57</sup> The period fixed effects ( $\delta_t$ ) capture unobserved time-specific shocks or trends that affect all occupations uniformly within each sub-period. A more demanding specification additionally includes occupation fixed effects ( $\gamma_j$ ), removing average occupational growth over 1985–2010 and identifying only from accelerations/decelerations in the respective sub-period.

Figure F.1 plots prices against employment growth for the pooled sample of 600 occupation–sub-periods (F.1a) as well as separately for each sub-period (F.1b), analogous to the main text Figure 2b. The previous finding is strengthened in the sense that each regression slope for above-median own-price elastic occupations (in blue) is flatter than any slope for below-median own-price inelastic occupations (in red). Similarly, Table F.2 shows that linear OLS and IV estimation on the pooled data essentially reproduce the results obtained in the main text. Even in estimations with occupation fixed effects ( $\gamma_j$ ), which only use deviations of price changes from their 1985–2010 averages interacted with the price elasticities, results are broadly similar to before.<sup>58</sup> In sum, estimation in a series of shorter intervals shows that the role of occupational price elasticities persists, with some evidence that even acceleration/deceleration of price growth in different sub-periods is translated into employment growth according to these elasticities.

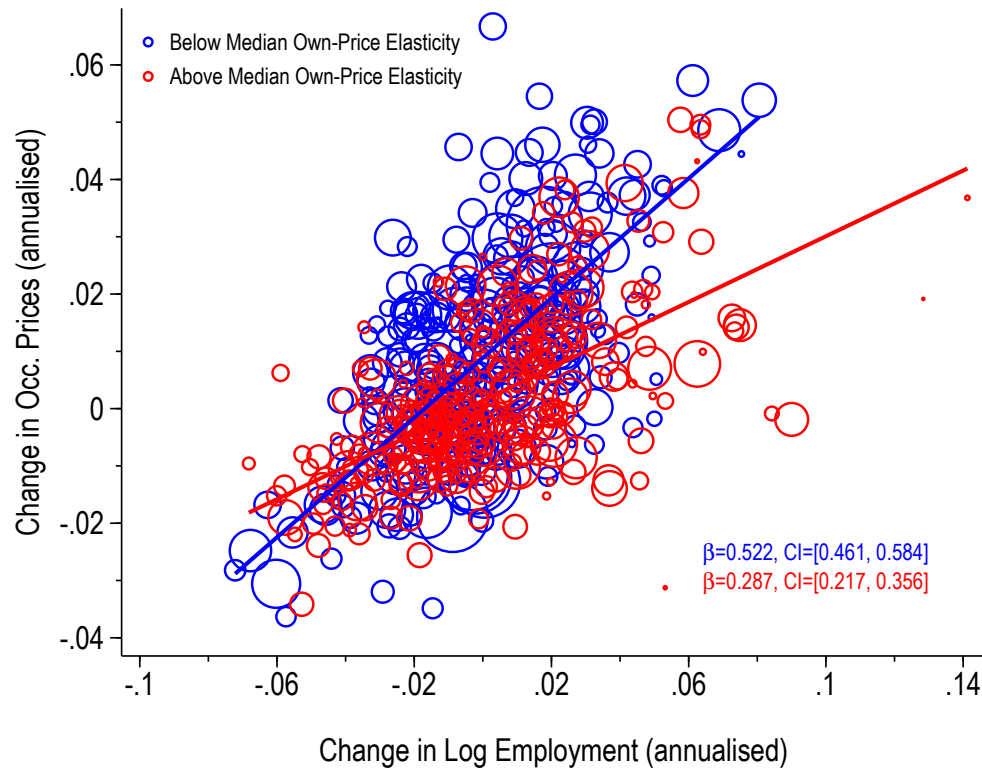
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<sup>57</sup>Consistent with the high autocorrelation of matrix  $D$  over time discussed in Table B.3, results are similar whether we use the baseline or the lagged matrix.

