Product market regulation, firm size, unemployment and informality in developing economies*

Abstract

This paper studies the impact of product and labor market regulations on informality and unemployment in a general framework where formal and informal firms are subject to the same externalities, differing only with respect to some parameter values. Both formal and informal firms have monopoly power in the goods market, they are subject to matching friction in the labor market, and wages are determined through bargaining between large firms and their workers. The informal sector is found to be endogenously more competitive than the formal one. We find that lower strictness of product or labor market regulations lead to a simultaneous reduction in informality and unemployment. The difference between these two policy options lies on their effect on wages. Lessening product market strictness increases wages in both sector but also increases the formal sector wage premium. The opposite is true for labor market regulation. We show that, while the so-called overhiring externality due to wage bargaining takes place in both sectors, and it translates into a smaller relative size of the informal sector.

Keywords Informality; Product and Labor Market Imperfections; Firm Size

JEL Classification E24; E26; J60; L16; O1

1 Introduction

Informal activities are pervasive in both developed and developing economies. According to Schneider and Enste (2000) estimates, the size of the shadow economy as a percentage of GDP ranges from 25 to 60% in Latin America, from 13 to 50% in Asia, and it is around 15% among

^{*}We thank Pedro Miguel Olea de Souza e Silva for excellent research assistance. We also thank participants from PET'10 Conference and from seminars at Université de Cergy-Pontoise, Université du Maine, Université Paris II, Université de Strasbourg, CEPII and University of Cambridge for comments and suggestions. We are indebted to Christian Haefke and Etienne Lehmann for valuable comments on a previous version of this paper. The usual disclaimer applies.

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OECD countries, reaching 30% in some European countries. Informal firms differ from formal ones in a number of measurable characteristics, and there is a growing literature trying to understand the causes of informality and its differences from formal businesses.

In developing countries, in particular, informality seems to be omnipresent in virtually all sectors of the economy. In Brazil, about 60% of all food-retailing market is operated by informal marketplaces, and about one third of all processed meat comes from informal businesses. Similar ratios are found in audiovisual and software sector, pharmaceutical industry, gasoline retailing, and so on (see Capp and Jones, 2005). We take the view that, in developing countries, informal firms should be taken as being subject to the same economic environment and they should face the same externalities as the formal ones, except, of course, for the fact that informal firms do not comply with taxes and regulations.

In this spirit, we propose a general framework where formal and informal firms are equal in all aspects, except for the value of some exogenous parameters related to labor market matching technology, productivity, workers bargaining power and, evidently, entry costs and labor taxes. Our numerical simulation is successful in replicating the key characteristics of the Brazilian economy. We study the effects of changes in product market regulation (PMR) modeled as changes in entry costs in the formal sector, and of changes in labor market regulation (LMR), proxied by changes in workers bargaining power, on the main endogenous variables of the model. We find that a fall in PMR strictness reduces unemployment and the size of the informal sector while it raises wages. A fall in LMR, on its turn, also reduces both unemployment and informality, but it reduces wages.

One noteworthy feature of our model is that the number and size of firms are endogenously determined. Our model endogenously generates a more competitive informal sector, which is in line with empirical evidence. Moreover, we show that both a fall in PMR and in LMR render the formal sector closer to the informal one in terms of competitiveness.

We chose Brazil as our benchmark case since it is a developing economy with a large informal sector. Brazil's informal sector employs around 40% of its labor force, while the country's unemployment rate ranged from 7% to 13% over the last decade. Moreover, Brazil has relatively high barriers to entry in the product market (Djankov et al., 2002), while labor legislation appear relatively moderate compared to some other Latin American countries (Botero et al., 2004). In this perspective, it is interesting to examine how unemployment and informality would react, had the government chosen a different mix between product and labor market regulations, that is, lower barriers to entry and/or stricter labor regulations.

There is a recent and growing literature on unemployment and informality in developing

countries. Our analysis highlights distortions that have not yet been contemplated by previous models as being shared by both formal and informal sectors. In sum, in our model: (i) there are frictions in both formal and informal labor markets; (ii) job seekers are identical and can find jobs in both sectors, that is, the labor market is not segmented; (iii) the number and size of firms in each sector is endogenous, which renders market power also endogenous; (iv) wages are set through bargaining between large firms and their workers, which generates externalities in the two sectors.

It is worth highlighting that, with respect to the labor market, we consider two sources of distortions. First, there are the standard congestion externalities linked to the matching process. Second, there are distortions resulting from wage bargaining between firms and workers, which may generate either over- or underhiring. These wage bargaining distortions were not considered in previous literature on informality. The size of overhiring is related to workers bargaining power and to the price elasticity of demand faced by firms. Since those two features are allowed to differ across sectors, the size of the overhiring externality itself may vary across sectors. Our numerical exercises indicate that overhiring takes place in the formal sector, while there is underhiring in the informal sector. This translates into a smaller relative size of the informal sector compared to the case without overhiring.

Following Blanchard and Giavazzi (2003), a number of recent papers have studied the impact of PMR and LMR on unemployment in economies with frictions in the labor market (e.g. Delacroix, 2006, Ebell and Haefke, 2009, Felbermayr and Prat, 2010). Those studies, however, do not consider the existence of an informal sector. Given that informality represents a large share of the economies, it is important to understand the impacts of policies on the informal sector as well. For instance, the relative size of the informal sector should be responsive to changes in the costs involved into creating a new business, since many of such costs are avoided by firms entering the informal sector. Indeed, Figure 1 below illustrates that, among Latin American countries, the informal sector tends to be larger in countries where barriers to entry are stricter. Many developing countries tend to have relatively larger barriers to entry of new businesses (see Djankov et al., 2002), which could be part of the explanation of informality being more pervasive among those countries.

The economic literature on informality has recently turned its attention to search and matching models of the labor market. Zenou (2008) studies the impact of labor market policies on informality, and he models the formal sector as subject to labor market frictions and presenting unemployment, while the informal one is taken as being competitive. Although it is generally acknowledged that one of the advantages of the informal sector relies on the fact that finding a

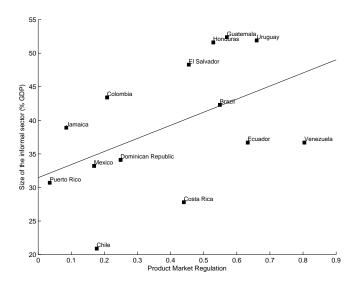


Figure 1: Informality and PMR in developing countries

job is easier, there is at best no appealing evidence that the informal labor market should be a fully competitive one. In any case, this particular case can easily be embedded in a more general model incorporating matching frictions in both formal and informal labor markets, as the one developed in this paper.

In Fugazza and Jacques (2004), there are search frictions in both sectors, but they are still segmented. Workers are not allowed to seek for jobs in the formal and informal sectors simultaneously, and they differ with respect to a 'moral' cost of working in the informal sector. In the case of developing countries, there is evidence that the informal sector is a integral part of the economy, rather than a residual sector in a segmented labor market. Based on the Latin American experience, Maloney (2004) claims that the informal sector should be viewed as an unregulated micro-entrepreneurial sector instead. In terms of the unemployed's behavior, for instance, job seekers in developing countries are likely to look simultaneously for formal and informal jobs, either because they cannot afford to do otherwise, or because there is less social stigma related to taking a job in the informal sector. In contrast, in more developed countries workers look for a job in the informal sector only after having failed to find one in the formal sector.

In Satchi and Temple (2009) workers can be employed either in agriculture or in a manufacturing sector. Agriculture is taken as being perfectly competitive while in manufacturing there are formal firms subject to matching frictions, and informal self-employed workers who seek formal jobs. Although there is no labor market segmentation, informality is still viewed as a disadvantaged or residual sector in that paper. Kolm and Larsen (2006) and Ulyssea (2009) assume, as we do, that unemployed workers seek both formal and informal jobs, and that both types of jobs are subject to matching frictions. Such assumptions on workers search behavior seem consistent with the empirical evidence on the Brazilian labor market presented in the next section, where it is shown that there is a relatively large degree of mobility between formal and informal jobs. This also leads us to argue that job seekers probably accept both types of jobs and that the formal and informal labor markets are not segmented for the workers. Kolm and Larsen (2006) analyze the effects of higher punishment and audit rates on labor market performance, while Ulyssea (2009) focuses on endogenous differences in productivity between the two sectors. We abstract from those considerations to focus on differences in firm size across sectors, which render their relative degree of competitiveness endogenous.

Alternatively, Boeri and Garibaldi (2006) and Albrecht et al. (2009) are interested in explaining the sorting of workers across sectors, and they assume that workers differ in their productivity. We are aware of the empirical evidence suggesting differences in workers skills and firms productivity in formal and informal sectors, but the aim of our paper is not to explain these features. We focus, instead, on explaining differences in firms size and competitiveness across sectors, as well as the impact of PMR and LMR on unemployment, the relative size of informal and formal sector, and their relative wages.

A common assumption to all those previous models is that each firm is allowed to hire only one worker. We depart from this assumption and let firms hire as many workers as they desire. El Badaoui et al. (2010) develop, to our knowledge, the only alternative model in this literature in which firm size is also an endogenous variable. Based on Burdett and Mortensen (1998), they build a model with on-the-job search and wage posting (instead of wage bargaining) where firms choice of wages determines their size. In our model, however, firms choose their size directly and wages are a result of a bargaining process between large firms and their workers. Additionally, firms size will ultimately have an effect on the number of firms in a sector, which, in turn, impacts firms market power in the goods market.

The paper is organized as follows. Section 2 presents some stylized facts for the Brazilian economy. The theoretical model is described in Section 3. The equilibrium is derived in section 4 while section 5 provides some quantitative exercises. Section 6 provides an in-depth discussion of the labor and product markets imperfections. Section 7 concludes. Technical details are gathered in the appendix.

2 Stylized Facts

We use data from the Monthly Employment Survey (Pesquisa Mensal de Emprego, or PME) conducted by the Brazilian Institute of Geography and Statistics (IBGE) for the greater metropolitan regions of São Paulo, Rio de Janeiro, Belo Horizonte, Porto Alegre, Salvador and Recife. PME collects information on employment and earnings, as well as on other observable characteristics such as the workers years of schooling, age, gender, state of residence, sector of activity and occupation.

In Brazil, all workers formally employed in the private sector are required to have a working card ('carteira de trabalho'), thus, by observing whether the individual has a valid working card we are able to sort formal and informal workers.¹ Among the self employed, it is also possible to distinguish those who pay social contributions from those who do not. We then define informal workers as those informally employed in the private sector and the self employed who do not pay social contribution. As shown in Figure 2, from 2003 to 2010 the share of the informal sector declined from around 40 to 35% in Brazil, while the unemployment rate also decreased from around 12 to 7%.

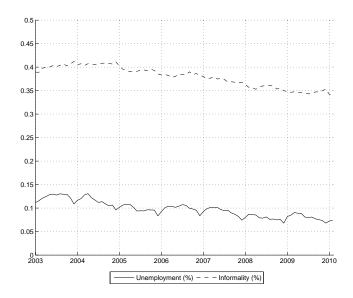


Figure 2: Informality and unemployment in Brazil

PME interviews the same individual at different moments in time for a period of 16 months. For each individual, four interviews are conducted over the first four months, then there is an

¹Notice that we also need the information of whether the individual works in the public sector, since public servants do not hold a working card as well. This question was included in the PME questionnaire from 2002 on. We then choose to use data starting in 2002. For data prior to 2002 it was not possible to sort informal workers from those working in the public sector.

interval of eight months, and once again the same individual is interviewed for four consecutive months. Thus the information is gathered in months t, t+1, t+2, t+3, t+12, t+13, t+14 and t+15. We use the fourth (t+3) and eighth (t+15) interviews of each individual to compute the transition frequencies across employment states. Table 1 below presents the transitions across unemployment, formality and informality, where each line displays the state of origin and the column the destination state. The table depicts some interesting patterns. An unemployed worker has virtually equal probability of being in either one of the three states one year later. Formal workers have a probability of 87.4% of remaining formal, while only 71.7% of informal workers remain informal after one year. Finally, informal workers become formal with a probability of 23.1%, whereas the reverse is true with a frequency of only 9.3%.