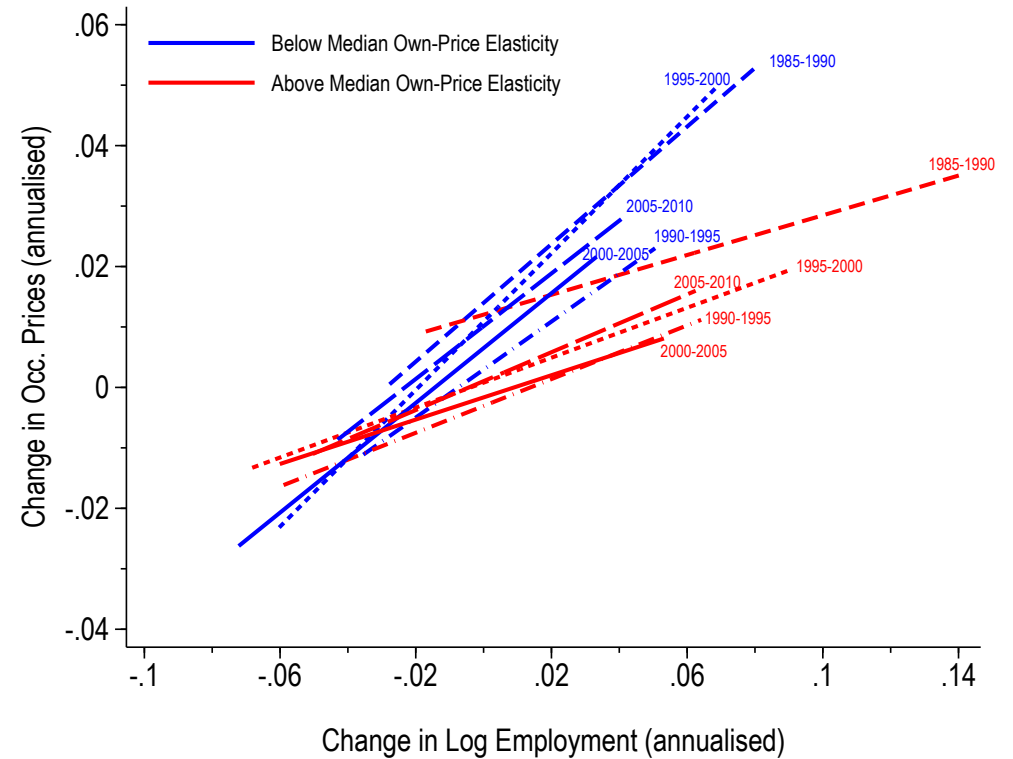
<sup>58</sup>Note that we can only do the OLS for this as our instrument does not vary by period.

**Figure F.1:** Occupational Price and Employment Changes (by Own-Price Elasticity Median Split)

**(a)** Pooled Sub-Periods. 600 Occupations  $\times$  Sub-Periods



**(b)** By Sub-Period



Notes: The figure shows the lines from an occupation-size weighted regression of price change on employment change, split by occupations below (blue, inelastic) and above (red, elastic) the median own-price elasticity ( $d_{jj}$ ). **Figure F.1a** shows this for the pooled sample of 600 occupation-sub-periods. **Figure F.1b** shows this separately for each sub-period. Sub-periods are: 1985–1990, 1990–1995, 1995–2000, 2000–2005, and 2005–2010.  $\beta$  refers to the slope coefficient and  $CI$  stands for the 95% confidence interval. Marker size indicates the baseline employment in each occupation.