State T \ State T+1	Unemployed	Employed: Registered	Employed: Unregistered			
Unemployed	35,8%	32,1%	32,1%			
Employed: Registered	3,4%	87,4%	9,3%			
Employed: Unregistered	5,3%	23,1%	71,7%			
Total	6,6%	62,2%	31,2%			
Total Observations (Different Individuals)		246 574				
Average Observations per Month		3 378				
Overall Period	Jan 2003-Feb 2010					
Estimation Sample		Jan 2004-Feb 2010				
Source	Monthly Labor Survey (PME) - IBGE					

Table 1: Transition probabilities

We have also computed the same transition matrix using two alternative subsamples.² In first one we restrict the sample to workers 23 and 65 years old, which corresponds to 155,002 observations. In the second subsample we consider only low-skill workers (those with lower than high-school education), which amounts to 124,569 observations. In all cases, we get broadly the same picture, with marginal differences. In particular, there are more marked differences in the probabilities for an unemployed to find a formal or an informal job using those subsamples. In the first subsample, among the unemployed at time t, 34.5% stay unemployed, 31.1% find a job in the formal sector, while 34.4% become an informal worker at t + 1. In the second subsample, the same percentages are 34.9%, 29.4 and 35.7% respectively.

Formal sector wages are 45 to 55% higher than wages in the informal sector. We know, however, that formal and informal sector workers differ in a number of characteristics that

²The results are available upon request.

affect wages. We therefore estimate the wage premium in the formal sector after controlling for observable individual characteristics available in the data.³ Figure 3 shows the path of the controlled wage gap from 2007 to 2010 and its confidence interval of 95%. Formal sector wage premium ranged from 23 to 30%, which is indeed much smaller than the observed one but still considerable. Note also that the formal sector wage premium decreased by approximately 20% over the period.⁴

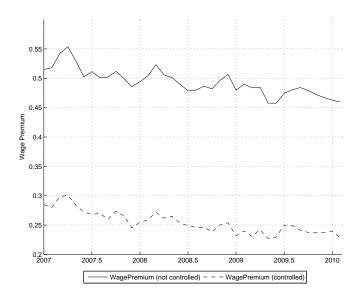


Figure 3: Wage Premium

With respect to firm size, while it is not possible to know the exact number of employees in a firm, we are able to divide firm size into three categories: the first one corresponds to firms with 2 to 5 employees, the second one with 6 to 10 employees, and the third with 11 employees or more. We create a size index by assigning a number from 1 to 3 to each of these categories. Figure 4 presents the averages of this size index for the informal and formal sectors. Formal sector firms are clearly larger than informal ones.

3 The model

We consider an economy with imperfect competition in the goods market and matching frictions in the labor market. The economy is populated by a continuum of risk neutral workers whose

³We run mincer regressions in cross section for each month, where wages are explained by a dummy for informal workers, a dummy for each city, and the following worker's characteristics: age, age square, education, education square, and position in the household.

 $^{^4}$ To be precise, within the 95% confidence interval, the decrease in wage premium ranged between 7% and 31 %

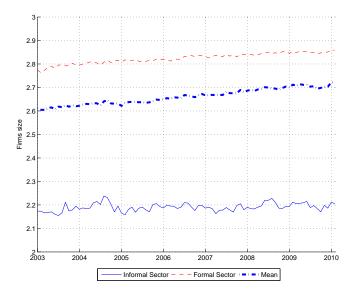


Figure 4: Firm size in formal and informal sectors

measure is normalized to unity. There are two sectors, formal (F) and informal (I), each producing one of the two consumption goods available in the economy.

3.1 The goods market

Households derive utility from consuming goods from both formal and informal sectors, and their preferences are represented by the following utility function:

$$U = \left[\alpha_F^{\frac{1}{\sigma}} C_F^{\frac{\sigma-1}{\sigma}} + \alpha_I^{\frac{1}{\sigma}} C_I^{\frac{\sigma-1}{\sigma}} \right]^{\frac{\sigma}{\sigma-1}}$$
 (1)

where C_F and C_I denote a household's consumption of the good produced in the formal and in the informal sectors, respectively, while σ stands for the elasticity of substitution between the two goods. Assuming, for the sake of simplicity, that $\alpha_F = \alpha_I \equiv \alpha$, the optimal consumption pattern of a household n with real income R_n is given by:

$$C_{jn} = \alpha R_n \left(\frac{p_j}{P}\right)^{-\sigma}, \text{ for } j \in \{F, I\}$$
 (2)

where p_j is the price of sector j good, P is the composite price index, $P = \left(\alpha \sum_{j=I,F} p_j^{1-\sigma}\right)^{1/(1-\sigma)}$, which we normalize to one without loss of generality. There is a continuum of identical consumers in the interval [0,1], hence aggregate consumption is:

$$C_j = \alpha R \left(\frac{p_j}{P}\right)^{-\sigma},\tag{3}$$

where $R \equiv \int_0^1 R_n dn$ denotes aggregate income.

Firms in each sector are identical. In a symmetric equilibrium, they all produce an equal share of the total demand for the sector, hence firms may be labeled only by the industry j they belong to. We then have that $C_j = N_j y_j$, where y_j denotes the production of a firm and N_j the number or firms in sector j. N_j is fixed in the short run, while in the long run it responds to changes in market profitability and is determined by a free entry condition.

In this way, as a result of Cournot competition among firms, the elasticity of demand faced by a firm in sector j, σ_j , is positively related to the number of firms operating in that sector as follows:

$$\sigma_j \equiv \sigma_j(N_j) = \sigma N_j. \tag{4}$$

Thus, in this simple framework, we have that the number of firms, N_j , determines the level of competition for a firm in sector j. A number of alternative ways to model imperfect competition in the goods market can be found in the literature, e.g. Blanchard and Giavazzi (2003), Delacroix (2006), Ebell and Haefke (2009), or Felbermayr and Prat (2010). Our main results would not change substantially when using alternative specifications.

Labor is the only input in production. Recent research on informality has highlighted the fact that informal firms are less productive than formal ones (see, for instance, Taymaz, 2009). In particular, in a careful empirical study on informality La Porta and Shleifer (2008) find that on average the productivity differential between small informal (unregistred) firms and small formal (registred) firms is in the range of 71 to 314%.

We allow for productivity differences across sectors by defining production function as:

$$y_j = A_j h_j \tag{5}$$

where A_j stands for a (sector-specific) productivity parameter and h_j is the firm's size, that is, the number of workers employed. The size of firms will be endogenously determined in the model. We will see that, in equilibrium, firms in the informal sector are smaller, which is in accordance with the stylized fact described in section 2 and previous findings in the literature (see Rauch, 1991 or Tybout, 2000).

3.2 The labor market

Empirical evidence indicates that informal workers have on average lower educational attainment levels (see, among others, Gong and Van Soest, 2002, Gong et al, 2004, and Maloney, 2004). Since informality would therefore be more a concern for low than for high skill workers, we choose to focus on identical workers ⁵ searching for a job in the formal and in the informal

⁵This is of course a simplification compared to the papers studying the sorting mechanism between the two sectors (e.g. Boeri and Garibaldi, 2006, Albrecht et al., 2009), but our focus is not on explaining sorting patterns

sector simultaneously when unemployed. This hypothesis is not necessarily too restrictive. La Porta and Shleifer (2008) present evidence that, while top managers in informal firms are indeed less educated, other employees have a comparable level of education in informal and in small formal firms.

Furthermore, we assume that both formal and informal sectors are subject to matching frictions in the labor market and that they share the same pool of unemployed workers. These two assumptions depart from other recent works that incorporate search-matching frictions to study informality, which assume a segmented labor market and takes the informal sector as a residual perfectly competitive sector.

In each sector, vacant jobs and unemployed workers are brought together in pairs by a matching function M_j . It maps the number of matches in sector j, M_j , to the total number of job seekers and vacancies in that sector:

$$M_j \equiv M_j(u, v_j) \tag{6}$$

where u and v_j correspond respectively to the mass of job seekers, which is the unemployment rate in the economy⁶, and to the mass of vacancies in the sector. The function M_j features standard properties: it is twice continuously differentiable, increasing and concave in both of its arguments, it is linearly homogeneous, satisfies the Inada conditions and the boundary conditions $M_j(0, v_j) = M_j(u, 0) = 0$ for $u, v_j \ge 0$.

We allow the matching function to be different across sectors to be able to capture their particularities. For instance, firms may rely on different methods to recruit their workers in the two sectors, so that the efficiency of the two matching processes may differ somewhat. It is also often argued that, compared to the formal sector, the informal sector is closer to a competitive market where it takes less time to match. In such a case, the matching process would be more efficient in the informal sector, resulting in more matches for the same level of inputs in the matching function. More specifically, in our numerical simulations we use a Cobb-Douglas function for the matching function, $M_j = \kappa_j u^{\eta} v_j^{1-\eta}$, with $\kappa_I \geq \kappa_F$ to capture the easier matching in the informal sector.

On average, a firm contacts a worker at rate M_j/v_j while a job seeker meets a sector j firm at rate M_j/u . Let $\theta_j \equiv v_j/u$ be the labor market tightness. Linear homogeneity of the matching function allows us to write those contact rates as $M_j/v_j \equiv m_j(\theta_j)$, with $m_j'(\theta_j) < 0$, and $M_j/u = \theta_j m_j(\theta_j)$, which is an increasing function of θ_j . Thus vacancies are filled at rate

across sectors.

⁶We assume job seekers are 'truly' unemployed. Alternatively, we could assume that they are in fact self-employed, and that the self-employed search for jobs.

 $m_j(\theta_j)$ in sector j while workers exit unemployment at rate $\sum_{j=F,I} \theta_j m_j(\theta_j)$.

A few remarks are in order. First, differences in job finding rates between the formal and the informal sector can easily be captured with two matching functions having different scale parameters. For instance, in the Cobb-Douglas case, $M_F = \kappa_F u^\eta v_F^{1-\eta}$ while $M_I = \kappa_I u^\eta v_I^{1-\eta}$, with $\kappa_I \geq \kappa_F$. Second, the assumption of search frictions in both sectors encompasses the particular case of perfect competition in the informal labor market considered in several papers. That would correspond to the limit case where $\kappa_I \to \infty$ in our framework, i.e. in a fully competitive labor market, where it takes no time to locate a job offer or to fill a vacancy. Finally, if it took no time to locate a formal job $(\theta_F m_F(\theta_F) \to \infty)$, all workers would be employed in the formal sector. Thus, matching frictions are an important reason for the existence of an informal sector, and the underlying assumption for the existence of the two sectors is that the formal sector is 'sufficiently' frictional.

Matches are dissolved at rate d_j , due either to an exogenous separation rate s_j between firms and workers or to the exit of firms from the market, which occurs with probability δ_j . Hence, the sector-specific destruction rate is:

$$d_j = \delta_j + s_j(1 - \delta_j) \tag{7}$$

Workers can be either employed or unemployed so that:

$$L_F + L_I = 1 - u \tag{8}$$

where $L_j = N_j h_j$ denotes employment in sector j, and u stands for unemployment. In steady-state equilibrium, the mass of unemployed workers that find a job in a sector has to equal the mass of workers that loose a job in that sector, that is:

$$d_i L_i = \theta_i m_i(\theta_i) u \tag{9}$$

Equation (9) states that when a fraction d_j of the jobs in sector j are destroyed, they are compensated by an inflow $\theta_j m(\theta_j) u$ of job seekers who are recruited in sector j.

3.3 Firms decisions

Following a growing body of the literature, we depart from the basic matching model by assuming firms can hire more than one worker. This implies that firm size becomes an endogenous variable which responds to changes in firm's expected profits. This feature of the model allows us to analyze the determinants of the relative size of firms in the two sectors. In particular, firm size depends on the elasticity of substitution σ_j , as we will show below, due to the assumption of imperfect competition in the goods market.

Firms choose the number of vacancies and its size so as to maximize expected profits, which can be written as:

$$V_{j}(h_{j}) = \max_{v_{j}, h'_{j}} \frac{1}{1+r} \left[p_{j} \left(y_{j} \left(h_{j} \right) \right) y_{j} \left(h_{j} \right) - w_{j} \left(h_{j} \right) h_{j} \left(1 + \tau_{j} \right) - \gamma_{j} v_{j} + \left(1 - \delta_{j} \right) V_{j} \left(h'_{j} \right) \right], \quad (10)$$

where r is the interest rate, γ_j is the cost of a vacancy, τ_j represent taxes on labor costs, and $w_j(h_j)$ is the wage function resulting from a bargaining process, which will be derived in the next section. h_j and h'_j represent the number of workers in current and next periods, respectively. The production function $y_j(h_j)$ is in equation (5) and the inverse demand function $p_j(y_j)$ is derived from demand in equation (3). Notice that, in this setting, firms do not take prices as given in the final goods market, as shown by the inverse demand function, and they enjoy some bargaining power in the labor market, which is captured by the wage function.

The number of workers next period, h'_{j} , is determined by the following transition function:

$$h'_{j} = m_{j}(\theta_{j})v_{j} + (1 - s_{j})h_{j},$$
 (11)

that is, next period's employment is equal to the number of matches for the vacancies posted plus the number of current workers that remain employed. Thus, firms advertise as many vacancies as necessary in order to hire, in expected value, the desired number of workers next period, taking into account the cost of a vacancy γ_j and the constraints on labor market flows given by the transition function (11).

The optimal number of vacancies posted is such that the marginal contribution of a worker to the firm's expected profit is equal to the expected search cost, that is:

$$(1 - \delta_j) \frac{\partial V_j(h_j')}{\partial h_j'} = \frac{\gamma_j}{m_j(\theta_j)}.$$
 (12)

From the profit function (10), the marginal contribution of a worker to the firm's profit, denoted the envelope condition, can be written as:

$$\frac{\partial V_j(h_j)}{\partial h_j} = \frac{1}{1+r} \begin{bmatrix} \frac{\sigma_j - 1}{\sigma_j} p_j A_j - \left(w_j(h_j) + \frac{\partial w_j(h_j)}{\partial h_j} h_j \right) (1+\tau_j) + \\ + (1-\delta_j) (1-s_j) \frac{\partial V_j(h'_j)}{\partial h'_j} \end{bmatrix},$$
(13)

where we have used the fact that $\frac{\partial p_j(y_j)}{\partial y_j} \frac{\partial y_j}{\partial h_j} y_j + p_j \frac{\partial y_j}{\partial h_j} = \frac{\sigma_j - 1}{\sigma_j} p_j A_j$ and that $\frac{\partial h'_j}{\partial h_j} = 1 - s_j$. The term $\frac{\sigma_j - 1}{\sigma_j} p_j A_j$ corresponds to marginal revenue to which the marginal costs $\left(w_j(h_j) + \frac{\partial w_j(h_j)}{\partial h_j} h_j \right) \times (1 + \tau_j)$ of expanding the labor force to h_j should be subtracted. Marginal costs differs from

⁷More precisely, price is a function of total production in the sector, which the sum of all firms production in the sector. With some abuse of notation, we express price as a function of one firm's production, implicitly taking the production of all other firms as given.

wage since firms take into account the effect of an additional worker on the wages of previously employed workers.

Substituting the envelope condition (13) into the optimal vacancies condition (12), we get that, in steady state:

$$p_j(h_j) = \frac{1}{A_j} \left(\frac{\sigma_j}{\sigma_j - 1} \right) \left[\left(w_j(h_j) + \frac{\partial w_j(h_j)}{\partial h_j} h_j \right) (1 + \tau_j) + \frac{\gamma_j(r + d_j)}{m_j(\theta_j)(1 - \delta_j)} \right]. \tag{14}$$

Equation (14) defines firms pricing behavior in steady state, and can be interpreted as a mark-up equation over total labor costs, inclusive of wages and search costs. Firms enjoy some market power on the goods market, but also on the labor market, due to the existence of search frictions. In the absence of frictions, price p_j would simply be equal to $\frac{1}{A_j} \left(\frac{\sigma_j}{\sigma_j - 1} \right) w_j$. Here, though, the marginal cost of labor also takes into account the existence of recruitment costs and the impact of an additional worker on the wages of the infra-marginal workers, $\frac{\partial w_j(h_j)}{\partial h_j} h_j$. The latter term is negative, as shown in next section. This means that employers exploit decreasing marginal returns in order to reduce the wages of each infra marginal worker. For this reason the term is usually denoted in the literature as the *overemployment* or *overhiring effect*. Alternatively, equation (14) can be interpreted as a labor demand equation which relates the firms optimal employment and wages choices.

3.4 Wage Bargaining

Let E_j and U denote respectively the asset values of a worker employed in sector j ($j \in \{F, I\}$) or searching for a job. An unemployed worker enjoys a flow utility z, which may correspond to e.g. a combination of home-production and/or flow utility from leisure enjoyed while unemployed. He has an utility gain of $(E_j - U)$ when he finds a job in sector j, which occurs with probability $\theta_j m$ (θ_j). Thus, in steady state we have that:

$$rU = z + \theta_F m(\theta_F) (E_F - U) + \theta_I m(\theta_I) (E_I - U)$$
(15)

A worker employed in sector j, on his turn, receives a wage w_j and incurs an utility loss of $U - E_j$ when the job is destroyed, which occurs at rate d_j . We then have that:

$$rE_j = w_j + d_j(U - E_j). (16)$$

Workers are not paid their full marginal product as in the standard neoclassical framework due to a combination of costly search and matching frictions which give rise to rent sharing. Most of the papers which study informality incorporating search frictions assume that wages result from Nash bargaining between one worker and one firm in the sector that experiences search frictions. We assume alternatively that bargaining takes place between a firm and its multiple workers, each worker being treated as the marginal worker. This is a good representation of reality when firms cannot commit to long-term contracts and may renegotiate wages with each worker at any time (Mortensen, 2009). This seems an adequate framework to represent a case like the Brazilian one, where job turnover is extremely high (see Gonzaga, 2003).

Furthermore, this interesting alternative assumption has not been implemented yet in the literature studying the composition of employment in terms of formal vs informal jobs. We follow a growing body of the literature that has applied this assumption in studies not related to informality⁸.

As it will become clear later, bargaining with multiple workers introduces some important differences compared to the standard one-worker-per-firm framework, as under the neoclassical framework where wages equal marginal product. In particular, this gives rise to an overhiring externality according to which firms hire workers above the point where the marginal revenue from hiring the marginal worker equals marginal cost, since by doing so the wage of all inframarginal workers is reduced.⁹

The bargain between firms and the marginal worker yields:

$$(1 - \beta_j) (E_j - U) = \frac{\beta_j}{1 + \tau_j} \frac{\partial V_j(h_j)}{\partial h_j}.$$
 (17)

where $\beta_j \in [0, 1]$ can be interpreted as workers bargaining power. Using equations (13), (16) and (17), after some algebra it is possible to show that the wage w_j is a solution to the following first-order linear differential equation: ¹⁰

$$w_j(h_j) = (1 - \beta_j)rU + \beta_j \left[\frac{A_j}{1 + \tau_j} \frac{\sigma_j - 1}{\sigma_j} p_j - \frac{\partial w_j(h_j)}{\partial h_j} h_j \right], \tag{18}$$

which has the following solution:

$$w_{j}(h_{j}) = (1 - \beta_{j})rU + \beta_{j} \frac{\sigma_{j} - 1}{\sigma_{j} - \beta_{j}} \frac{A_{j}p_{j}(h_{j})}{1 + \tau_{j}}.$$
(19)

Equation (19) can be interpreted as the wage curve, which defines the wage as a weighted average of workers reservation value rU and of firm's marginal revenue, captured by the term $\frac{\sigma_j-1}{\sigma_j-\beta_j}\frac{p_j(h_j)A_j}{1+\tau_j}$

⁸See, among others, Bertola and Caballero (1994), Stole and Zwiebel (1996), Smith (1999), Cahuc and Wasmer (2001), Delacroix (2006), Cahuc, Marque and Wasmer (2008), Ebell and Haefke (2009), and Felbermayr and Prat (2010).

⁹Our framework is fairly general. It is always possible to compare the situation where overhiring is ruled out to the case where it takes place. It is also possible to allow for overhiring in one sector only.

 $^{^{10}}$ See appendix for the derivation of equations (18) and (19).

The relation between wages and employment is clear when one evaluates $\frac{\partial w_j(h_j)}{\partial h_j}h_j$. Combining equations (18) and (19) we get:

$$\frac{\partial w_j(h_j)}{\partial h_j}h_j = - \qquad \underbrace{\frac{\sigma_j - 1}{\sigma_j - \beta_j}}_{\qquad \qquad \underbrace{\sigma_j - \beta_j}} \qquad \frac{\beta_j A_j p_j(h_j)}{\sigma_j (1 + \tau_j)} < 0.$$
 (20)

overhiring and market power effects

It is clear from equation (20) that wage depends on a term combining overhiring and market power effects. The equation also implies that the bargained wage is a decreasing function of employment. This is due to the fact that the firm's marginal revenue decreases with the number of workers, since the increased production from hiring an extra worker tends to reduce the price p_j . This effect is taken into account by the firms enjoying some market power. Given that each worker is treated as the marginal worker, hiring one more worker reduces the wage by $\left|\frac{\partial w_j(h_j)}{\partial h_j}\right|$. This leads to the so-called overhiring externality.

Notice that the overhiring effect differs across sectors, since they have different market and bargaining powers. From equation (20), the overhiring externality increases with workers bargaining power β_j and decreases with competition σ_j . It vanishes when $\beta_j \to 0$ or $\sigma_j \to \infty$. In such limit cases, workers are paid a constant wage: they get their reservation wage in the first case, while the marginal product of a worker is constant under full competition in the second. Such limit cases are more likely to apply to the informal sector, since workers bargaining power is smaller in the informal sector and competition is more intense than in the formal sector.