**Table F.2:** Full Model Pooled Sub-Periods (OLS–IV)

		Dependent Variable: $\Delta e_j$			
		Unrestricted model	Restricted model		
		(1)	(2)	(3)	(4)
fixed relationship:	$\bar{d}_{diag}\Delta p_j$	3.90 (0.67)			
heterogeneous own effect:	$(d_{jj} - \bar{d}_{diag})\Delta p_j$	4.04 (0.83)	4.01 (0.56)	3.18 (0.51)	4.17 (1.32)
total cross effect:	$\sum_{k \neq j} d_{jk}\Delta p_k$	3.69 (1.09)			
R-squared		0.492	0.491	0.791	-
Number of occupations		600	600	600	600
Estimation method		OLS	OLS	FE	IV
F-statistic 1st Stage		-	-	-	13

*Notes:* The table presents the estimates from different versions of eq. (45). Pooled panel sample containing 600 observations (120 occupations  $\times$  5 sub-periods). Sub-periods are: 1985–1990, 1990–1995, 1995–2000, 2000–2005, and 2005–2010. All regressions include dummies for the respective five-year estimation period. The regressor in columns (2)–(4) is the full  $\sum_k d_{jk}\Delta p_k = \mathbf{d}_j\Delta \mathbf{p}$  and in column (4) this is instrumented by  $\mathbf{d}_jV\mathbf{r}$  (see eq. (20)). Column (3) uses occupation fixed effects. Observations weighted by occupation  $j$ 's initial employment size (e.g. for the period 1985–1990, this is 1985; for the 2000–2005 period, this is 2000, and so on). Standard errors clustered at the occupation level in parentheses; all coefficients shown are significant at the 1% level.



### F.3 Alternative Occupational Price Estimation

The main results in Section 4–5 use wage changes of occupation stayers’ (i.e., workers who do not switch occupations from one year to the next) as the main estimate of changes in occupational prices. This accounts flexibly for the selection into occupations based on observable and unobservable individual characteristics. In this section, we use an alternative price estimation that also controls for the occupation-specific effect of time-varying observable characteristics on wages.

In this approach, originally proposed by Cortes (2016), observed log wages for individual  $\omega$  in period  $t$  are modeled by

$$\ln w_t(\omega) = \sum_j Z_{jt}(\omega) \varphi_{jt} + \sum_j Z_{jt}(\omega) X_t(\omega) \zeta_j + \sum_j Z_{jt}(\omega) \kappa_j(\omega) + \mu_t(\omega) \quad (46)$$

where  $Z_{jt}(\omega)$  is an occupation selection indicator that equals one if individual  $\omega$  chooses occupation  $j$  at time  $t$ ,  $\varphi_{jt}$  are occupation-time fixed effects, and  $\kappa_j(\omega)$  are occupation-spell fixed effects for each individual. The model allows for time-varying observable skills (e.g. due to general human capital evolving over the life cycle) by including in the control variables  $X_t$  a set of dummies for five-year age bins interacted with occupation dummies.<sup>59</sup> Finally,  $\mu_t(\omega)$  reflects classical measurement error, which is orthogonal to  $Z_{jt}(\omega)$ . It may be interpreted as a temporary idiosyncratic shock that affects the wages of individual  $\omega$  in period  $t$  regardless of their occupational choice. The estimated occupation-year fixed effects ( $\varphi_{jt}$ ) are the parameters of interest, which allow studying changes over time in occupation’s log prices ( $\Delta p_j = \varphi_{j,2010} - \varphi_{j,1985}$ ).

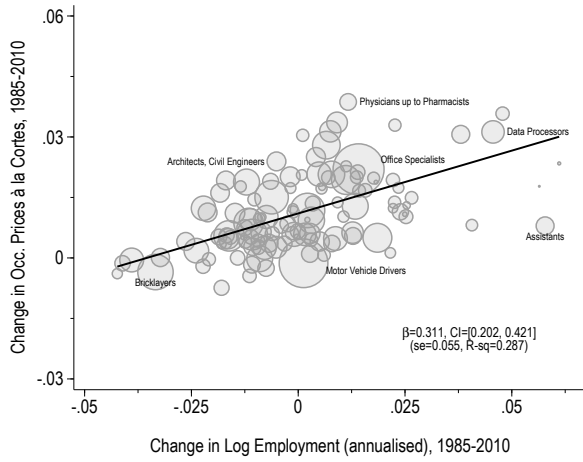
The results using occupational prices à la Cortes (2016) turn out similar to our main results. The main figures of the paper using this alternative measure for changes in occupational prices are replicated in Figure F.2. The main regression results, shown in Table F.3, including those when accounting for non-employment transitions, turn out very similar. Our findings hence remain consistent and robust to this alternative price estimation.