Combining equations (14) and (20), we get the equation that determines the optimal employment choice:

$$\left[w_j(h_j)(1+\tau_j) + \frac{\gamma_j(r+d_j)}{m_j(\theta_j)(1-\delta_j)}\right] \frac{\sigma_j - \beta_j}{\sigma_j} = A_j p_j(h_j) \frac{\sigma_j - 1}{\sigma_j}$$
(21)

According to equation (21), firms set employment, and therefore wages, so as to equalize marginal costs to marginal revenue. Marginal revenue, on the right hand side, includes a factor $\frac{\sigma_j-1}{\sigma_j} < 1$, due to their market power in the goods market. Marginal costs, on the left hand side of the equation, consist of wages, taxes on labor and expected search costs (i.e. the overall employment cost). It is weighted by an overhiring factor $\frac{\sigma_j-\beta_j}{\sigma_j} < 1$, which establishes that they set h_j above the efficient level where benefit from hiring the marginal worker equals his cost. Firms are willing to do so because they are aware that hiring more workers tends to depress wages paid for their entire workforce. In our two-sector setting, overhiring should be less important in the sector where workers bargaining power β_j is smaller or where the elasticity σ_j is larger. Typically, that should be the case in informal sectors where there is a larger number of firms and where workers have lower bargaining power (see Camargo, 2003).¹¹

 $^{^{11}}$ Notice that the intuition provided here takes workers outside options are fixed. Section 6 studies the impact of

4 Equilibrium

4.1 Equilibrium in the short-run

We are now ready to determine the short-run equilibrium where the number of firms in each sector is constant. Given our previous assumptions, having a fixed number of competitors N_j is equivalent to fixing the elasticity σ_j faced by each firm in industry j. Hence a short-run equilibrium is defined for a given value of N_j for each industry, while prices p_j , wages w_j , firm size h_j and sectoral employment $L_j = N_j h_j$, aggregate unemployment $u = 1 - \sum_{j=I,F} L_j$, tightness θ_j and workers reservation value are endogenously determined. In the simulations of the model we do comparative statics analysis to investigate the impact of some of the parameters. In particular, we highlight the impact of fiercer competition on all variables in the short run by investigating the impact of changes in the degree of competition $\sigma_j = \sigma N_j$, captured by a change in N_j .

In the short-run, the endogenous variables of our model are all functions of two main unknowns: labor market tightness in the two sectors (θ_F^*, θ_I^*) , determined by the equilibrium conditions in the goods and in the labor markets as follows. First, using demand and supply equations (3) and (5) we find the employment ratio between the two sectors that satisfy the goods market equilibrium. We denote it the product market equilibrium (PME) condition, given by:

$$\frac{L_I^*}{L_F^*} = \frac{A_F}{A_I} \left[\frac{p_I(\theta_F^*, \theta_I^*)}{p_F(\theta_F^*, \theta_I^*)} \right]^{-\sigma}, \tag{22}$$

which defines implicitly the intersectoral allocation of labor as a function of relative prices and relative productivity, an usual property.

Note that the ratio L_I^*/L_F^* is a function of tightness θ_F^* and θ_I^* due to the (positive) dependence of prices p_F and p_I on these variables (please, refer to the appendix for the derivation of the price equations). A rise in θ_j^* , would imply a rise in wages, translating into a higher price. The quantity consumed thus decreases, resulting in lower employment in the sector. However, as given by PME condition (22), the relative labor allocation L_I^*/L_F^* depends on relative (rather than absolute) prices. Since both prices depend positively on θ_F^* and θ_I^* , the impact of a change in these variables on relative prices is ambiguous. It depends on which price is more sensitive to changes in labor market tightness, which is captured by a condition on price elasticities.¹²

such a wage bargaining externality when workers outside options are endogenous. It is then shown that *overhiring* in the formal sector may translate into underhiring in the *informal* sector. In any case, there are reasons to think that the so-called overhiring externality implies a smaller relative size of the informal sector.

¹²Differentiating equation (22) we get that the ratio L_I^*/L_F^* decreases with θ_I^* if and only if $\varepsilon_{p_F/\theta_I} < \varepsilon_{p_{I/\theta_I}}$, where $\varepsilon_{p_i/\theta_j}$ denotes the elasticity of prices in sector i with respect to labor tightness in sector j. Similarly, the ratio L_I^*/L_F^* increases with θ_F^* if and only if $\varepsilon_{p_F/\theta_F} > \varepsilon_{p_{I/\theta_F}}$.

The comparative statics properties of this relationship is ambiguous as well, since it depends on which price is impacted the most by a change in parameters in equation (22).¹³

Second, from equation (9) we derive the relative employment in the two sectors that is compatible with equilibrium in the labor market. We get then the labor market equilibrium (LME) condition:

$$\frac{L_I^*}{L_F^*} = \frac{d_F}{d_I} \frac{\theta_I^* m_I(\theta_I^*)}{\theta_F^* m_F(\theta_F^*)}.$$
 (23)

which defines the intersectoral allocation of labor as a function of sectoral tightness, efficiency parameter of the matching processes and turnover rates. Hence, the LME condition imply that the informal sector is relatively larger when its own labor market tightness θ_I^* is higher and when the formal sector's tightness θ_F^* is lower. Moreover, the formal sector is larger also when its own destruction rate of jobs is lower and the informal sector's one is higher.

The intersectoral allocation of labor in equilibrium is determined when PME and LME relationships are satisfied simultaneously. Hence, by equalizing equations (22) and (23) we determine the Intersectoral Allocation of Labor curve (IALC):¹⁴

$$\frac{d_F}{d_I} \frac{\theta_I^* m_I(\theta_I^*)}{\theta_F^* m_F(\theta_F^*)} = \frac{A_F}{A_I} \left[\frac{p_I(\theta_F^*, \theta_I^*)}{p_F(\theta_F^*, \theta_I^*)} \right]^{-\sigma}, \tag{IALC}$$

which determines a first relationship between θ_F^* and θ_I^* .

A second relationship between the two sectoral tightness is obtained using the aggregate price index and normalizing it to one:

$$P^* = 1 = \alpha^{\frac{1}{1-\sigma}} \left[p_I(\theta_I^*, \theta_F^*)^{1-\sigma} + p_F(\theta_I^*, \theta_F^*)^{1-\sigma} \right]^{\frac{1}{1-\sigma}}.$$

We get the Price Curve (PC):

$$1 - \alpha p_I(\theta_I^*, \theta_F^*)^{1-\sigma} = \alpha p_F(\theta_I^*, \theta_F^*)^{1-\sigma},$$
 (PC)

which defines a decreasing relationship between θ_I^* and θ_F^* .

The IALC and PC relationships together determine the equilibrium levels of labor market tightness in the two sectors, θ_F^* and θ_I^* , by means of a fixed point argument.

The equilibrium is unique provided the IALC relationship evolves monotonically with respect to θ_I^* and θ_F^* , as represented in Figure 5. The numerical simulation in the next section checks this monotonicity, and Figure 13 depicts the corresponding equilibrium.

¹³We therefore study the comparative statics on the basis of numerical exercises, and we get monotonic responses of $\frac{L_{r_0}^*}{L_{r_0}^*}$ to changes in the parameters considered. See sections 5 and 6.

¹⁴As mentioned above, the relationship is not necessarily monotonic, given that PME is not necessarily monotonic. IALC is monotonically increasing under the same conditions on price elasticities $\varepsilon_{p_F/\theta_I} < \varepsilon_{p_{I}/\theta_I}$, and $\varepsilon_{p_F/\theta_F} > \varepsilon_{p_{I}/\theta_F}$ guaranteeing that the PME locus is increasing in θ_F and decreasing in θ_I . We check in our simulations that those conditions are satisfied.

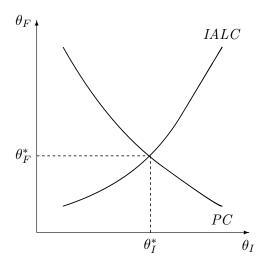


Figure 5: Unique Equilibrium

Once having determined equilibrium values for labor market tightness θ_I^* and θ_F^* , all the other variables of the model follow. Formal and informal sectors are interdependent for basically two reasons: (i) in equilibrium, demand for goods and therefore sectors relative size depend on relative prices, as it is clear from equation (22); (ii) workers search for jobs in both sectors, as established by equation (15). As a result, a change in sector-specific parameters affects both sectors, as will be shown in the next section through numerical exercises.¹⁵

4.2 Long-run general equilibrium

The next step is to determine the long run equilibrium in which the number of firms in each industry is endogenous. The timing of events is the following. At the beginning of a period firms decide whether to enter the market. If they enter they pay an entry cost, c_j , on top of the cost of posting vacancies in a number sufficient to recruit the desired amount of workers. ¹⁶ Business is then started and profits are received at the end of that period/beginning of the next period.

Entry costs entail direct administrative costs as well as indirect costs due to administrative delays. Several of the entry costs do not apply to the informal sector, such as, for instance, the official registration to comply with legislation. Although it would be fair to say that barriers to entry are essentially a problem in the formal sector, informal firms may still incur in entry

¹⁵The case with identical sectors is studied in the appendix. In that case, the IALC curve becomes the 45° line, and only the PC curve with $\theta_I = \theta_F$ shifts as parameters change.

¹⁶Notice that, in our setup, firms jump to their steady state size when they enter the market. This is a consequence of our assumption of linearity of adjustment costs. See Bertola and Caballero (1994) for a model with convex costs. See also Acemoglu and Hawkins (2010) for an alternative framework where firms cannot hire a large number of workers in each period.

costs since it may take some time and resources to set up a business in this sector. It is then reasonable to assume that $0 \le c_I < c_F$.

In equilibrium, the free entry condition establishes that the costs of setting a business must equal its profits, as in:

$$c_j + \frac{\gamma_j h_j^*}{m_j(\theta_j^*)} = \frac{1+r}{r+\delta_j} \pi_j^*, \text{ for } j \in \{I, F\},$$
 (24)

where the second term in the left-hand side corresponds to the cost of posting vacancies to hire the desired amount of labor h_i^* , and π_i^* stands for profits, which is given by:

$$\pi_j^* = p_j^* A_j h_j^* - w_j^* h_j^* (1 + \tau_j) - \gamma_j v_j^*$$

$$= p_j^* A_j h_j^* - w_j^* h_j^* (1 + \tau_j) - \gamma_j s_j h_j^* / m_j(\theta_j^*).$$
(25)

In the previous section we have derived all short run variables as functions of labor market tightness θ_I^* and θ_F^* , which are themselves parametrized by the number of firms operating in each sector, N_I and N_F . Hence, in a long run equilibrium, all variables are defined as functions of N_I and N_F and equation (24) closes the model.

Firms profit opportunities decline with the number of firms operating in the market N_j^* since with more firms there is more competition and lower markups. Under free entry, a rise in the left hand side of the free entry condition (24), for instance, due to an increase in entry costs c_j or in hiring costs $\frac{\gamma_j h_j^*}{m_j(\theta_j^*)}$ must be compensated by an equal rise of the right hand side of (24), i.e. higher profits, which is obtained by a smaller equilibrium number of firms.

5 Quantitative analysis

5.1 An application to Brazil

We choose parameters with two criteria in mind: (i) they have to be realistic and coherent with the values usually used in the literature, (ii) the values of endogenous variables stemming from the simulations have to be realistic and/or comparable with the values found in previous studies. We choose the Brazilian economy to guide our parametrization. Brazil is a large developing country with a sizable informal sector, with the advantage of having high quality micro data available, which has already been exploited in a number of empirical studies. Hence, we have both access to data and to other studies that have worked on them.

Our reference period is a month and we use 2003 as reference year. The discount rate r is set to 0.6434% which correspond to an annual rate of 8% as in Heckman and Pagés (2003). All relevant variables and parameters are allowed to differ between the formal and the informal sectors. Informal sector firms are assumed to be less productive than formal ones, and their

productivity is normalized to one. The productivity differential between the formal and the informal sector is large and consistent with the range of the estimates provided by La Porta and Shleifer (2008). The productivity parameter in the formal sector is 2, capturing a productivity differential of 100%, as used by other studies (see, for instance, Ulyssea, 2009). In terms of our notation, we have then that $A_F = 2$ and $A_I = 1$.

In a recent study, Bartelsman, Haltiwanger, and Scarpetta (2009) estimate that the annual exit rate for Brazilian firm ranges between 5% to 10%, and they indicate that exit rate is higher among smaller firms. Since firms are on average smaller in the informal sector than in the formal one, we use the lower bound of the interval to define firms' exit rate in the formal sector and, conversely, the upper bound to define firms' exit rate in the informal sector. It follows that the monthly values for the two parameters are set to $\delta_F = 0.0041$ and $\delta_I = 0.0080$ which is consistent with the intuition that on average firms' turnover is higher in the informal sector, i.e. $\delta_F < \delta_I$. Labor turnover is higher in the informal sector $d_F < d_I$. We choose the parameters to be equal to $d_F = 0.0221$ and $d_I = 0.0102$ which correspond to an annual rate of 13% and 30% as in Heckman and Pagés (2003) and Ulyssea (2009). Finally, making use of equation (7), the exogenous separation rates are set to $s_F = 0.0062$ and $s_I = 0.0142$ respectively.

Matching functions are of the Cobb-Douglas form, i.e. $M_F = \kappa_F u^\eta v_F^{1-\eta}$ and $M_I = \kappa_I u^\eta v_I^{1-\eta}$. The elasticity of the matching function is set to one half, as usual in the literature (Petrongolo and Pissarides, 2001, Shimer, Rogerson and Wright, 2005) while the scale parameter of the matching function is set to target an unemployment rate of approximatively 12.5% as in the data (See section 2). According to Camargo (2005) the bargaining power in the informal sector is approximately 1/3 of that in the formal sector. Those parameters can then be set to $\beta_F = 0.45$ and $\beta_I = 0.15$, as in Ulyssea (2009). By definition, the labor tax rate is nil in the informal sector and we set the formal tax rate equal to 30% which is consistent with the value reported in the World Doing Business Indicators for social security contributions and payroll taxes.

Keeping in mind that firms in informal sectors face lower (if any) entry and flow costs $(c_F > c_I \text{ and } \gamma_F > \gamma_I)$, we set the remaining free parameters so as: (i) to replicate the size of the informal sector; (ii) to get a reasonable wage premium $(w_F > w_I)$; (iii) to have a faster (more efficient) matching process in the informal sector $(M_F < M_I)$; (iv) to have more firms in the informal sector $(N_F < N_I)$ but with a lower size $(h_F > h_I)$. Baseline parameters are reported in Table 2.

Table 2: Baseline Parameters						
Parameter	Sector		Informal/Formal	Description		
	Informal	Formal				
A_j	1	2	0.50	Productivity		
δ_j	0.80%	0.41%	1.95	Firms exit rate		
d_{j}	2.21%	1.02%	2.16	Matches dissolution rate		
γ_j	0.45	1.10	0.41	Cost of a vacancy		
κ_j	0.0500	0.0475	1.05	Matching function parameter		
eta_j	0.15	0.45	0.33	Workers bargaining power		
$ au_j$	0	30%	-	Tax on labor costs		
c_{j}	0.50	2.25	0.22	Entry cost		
		G	eneral parameters			
\overline{r}		0.65% Discount rate		Discount rate		
σ		2.05 Elasticity of substituti		Elasticity of substitution		
α		0.5		Utility function parameter		
z		0.	05	Workers reservation value		

5.2 Results

The benchmark results of our numerical exercise are summarized in Table 3.¹⁷ They match our targets in terms of aggregate variables, with an unemployment rate around 12% and an informal sector representing 40% of total employment. Wages are approximately 18% higher in the formal sector compared to the informal one, which is roughly consistent with the lower bound of estimated wage differentials between the two sectors, as presented in Figure 3, section 2. Almost similar patterns can be found in Bargain and Kwenda (2009) and Tannuri-Pianto and Pianto (2002) for quantile regressions.

The job finding rate is two times larger in the informal than in the formal sector. Although this difference is somewhat larger than the one found in Table 1 of section 2, it is consistent with the viewpoint taken in most existing studies where finding a job in the informal sector is easier than in the formal one (see, e.g. Zenou, 2008, Ulyssea, 2009).

Also consistent with the evidence, there are fewer and larger firms in the formal than in the informal sector as argued by Rauch (1991) and discussed in Tybout (2000) and La Porta and Shleifer (2008). More precisely, we find formal firms to be approximately two times larger than informal ones. Correspondingly, informal firms are approximatively two times more numerous in the informal sector. The resulting price elasticity of demand is around 6 in the formal sector

¹⁷Figure 13 in Appendix presents a representation of the equilibrium. It certifies that the key IALC condition is monotonic in equation (23).

Table 3: Main endogenous variables

Variable	Sector		Sector		Informal/Formal	Description
	Formal	Informal				
$\overline{w_j}$	0.91	0.77	0.85	Wage		
$ heta_j$	0.69	2.18	3.16	Labor market tightness		
n_{j}	3.12	5.55	1.78	Number of firms		
h_{j}	0.15	0.07	0.47	Firm size		
σ_{j}	6.40	11.37	1.78	Elasticity of demand for a firm		
π_j	0.05	0.02	0.04	Profits		
u		12.	17	Unemployment rate		
L_I	40.6		67	Informality rate		

compared to about 11 in the informal one. As a consequence, profits are higher in the formal sector. Having different values for the elasticity is a desirable feature of our model. It implies that the various externalities stemming from market and bargaining powers are of different magnitude across sectors.

5.3 Short run analysis

Competition in the formal sector The number of firms in each sector is fixed in the shortrun. We first examine the impact of a change in the number of firms in the formal sector on the main variables of the model. With this exercise we are able to understand the effect of an exogenous shock on relative competitiveness between the formal and informal sectors. It could represent, in a crude way, the impact of opening to international trade, when domestic producers face international competition and thereby suffer a decrease in its monopoly power.

Figure 6 about here

Figures 6 and 7 depict how the economy reacts to an exogenous variation of the number of firms in the formal sector compared to the baseline case. The effect of an increase in the number of formal firms is unambiguously (i) a fall in unemployment, though this effect is of moderate magnitude, (ii) a marked rise in the relative size of the formal sector in total employment, though (iii) the relative size of each firm in the formal sector tends to decrease. Finally, it can be seen that (iv) each formal firm pays a relatively higher wage compared to the informal sector when competition in the formal sector becomes fiercer.

Figure 7 about here

These results can be understood by looking at labor market tightness and prices. We see

that a rise in competition in the formal sector affects tightness in opposite ways across sectors: tightness increases in the formal sector (θ_F) , while it decreases in the informal one (θ_I) . Therefore, this suggests that this is mainly a result of an upward move of the IALC curve in Figure 5, assuming that the IALC relationship is monotonically increasing. This results in a rise in p_I and a fall in p_F , so that the relative price p_I/p_F goes up. The increase in informal sector relative price explains the fall in relative employment in that sector observed in Figure 6, since $L_I/L_F = (A_F/A_I) (p_I/p_F)^{-\sigma}$, from the PME condition (22). In addition, we see from Figure 7 that this change in relative employment corresponds to a rise in formal sector employment L_F and a fall in informal sector employment L_I .

The decrease in the relative size of formal sector firms corresponds to a fall in firm size in both sectors, as shown in Figure 7. Employment in sector j is equal to $L_j = N_j \times h_j$. In this exercise, the number of firms is fixed in the informal sector. Hence, the fall in sectoral employment L_I translates into a decrease in firm size h_I . For the formal sector, total employment L_F rises, but so does the number of firms N_F . The fact that firm size decreases in that sector means that the former effect is more than offset by the latter.

Figure 7 also shows that the change in relative wages corresponds to a rise in wages in both sectors. This is the result of two opposite effects, since θ_F goes up while θ_I goes down. We can therefore conclude that the rise in θ_F induces a rise in both wages, which dominates the negative effect of the fall in θ_I .

Overall, if the formal sector were more similar to the informal one in terms of the degree of competition, then aggregate employment would be slightly higher while the informal sector would represent a significantly lower share of total employment. Wages would increase in both sectors, with a relatively larger increase in the informal sector. Firms profits, however, would be negatively impacted.

5.4 Long run analysis

Entry costs We now study the long-run impact of a change in entry costs in the formal sector c_F on unemployment u, the share of informal employment L_I/L_F , relative firms size h_I/h_F , and relative wages w_I/w_F .

A decrease in formal sector entry costs would increase the number of formal sector firms in the long-run. Hence, the long-run impacts of decreasing entry costs are very similar qualitatively to the impact of increasing the number of firms in the formal sector studied in the previous subsection. In particular, almost similar patterns for θ_j and p_j can be found in the long and in the short run.

Figure 8 about here

The quantitative effects are, however, not exactly the same. A decrease in the entry costs not only increases the number of firms operating in the formal sector, but also decreases the number of informal firms, though this latter effect is of smaller magnitude. As a result, price elasticities increase for formal sector firms and slightly decrease in the informal sector. This implies that even if the effects do not differ qualitatively between figures 6 and 8, they should be somewhat different in quantitative terms since price elasticities are slightly different. In particular, higher price elasticities in the formal sector also imply smaller profits. The impact is then larger on the formal sector than on the informal one, as can be seen from Figure 9 that shows that relative price elasticity $\sigma_I/\sigma_F = N_I/N_F$ is positively related to entry costs.

Figure 9 about here

There are some noteworthy effects on the labor market. Formal employment increases with lower entry costs in the formal sector, while informal employment and unemployment decrease. From these results, we can conclude that the drop in informality is not sufficient to compensate the rise in formal employment, resulting in lower unemployment.¹⁸ Finally, changes in sectoral employment following a drop in c_F decrease firms size in both sectors and is more pronounced in the formal sector. As in the short-run, reductions in firms' size are driven by the increase in the number of operating formal firms and by the collapse in informal employment respectively.

Overall, it turns out that a decrease in c_F , due to e.g. a waning in the product market regulation, would lead to lower unemployment and a smaller share of informal jobs in total employment. Wages would then be higher in both sectors, with a smaller wage ratio w_I/w_F . As we have seen in section 2, the Brazilian economy has experienced a simultaneous reduction in informality and in unemployment over the past the case. These movements, however, were accompanied by an **increase** in informal sector relative wages. Hence, a decrease in formal sector entry costs cannot fully account for the pattern of changes of Brazilian variables.

Bargaining power We now study the long-run impact of a change in workers bargaining power in the formal sector β_F on unemployment u, share of informal employment L_I/L_F , relative firms size h_I/h_F , and relative wages w_I/w_F . Note that the bargaining power variable should not be taken literally here. Rather, this variable should be thought as broad institutions that impede the functioning of the labor market and allow workers to extract rents.¹⁹ Figures 10 and

¹⁸Notice that while this is true in our numerical exercise, it is not necessarily the case for alternative numerical configurations.

¹⁹Similar interpretations are made in e.g. Blanchard and Giavazzi (2003) or Ebell and Haefke (2009).

12 display how the economy reacts to a (quite large) exogenous change of workers bargaining power in the formal sector, which ranges from 0.35 to 0.55. The long-run impact of changing workers bargaining power is a combination of its direct impact and of its impact on the number of firms in each sector in the long-run equilibrium, N_I and N_F . Lower workers bargaining power increases profits, which, in turn, should lead to a higher number of firms. The effect is larger in the formal sector, as can be seen from Figure 12, where the relative elasticity $\sigma_I/\sigma_F = N_I/N_F$ decreases with a lower β_F .

The effect of a decrease in formal workers bargaining power is unambiguously (i) a decrease in unemployment, (ii) a decrease in informal employment relative to formal employment and (iii) a rise in the relative size of informal firms compared to formal firms, and (iv) an increase in relative wages w_I/w_F .