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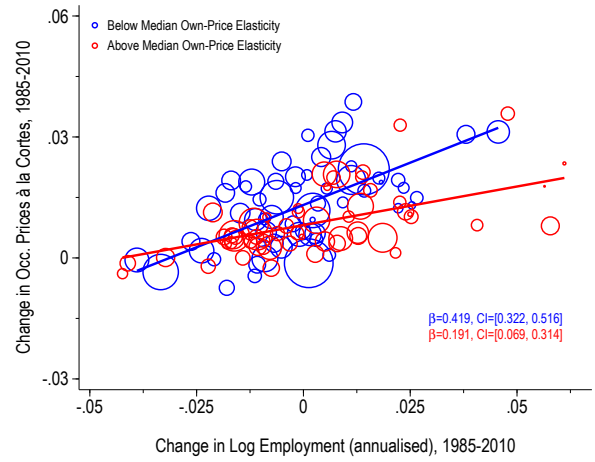
<sup>59</sup>The bins are for ages 25–29, 30–34, 35–39, 40–44, 45–49, 50–54, and 55–59.

**Figure F2: Occupational Prices à la Cortes (2016) and Employment**

**(a) Overall Relationship**



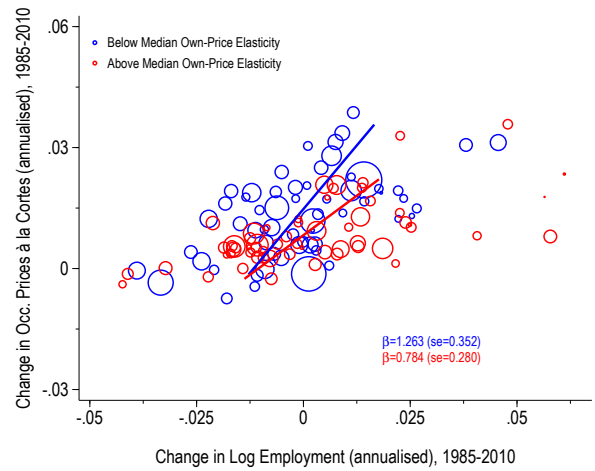
**(b) By  $d_{ij}$  Median Split**



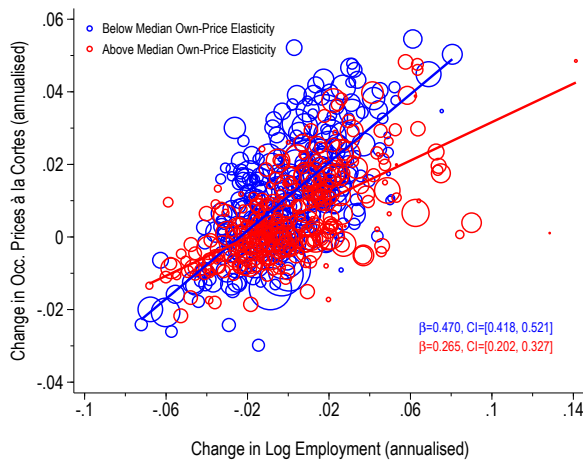
**(c) By  $d_{ij}$  Quartiles**



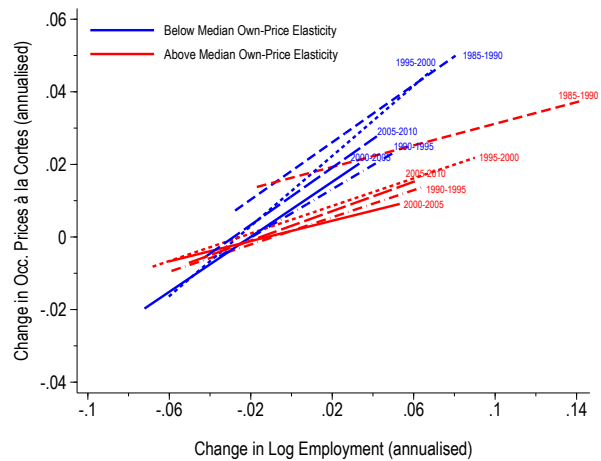
**(d) IV Second-Stage: Inverse Supply Curve**



**(e) Pooled Sub-Periods. By  $d_{ij}$  median split**



**(f) Sub-Periods. By  $d_{ij}$  median split**



Notes: Panel (a) shows the line from an occupation-size weighted regression of price change on employment change. Panel (b) shows a split by occupations below (blue, inelastic) and above (red, elastic) the median own-price elasticity  $d_{ij}$ . Panel (c) shows a split by occupations in the lowest (blue), second (green), third (orange), and highest (red) quartile of  $d_{ij}$ . Panel (d) shows, by  $d_{ij}$  median split, the IV-2SLS second-stage of occupations' price on employment changes using initial task contents as the instrument. Panel (e) shows the overall regression line for the pooled 600 occupations  $\times$  sub-periods case. Finally, panel (f) splits by  $d_{ij}$  median the pooled occupations  $\times$  sub-periods sample.  $\beta$  refers to the slope coefficient,  $CI$  to the 95% confidence interval,  $se$  refers to standard error, and  $R-sq$  stands for R-squared of the regression. Marker size indicates the baseline employment in each occupation.

**Table F.3:** Occupational Prices à la Cortes (2016) and Changes in Employment. Main Results.

		Dependent Variable: $\Delta e_j$						