Figure 10 about here

These results can be understood with the analysis of the impact of β_F on tightness and prices as depicted on Figure 11. A decrease in bargaining power β_F results in a rise in tightness for both sectors, θ_I and θ_F . This suggests an upward shift of the PC curve in Figure 5. This leads to a rise in the price in the informal sector p_I . The price p_F , however, decreases despite higher tightness, as a result of the decrease in labor costs due to lower bargaining power of the sector's workers.

Figure 11 about here

In turn, the relative price p_I/p_F goes up, which explains the decrease in $L_I/L_F = (A_F/A_I) (p_I/p_F)^{-\sigma}$ in Figure 10. Wages decrease in both sectors, in spite of the increase in tightness: the fall in bargaining power more than compensates the rise in tightness. Note however that this effect is of second order in the informal sector since β_F only affects the informal wage through workers reservation utility. It follows that wages decrease by a larger amount in the formal sector, so that relative wages w_I/w_F increase.

Note that, as shown in Figure 10, formal sector employment increases when their workers have lower bargaining power. In the informal sector, on the contrary, employment drops with smaller β_F . Unemployment, on its turn, always decreases with lower β_F , meaning that the rise in formal employment is larger than the fall in informal employment. Hence, it appears that the impact of changes in formal employment on unemployment is cushioned by the informal sector. With respect to the number of operating firms, it increases in the formal sector and slightly decreases in the informal sector. This translates in changes in firms size in each sector

as follows. In the formal sector, firms size h_F decreases as a result of the increase in formal employment L_F and in the number of operating firms, N_F , the effect being of a relatively large magnitude. On the contrary, firms size reacts less in the informal sector due to the fact that the number of operating firms in that sector is faintly affected by changes in the bargaining power. As a result firms relative size decreases.

Figure 12 about here

Overall, it turns out that if the formal sector were more similar to the informal one in terms of bargaining power (lower β_F , due to a cutback in labor market regulation, for instance), then unemployment would be lower, and the informal sector would represent a lower share of total employment. Moreover, the wage ratio w_I/w_F would increase. This set of effects is compatible with the stylized facts observed for the Brazilian economy since 2002: unemployment and informality decreased, while informal sector relative wage increased.

6 Discussion

In this section we discuss the role of each of the three externalities at play in our model: wage bargaining, matching frictions, and monopoly power in the product market. In this purpose, we analyze the impact of changes in workers bargaining power β_F and in entry costs c_F under alternative scenarios with respect to the externalities intensities. More precisely, we perform three exercises. In the first exercise, we rule out the wage bargaining externality by imposing $\frac{\sigma_j - \beta_j}{\sigma_j} = 1$ in both sectors. In a second exercise, we consider a less frictional labor market by decreasing in 10% the scale parameter of the matching function κ_j , also in both sectors. Finally, we consider a more competitive goods market by increasing σ in 10%. Tables 4 and 5 present the percentage changes with respect to the benchmark case for each scenario, and for alternative values of bargaining power and entry costs. Since $\beta_F = 0.45$ and $c_F = 2.25$ correspond to the baseline simulation, the percentage changes in those two columns are equal across tables. With these exercises, we seek to shed some light of the relative impact of each externality of our model. In addition, they are also useful to evaluate the robustness of some of our results.

The role of wage bargaining. We first compare the results obtained in the benchmark case to those obtained when the overhiring externality is ruled out in the two sectors. First, as shown in the first line of tables 4 and 5, it turns out that unemployment would be higher in the absence of the wage bargaining ('overhiring') externality, compared to the benchmark case with overhiring, as expected. Ruling out the wage bargaining externality would cause an increase in

Table 4: Changes in bargaining power under lesser imperfections

Bargaining power:		$\beta_F = 0.35$	$\beta_F = 0.40$	$\beta_F = 0.45$	$\beta_F = 0.50$	$\beta_F = 0.55$	
		Percentage change with respect to benchmark					
No overhiring	u	0.82	0.84	0.84	0.81	0.75	
$\frac{\sigma_j - \beta_j}{\sigma_j} = 1$	L_I/L_F	1.91	2.41	2.96	3.57	4.24	
	w_I/w_F	0.15	0.17	0.19	0.20	0.20	
Lesser matching	u	-10.49	-10.37	-10.25	-10.12	-9.99	
friction	L_I/L_F	-0.14	-0.29	-0.46	-0.65	-0.86	
$\kappa \searrow 10\%$	w_I/w_F	1.11	1.38	1.63	1.89	2.16	
Lesser monopoly	u	-2.19	-2.14	-2.10	-2.06	-2.02	
power	L_I/L_F	-0.15	-0.11	-0.06	-0.01	0.06	
$\sigma \nearrow 10\%$	w_I/w_F	0.17	0.22	0.28	0.33	0.38	

Table 5: Changes in entry costs under lesser imperfections

Entry cost:		$c_F = 1.75$	$c_F = 2.0$	$c_F = 2.25$	$c_F = 2.5$	$c_F = 2.75$
		Perce	ntage chang	ge with respe	ect to bench	nmark
No overhiring	u	0.76	0.80	0.84	0.87	0.91
$\frac{\sigma_j - \beta_j}{\sigma_j} = 1$	L_I/L_F	2.52	2.75	2.96	3.17	3.37
	w_I/w_F	0.15	0.17	0.19	0.21	0.23
Lesser matching	u	-10.24	-10.24	-10.25	-10.26	-10.26
friction	L_I/L_F	-0.49	-0.48	-0.46	-0.44	-0.43
$\kappa \searrow 10\%$	w_I/w_F	1.64	1.64	1.63	1.63	1.63
Lesser monopoly	u	-2.07	-2.09	-2.10	-2.11	-2.12
power	L_I/L_F	0.10	0.01	-0.06	-0.12	-0.17
<i>σ</i> ≯ 10%	w_I/w_F	0.29	0.28	0.28	0.27	0.26

unemployment of the order of 0.8%, which is quite modest. Nevertheless, that externality has a relatively stronger impact on the relative size of the informal sector. More accurately, L_I/L_F is 1.9 to 4.2% larger when overhiring is ruled out for different values of workers bargaining power, and 2.5 to 3.3% larger for different values of entry costs, as presented in the second line of Tables 4 and 5, respectively. Furthermore, the increase in informality is larger for higher values of β_F and c_F . Since L_I/L_F increases in those two variables, it means that changes in bargaining power and in entry costs have a stronger impact on the relative size of the informal sector when there is no overhiring. These results can be understood by comparing tightnesses and prices with and without overhiring in Tables 6 and 7 below:

The wage bargaining externality increases tightness in the formal sector and lowers it in the

Table 6: Changes in β_F without overhiring

Percentage changes compared to the benchmark case							
	$\beta_F = 0.35$ $\beta_F = 0.40$ $\beta_F = 0.45$ $\beta_F = 0.50$ $\beta_F = 0.55$						
p_I	-0.56	-0.71	-0.86	-1.02	-1.20		
p_F	0.36	0.46	0.57	0.69	0.83		
$ heta_I$	0.24	0.69	1.22	1.84	2.55		
$ heta_F$	-3.48	-3.99	-4.52	-5.06	-5.62		

Table 7: Changes in c_F without overhiring

Pe	Percentage changes compared to the benchmark case							
	$c_F = 1.75$	$c_F = 2.0$	$c_F = 2.25$	$c_F = 2.5$	$c_F = 2.75$			
p_I	-0.73	-0.80	-0.86	-0.91	-0.97			
p_F	0.48	0.52	0.57	0.61	0.64			
$ heta_I$	0.95	1.09	1.22	1.35	1.46			
θ_F	-3.94	-4.24	-4.52	-4.79	-5.05			

informal one²⁰. While the wage bargaining externality studied in sub-section 3.4 takes place in both sectors, it leads to *overhiring* in the formal sector, but to *underhiring* in the informal one, as a result of the interplay between the two sectors. Notice that this result contrasts with what would prevail if the two sectors where perfectly identical (studied in the appendix). In such a case, it is possible to show that the presence of the wage bargaining externality would make tightness larger in the two sectors, and would therefore lead to overhiring everywhere. Those results are similar to those highlighted in Cahuc, Marque and Wasmer (2008) in a model with large firms and an aggregate production function. Our results, however, are driven by sectoral heterogeneity and simultaneous (undirected) search in the two sectors rather than by interactions in the aggregate production function.

In terms of Figure 5, the comparison of θ_I and θ_F with and without overhiring suggests that the IALC curve with overhiring is above the one without overhiring. As a result, the price p_I is larger with overhiring while the converse is true for p_F , so that the price ratio p_I/p_F is higher, leading to a smaller relative size of the informal sector²¹, as $\frac{L_I}{L_F} = \left(\frac{p_I}{p_F}\right)^{-\sigma}$. Finally, informal firms pay lower relative wages with overhiring compared to without, but the difference between the two cases is quite small. Overall, the wage differential response to an increase in workers' bargaining power β_F or to an increase in entry costs c_F are not substantially affected by the

²⁰For instance, in the benchmark economy, tightnesses are equal to $\theta_I = 2.18$ and $\theta_F = 0.69$ with the overhiring externality and to $\theta_I = 2.21$ and $\theta_F = 0.66$ without.

²¹For instance, in the benchmark economy, prices are equal to $p_I = 1.2549$ and $p_F = 0.8326$ with the overhiring externality and to $p_I = 1.2441$ and $p_F = 0.8373$ without. This yields a relative price that is worth 1.5072 in the former case and 1.4858 in the latter.

presence or absence of the wage bargaining externality, as can be seen in the third line of tables 4 and 5.

In summary, the so-called overhiring externality leads to higher aggregate employment and a lower proportion of informal jobs in total employment.

The role of matching frictions. We now compare the results obtained in the benchmark case to those obtained when the formal and informal labour markets experience a 10% improvement in the efficiency parameter of their matching processes κ_i . The results are reported in the fourth to sixth lines in Tables 4 and 5. First, we have that unemployment is lower by approximately 10% in both tables, when labor markets become less frictional. Second, the relative size of the informal sector L_I/L_F is reduced, as expected. Namely, matching frictions provide a rationale to the existence of the informal sector: if it took no time to locate a job offer in the formal sector, there would not be an informal sector. Therefore, the underlying assumption for the existence of the two sectors is that they are sufficiently frictional. It is also interesting to note that the decrease in the informality rate is stronger as bargaining power increases (fourth line of Table 4), while it is weaker for higher values of entry costs (fourth line of Table 5). It means that lessening matching frictions makes relative size of informality less responsive to bargaining power changes, and more responsive to entry costs changes. Third, relative wages w_I/w_F become larger when matching frictions are reduced. The increase in relative wages is virtually the same for all values of entry costs, at 1.6% (fifth line of Table 5), whereas it is stronger for higher values of bargaining power, from 1.1 to 2.2 % (fifth line of Table 4). Since relative wages are a decreasing function of bargaining power, as shown in Figure 9, we have that relative wages become more responsive to bargaining power changes under lesser matching frictions.

In a nutshell, when there are lower matching frictions, unemployment and informality are reduced, while relative wages are increased. Furthermore, both relative size of sectors and relative wages become less responsive to wage bargaining changes.

The role of market power. In the last exercise, we increase the elasticity of substitution between formal and informal goods σ by 10% to analyze the role of market power in our model; The results are presented in the last three lines of Tables 4 and 5. First, it turns out that lowering market power by 10% would decrease unemployment by a little more than 2%. It is interesting to note that the unemployment reduction increases with bargaining power and decreases with entry costs. Since unemployment increases with these two variables, as shown in figures 7 and 9, this means that a lessening of market power renders unemployment less responsive to bargaining

power and more to entry costs.

Second, the impact of a reduction in market power on the relative size of the informal sector is ambiguous, but the effect is quite small. When bargaining power is high or when entry costs are low, lessening market power increases informality. The opposite is true for low bargaining power or high entry costs. Given the positive relation between those variables and informality relative size, we have that this variable responds more to bargaining power and less to entry costs changes when firms have less market power. The impact of market power on informality relative size is quantitatively small, though, of the order of $\pm 0.1\%$.

Finally, lower market power means lower relative wages in the informal sector. The impact is stronger for higher values of entry costs, while it is virtually the same for all bargaining power values considered. Thus, relative wages respond more to entry costs changes in a more competitive environment.

7 Conclusion

Using a matching model with large firms similar in spirit to Delacroix (2006) and Ebell and Haefke (2009), we have studied the impact of product and labor market regulations on equilibrium unemployment, the size of formal and informal sectors and wages. Our model endogenously generates a less competitive formal sector, which is a common assumption taken by previous literature. In this setting, we have shown that a fall in PMR strictness (captured by a fall in entry costs in the formal sector) reduces the size of the informal sector and unemployment while it raises wages. Conversely, a fall in LMR (captured by a fall in workers bargaining power in the formal sector) reduces both unemployment and informality while it reduces wages. For policy purposes, this means that it is possible to reduce informality without diminishing wages by reducing PMR instead of LMR strictness, or by reducing both simultaneously. Notice that, in this case, although wages would increase, wage inequality would increase with the rise in the formal sector wage premium. Finally, we consider the effects of wage bargaining in both sectors, which leads to 'overhiring' in the formal sector. This translates into a smaller relative size of the informal sector.

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8 Technical Appendix

8.1 Firm decision: optimal firm size

Step (i): determination of $\frac{\partial V_j(h_j)}{\partial h_j}$. From the envelop condition (13) we have

$$\frac{\partial V_j(h_j)}{\partial h_j} = \frac{1}{1+r} \left[\frac{\sigma_j - 1}{\sigma_j} p_j A_j - \left(w_j(h_j) + \frac{\partial w_j(h_j)}{\partial h_j} h_j \right) (1+\tau_j) + (1-\delta_j) (1-s_j) \frac{\partial V_j(h_j')}{\partial h_j'} \right], \tag{26}$$

In steady state firms' size is constant, so that $h_j = h'_j$. Hence, the first order condition (12) implies:

$$\frac{\partial V_j(h_j)}{\partial h_j} = \frac{\partial V_j(h'_j)}{\partial h'_j} = \frac{\gamma_j}{m_j(\theta_j)(1 - \delta_j)}$$
(27)

Using the steady-state condition $\frac{\partial V_j(h_j)}{\partial h_j} = \frac{\partial V_j(h_j')}{\partial h_j'} = \frac{\gamma_j}{m_j(\theta_j)(1-\delta_j)}$, and the envelope condition (??) we get:

$$\frac{\partial V_j(h_j)}{\partial h_j} = \frac{1}{r+d_j} \left[A_j \frac{\sigma_j - 1}{\sigma_j} p_j - \left(w_j(h_j) + \frac{\partial w_j(h_j)}{\partial h_j} h_j \right) (1+\tau_j) \right]$$
(28)

which will be useful for the derivation of the wage function.

Finally, substituting (27) into (28), we get:

$$p_j(h_j) = \frac{1}{A_j} \frac{\sigma_j}{\sigma_j - 1} \left[\left(w_j(h_j) + \frac{\partial w_j(h_j)}{\partial h_j} h_j \right) (1 + \tau_j) + \frac{\gamma_j(r + d_j)}{m_j(\theta_j)(1 - \delta_j)} \right]$$

which corresponds to equation (14) in text, and implicitely determines optimal firm size.

8.2 Wage determination

From (17), wages solve the following equation

$$(1 - \beta_j)(E_j - U) = \frac{\beta_j}{1 + \tau_j} \frac{\partial V_j(h_j)}{\partial h_j}.$$
 (29)

where the term $\frac{\partial V_j(h_j)}{\partial h_j}$ is given by (28). Substituting equations (28) and (16) into equation (29) we get:

$$(1 - \beta_j) \frac{w_j - rU}{r + d_j} = \frac{\beta_j}{(r + d_j)(1 + \tau_j)} \left[A_j \frac{\sigma_j - 1}{\sigma_j} p_j - \left(w_j(h_j) + \frac{\partial w_j(h_j)}{\partial h_j} h_j \right) (1 + \tau_j) \right]$$

or

$$w_j = (1 - \beta_j)rU + \frac{\beta_j}{1 + \tau_j} \left[A_j \frac{\sigma_j - 1}{\sigma_j} p_j - \frac{\partial w_j(h_j)}{\partial h_j} h_j (1 + \tau_j) \right]$$

or

$$\frac{\partial w_j(h_j)}{\partial h_j} + \frac{1}{\beta_j h_j} w_j - \frac{(1 - \beta_j)rU + \beta_j \frac{\sigma_j - 1}{\sigma_j (1 + \tau_j)} p_j A_j}{\beta_j h_j} = 0$$
(30)

which defines the wage w_j as a solution to a differential equation of the form $\frac{\partial w_j}{\partial h_j} + F(h_j)w_j(h_j) + G(h_j) = 0$, with $F(h_j) = \frac{1}{\beta_j h_j}$ and $G(h_j) = -\frac{(1-\beta_j)rU + \beta_j \frac{\sigma_j - 1}{\sigma_j (1+\tau_j)}p_j A_j}{\beta_j h_j}$. Equation (30) admits as a solution

$$w_j(h_j) = \left[K - \int_0^{h_j} \frac{G(\zeta)}{H(\zeta)} d\zeta\right] H(h_j) \tag{31}$$

where H(.) solves the homogeneous equation $dH/dh_j + F(h_j)H(h_j) = 0$ which can be rewritten

$$\frac{dH/dh_j}{H(h_j)} = -F(h_j) \text{ or } h_j \frac{dH/dh_j}{H(h_j)} = -1/\beta_j$$

Thus

$$H(h_j) = h_j^{-1/\beta_j}$$

As in Cahuc and Wasmer (2001), we assume the wage w_j is bounded at $h_j = 0$, which implies K = 0 in equation (31). w_j can then be rewritten as:

$$w_{j}(h_{j}) = h_{j}^{-1/\beta_{j}} \int_{0}^{h_{j}} \zeta^{1/\beta_{j}-1} \left[\frac{(1-\beta_{j})}{\beta_{j}} rU + \frac{\sigma_{j}-1}{\sigma_{j}(1+\tau_{j})} p_{j}(\zeta) A_{j} \right] d\zeta$$
$$= (1-\beta_{j}) rU + \beta_{j} \frac{\sigma_{j}-1}{\sigma_{j}(1+\tau_{j})} h_{j}^{-1/\beta_{j}} A_{j} \int_{0}^{h_{j}} \zeta^{1/\beta_{j}-1} p_{j}(\zeta) d\zeta$$

Integrating by parts and using the fact that $dp_j/d\zeta = -p_j/\sigma_j\zeta$ according to equation (??), so that $\int_0^{h_j} \zeta^{1/\beta_j-1} p_j(\zeta) d\zeta = \frac{\sigma_j}{\sigma_j-\beta_j} h_j^{1/\beta_j} p_j(h_j)$. This leads to equation (19):

$$w_{j}(h_{j}) = (1 - \beta_{j})rU + \beta_{j} \frac{\sigma_{j} - 1}{\sigma_{i} - \beta_{j}} \frac{A_{j}p_{j}(h_{j})}{(1 + \tau_{i})}.$$
(32)

as appears in equation (19)...

Finally, differentiating (32) with respect to h_j , and using the fact that $h_j \frac{\partial p_j(h_j)}{\partial h_j} = -\frac{1}{\sigma} p_j(h_j)$ yields

$$\frac{\partial w_j(h_j)}{\partial h_j}h_j = -\frac{\sigma_j - 1}{\sigma_j - \beta_j} \frac{\beta_j A_j p_j(h_j)}{\sigma_j (1 + \tau_j)} < 0.$$
(33)

as appears in equation (20).

8.3 Price determination

From the mark-up equation (14) we have:

$$p_j(h_j) = \frac{1}{A_j} \left(\frac{\sigma_j}{\sigma_j - 1} \right) \left[\left(w_j(h_j) + \frac{\partial w_j(h_j)}{\partial h_j} h_j \right) (1 + \tau_j) + \frac{\gamma_j(r + d_j)}{m_j(\theta_j)(1 - \delta_j)} \right]$$
(34)

Then, the terms $w_j(h_j)$ and $\frac{\partial w_j(h_j)}{\partial h_j}h_j$ in (34) can be substituted by their expressions, given respectively by (32) and (33). This yields

$$p_{j} = \frac{1}{A_{j}} \frac{\sigma_{j} - \beta_{j}}{\sigma_{j} - 1} \left[rU(1 + \tau_{j}) + \frac{\gamma_{j}(r + d_{j})}{m_{j}(\theta_{j})(1 - \delta_{j})(1 - \beta_{j})} \right]$$
(35)

which determines the optimal price set by firms as a function exclusively of variables exogenous to the firm's decision. Then, substituting workers' reservation wage in equation (35), it can then be shown that prices depend on sectoral tightnesses solely. Namely, from (15), workers' reservation wage can be written:

$$rU = z + \sum_{j \in \{I,F\}} \theta_j m_j(\theta_j) (E_j - U)$$

or, using the Nash bargaining equation (29) and the optimality condition $\frac{\partial V_j}{\partial h_j} = \frac{\gamma_j}{m_j(\theta_j)(1-\delta_j)}$

$$rU = z + \sum_{j \in \{I,F\}} \theta_j m_j(\theta_j) \frac{\beta_j}{(1+\tau_j)(1-\beta_j)} \frac{\partial V_j}{\partial h_j}$$
(36)

$$= z + \sum_{j \in \{I,F\}} \frac{\beta_j}{(1+\tau_j)(1-\beta_j)} \frac{\gamma_j \theta_j}{1-\delta_j}$$
 (37)

Finally, substituting (36) in (35) yields:

$$p_{j} = \frac{1}{A_{j}} \frac{\sigma_{j} - \beta_{j}}{\sigma_{j} - 1} \left[(1 + \tau_{j})z + \frac{1 + \tau_{j}}{1 + \tau_{k}} \frac{\beta_{k}}{1 - \beta_{k}} \frac{\gamma_{k}\theta_{k}}{1 - \delta_{k}} + \frac{r + d_{j} + \theta_{j}m_{j}(\theta_{j})}{(1 - \delta_{j})(1 - \beta_{j})} \frac{\gamma_{j}}{m_{j}(\theta_{j})} \right]$$
(38)

where $j, k \in \{I, F\}, k \neq j$. With some abuse of notation, this can be written $p_j(\theta_j, \theta_k)$, an increasing function of its two arguments, θ_j and θ_k .

8.4 Summary of equilibrium relationships

8.4.1 Short-run equilibrium

A short-run equilibrium is defined as a tuple $(rU^*, p_j^*, w_j^*, L_j^*, u^*, \theta_j^*, v_j^*, h_j^*, C_j^*, R^*)$, with j = I, F, for a given value of N_j for each industry.