		Unrestricted Model	Restricted Full Model					
		(1)	(2)	(3)	(4)	(5)	(6)	(7)
fixed relationship:	$\bar{d}_{diag}\Delta p_j$	4.46 (1.30)						
heterogeneous own effect:	$(d_{jj} - \bar{d}_{diag})\Delta p_j$	4.65 (1.73)	5.18 (1.15)	6.48 (2.12)	4.76 (1.10)	5.45 (1.78)	4.43 (0.70)	4.92 (1.56)
total cross effect:	$\sum_{k \neq j} d_{jk}\Delta p_k$	3.23 (1.81)						
R-squared		0.371	0.350	-	0.402	-	0.486	-
Number of occupations		120	120	120	120	120	600	600
Estimation method		OLS	OLS	IV	OLS	IV	OLS	IV
F-stat 1st Stage		-	-	10	-	23	-	11
Accounting for non-employment transitions		no	no	no	yes	yes	no	no
Analysis pooling five-year sub-periods		no	no	no	no	no	yes	yes

Notes: Regressor in columns (2)–(7) is  $\sum_k d_{jk}\Delta p_k$ , i.e. corresponding to the full model. In columns (3), (5), and (7), regressor  $\sum_k d_{jk}\Delta p_k = \mathbf{d}_j\Delta \mathbf{p}$  is instrumented by  $\mathbf{d}_jV\mathbf{r}$  (see eq. (20)). In columns (4)–(5), we consider  $M = 3$  different non-employment sectors: unemployment, out of the labour force (during the career and including part-time as well as employment with benefit receipt), and entry or exit due to newly joining the labour force at age 25–32 or retiring at age 52–59. In columns (6)–(7), we use the pooled panel sample containing 600 observations (120 occupations  $\times$  5 sub-periods). Sub-periods are: 1985–1990, 1990–1995, 1995–2000, 2000–2005, and 2005–2010. These regressions include dummies for the respective five-year estimation period and cluster standard errors at the occupation level. Observations weighted by occupation  $j$ 's initial employment size.