Workers' Reservation wage. From (36), we have

$$rU^* = z + \sum_{j=F,I} \frac{1}{1+\tau_j} \frac{\beta_j}{1-\beta_j} \frac{\gamma_j \theta_j^*}{1-\delta_j}$$

$$\tag{39}$$

Prices. From (38),

$$p_{j}^{*} \equiv p_{j} \left(\theta_{j}^{*}, \theta_{k}^{*} \right) = \frac{\sigma_{j} - \beta_{j}}{\sigma_{j} - 1} \frac{1}{A_{j}} \left[\left(1 + \tau_{j} \right) z + \frac{1 + \tau_{j}}{1 + \tau_{k}} \frac{\beta_{k}}{1 - \beta_{k}} \frac{\gamma_{k} \theta_{k}^{*}}{1 - \delta_{k}} + \frac{r + d_{j} + \beta_{j} \theta_{j}^{*} m_{j} \left(\theta_{j} \right)}{\left(1 - \delta_{j} \right) \left(1 - \delta_{j} \right)} \frac{\gamma_{j}}{m_{j} \left(\theta_{j}^{*} \right)} \right]$$

$$(40)$$

Wages. By substituting (35) into the wage function (32), we derive wages as a function of variables the firm takes as given when making decisions:

$$w_j = rU^* + \frac{\beta_j}{1 - \beta_j} \frac{\gamma_j(r + d_j)}{m_j(\theta_j^*)(1 - \delta_j)(1 + \tau_j)}$$
(41)

Then, substituting (39) into (41) we get

$$w_{j}^{*} \equiv w_{j} \left(\theta_{j}^{*}, \theta_{k}^{*} \right) = z + \frac{\beta_{j}}{1 - \beta_{j}} \frac{\gamma_{j} \left(r + d_{j} + \theta_{j}^{*} m_{j} \left(\theta_{j}^{*} \right) \right)}{\left(1 - x_{j} \right) m_{j} \left(\theta_{j}^{*} \right) \left(1 + \tau_{j} \right)} + \frac{1}{1 + \tau_{k}} \frac{\beta_{k}}{1 - \beta_{k}} \frac{\gamma_{k} \theta_{k}^{*}}{1 - \delta_{k}}$$
(42)

for $j \in \{I, F\}$ and $k \neq j$.

Aggregate Price Index.

$$P^* = 1 = \left[\alpha p_I^{*1-\sigma} + \alpha p_F^{*1-\sigma}\right]^{1/(1-\sigma)}$$

Labor Market Flow Equilibrium.

$$L_{j}^{*} = \left[1 + \frac{d_{j}}{\theta_{j}^{*}m(\theta_{j}^{*})} + \frac{d_{j}}{d_{k}}\frac{\theta_{k}^{*}m_{k}(\theta_{k}^{*})}{\theta_{j}^{*}m_{j}(\theta_{j}^{*})}\right]^{-1}, \text{ for } j = F, I,$$
(43)

$$u^* = 1 - L_F^* - L_I^* \tag{44}$$

$$v_i^* = \theta_i^* u^* \tag{45}$$

Firms' size.

$$h_j^* = L_j^* / N_j \equiv h_j(\theta_j^*, \theta_k^*) \tag{46}$$

where $j \in \{I, F\}$ and $k \neq j$, and where N_j can be treated as a parameter in the short run, and will be endogenized in the longer run.

Product Market equilibrium.

$$C_j^* = (p_j^*)^{-\sigma} \alpha R^* = A_j L_j^* \tag{47}$$

Aggregate Income.

$$R^* = \sum_{j=I,F} A_j p_j \left(\theta_j^*, \theta_k^*\right) L_j \left(\theta_j^*, \theta_k^*\right). \tag{48}$$

8.4.2 Long-run equilibrium

The next step is to determine the equilibrium number of firms in each industry. We have : Sectoral elasticities.

$$\sigma_i^* = \sigma N_i^*$$

Free entry.

$$c_j + \frac{\gamma_j h_j^*}{m_j(\theta_j^*)} = \frac{1+r}{r+\delta_j} \pi_j^* \tag{49}$$

Firms' profits.

$$\pi_j^* = p_j^* A_j h_j^* - w_j^* h_j^* (1 + \tau_j) - \gamma_j v_j^*$$

$$= p_j^* A_j h_j^* - w_j^* h_j^* (1 + \tau_j) - \gamma_j s_j h_j^* / m_j(\theta_j^*)$$
(50)

8.5 A particular case: identical sectors

It makes sense to determine how the economy would behave in the absence of differences between the formal and the informal sector, that is, if there were only one sector in the economy. This symmetric case can serve as a reference point to be compared to the case studied in our paper, where there are two different sectors. In the symmetric case, we have $p_j^* = p_k^* = 1$, $\theta_j^* = \theta_k^* = \theta^*$ and $L_j^* = L_k^* = L^*$, which makes the model particularly simple to study. From equation (??), labor market tightness θ^* is implicitly defined by:

$$A = \frac{\sigma N - \beta}{\sigma N - 1} \left[(1 + \tau)z + \frac{\beta}{1 - \beta} \frac{\gamma \theta^*}{1 - \delta} + \frac{1}{1 - \beta} \frac{r + d + \beta \theta^* m(\theta^*)}{1 - \delta} \frac{\gamma}{m(\theta^*)} \right]. \tag{51}$$

By applying the implicit function theorem to equation (51) we carry out a number of comparative statics which are described below.

Effect of a rise in competition N on wages, tightness and (un)employment. From equation (51), the short-run impact of increasing competition is unambiguously a rise in θ^* . In turn, this implies a rise in employment $L^* = \frac{2\theta^*m(\theta^*)}{2\theta^*m(\theta^*)+d}$ and a decrease in unemployment $u^* = \frac{d}{2\theta^*m(\theta^*)+d}$. However, this is the result of two opposite effects, as the term $\frac{\sigma N-\beta}{\sigma N-1}$ in equation (51) can itself be decomposed in two terms: (i) N reduces the markup factor $\frac{\sigma N}{\sigma N-1}$ while (ii) it increases the overhiring factor $\frac{\sigma N-\beta}{\sigma N}$. According to (i), more competition leads to lower markup, higher output and lower unemployment. According to (ii), overhiring is positively related to market power. A rise in N thus reduces incentives to overhire, and thus tends to increase wages, which is detrimental to employment. It is straightforward to show that the former effect always dominates the latter so that employment increases when market power decreases.

Effect of a rise in workers' bargaining power β . The short-run impact of raising workers' bargaining power β on tightness is a priori ambiguous. This is the result of two opposite effects: (i) a rise in β translates into higher labor costs (the term in brackets in equation (51)) which reduces tightness θ^* . However, (ii) a rise in β increases firms incentives to overhire, which counteracts (i). It is possible to show that $\partial \theta/\partial \beta \geq 0$ whenever

$$\sigma \leq \frac{(1+\tau)z + \frac{1}{1-\beta} \frac{r + d + 2\beta\theta^* m(\theta^*)}{1-\delta} \frac{\gamma}{m(\theta^*)} + \beta \frac{r + d + 2\theta^* m(\theta^*)}{(1-\delta)(1-\beta)^2} \frac{\gamma}{m(\theta^*)}}{\frac{r + d + 2\theta^* m(\theta^*)}{(1-\delta)(1-\beta)^2} \frac{\gamma}{m(\theta^*)}}$$

For low levels of σ (low competition), a rise in β raises firms' incentives to overhire. As a result, θ^* and L^* should increase. For larger levels of σ , a rise in workers' bargaining power β raises labor costs and this leads to a fall in θ^* and L^* .

Effect of a rise in τ , z, γ . The short-run impact of a rise in τ , z and γ is lower tightness and lower employment. From (51), those three parameters increase wage or search costs for firms, which leads to a fall in tightness and employment. On the contrary, the short run impact of a rise in productivity is higher tightness and higher employment.

Effect of the overhiring factor $\frac{\sigma N - \beta}{\sigma N}$. In the absence of bargaining externalities, the overhiring factor $\frac{\sigma N - \beta}{\sigma N}$ in equation (51) would be equal to one, and the resulting equilibrium tightness θ_{noovh} would solve :

$$A = \frac{\sigma N}{\sigma N - 1} \left[(1 + \tau)z + \frac{\beta}{1 - \beta} \frac{\gamma \theta_{noovh}}{1 - \delta} + \frac{1}{1 - \beta} \frac{r + d + \beta \theta_{noovh} m(\theta_{noovh})}{1 - \delta} \frac{\gamma}{m(\theta_{noovh})} \right]$$
(52)

A comparison of (52) and (51) implies that $\theta^* \geq \theta_{noovh}$. This also implies that $w(\theta^*) \geq w(\theta_{noovh})$, and that $L^* \geq L_{noovh}$. That is, tightness, wages and employment are higher in the presence of the overhiring externality.

8.6 Uniqueness of equilibrium

Step 1. Properties of the price functions (40).

$$p_{j} = \frac{\sigma_{j} - \beta_{j}}{\sigma_{j} - 1} \frac{1}{A_{j}} \left[(1 + \tau_{j})z + \frac{1 + \tau_{j}}{1 + \tau_{k}} \frac{\beta_{k}}{1 - \beta_{k}} \frac{\gamma_{k}\theta_{k}}{1 - \delta_{k}} + \frac{1}{1 - \beta_{j}} \frac{r + d_{j} + \beta_{j}\theta_{j}m_{j}(\theta)}{1 - \delta_{j}} \frac{\gamma_{j}}{m_{j}(\theta_{j})} \right]$$
(53)

where p_j is increasing in θ_j and θ_k .

Step 2. Properties of the Product Market Equilibrium condition (PME).

Combining (47) and (40) we get

$$\frac{L_I}{L_F} = \frac{A_F}{A_I} \left[\frac{p_I(\theta_I, \theta_F)}{p_F(\theta_I, \theta_F)} \right]^{-\sigma} \tag{54}$$

The properties of the PME curve then results from the implicit function theorem. Differentiating (54) we get that the ratio $\frac{L_I}{LF}$ decreases with θ_I if the following condition on price elasticities is fulfilled:

$$\theta_I \frac{\partial p_F / \partial \theta_I}{p_F} < \theta_I \frac{\partial p_I / \partial \theta_I}{p_I}. \tag{55}$$

Similarly, the ratio $\frac{L_I}{LF}$ increases with θ_F if the following condition on price elasticities holds:

$$\theta_F \frac{\partial p_F / \partial \theta_F}{p_F} > \theta_F \frac{\partial p_I / \partial \theta_F}{p_I} \tag{56}$$

If these two conditions are not fulfilled, then the PME curve is not necessarily monotonic in the (θ_{F}, θ_{I}) space. Nevertheless, our simulations indicate that this is the case.

Step 3. Properties of the labor Market Flow Equilibrium condition (LME).

$$\frac{L_I}{L_F} = \frac{d_F}{d_I} \frac{\theta_I m_I(\theta_I)}{\theta_F m_F(\theta_F)} \tag{57}$$

The RHS of (57) is decreasing in θ_F and increasing in θ_I . Therefore, the (LME) curve is upward sloping in the (θ_F, θ_I) space.

Step 4. Properties of the IAL curve.

Using LME and PME, we get the following IAL relationship:

$$\frac{d_F}{d_I} \frac{\theta_I m_I(\theta_I)}{\theta_F m_F(\theta_F)} = \frac{A_F}{A_I} \left[\frac{p_I(\theta_I, \theta_F)}{p_F(\theta_I, \theta_F)} \right]^{-\sigma} \tag{58}$$

which implicitly defines θ_I as a function of θ_F . From step 2, we know that the LHS of equation (58) is monotonic if conditions (55) and (56) are met. Under those assumptions, the IALA

relationship depicts an increasing relationship between θ_I and θ_F . Here, again, our simulations indicate that this is the case.

Step 5. Properties of the PC curve.

Using (??), the definition of the aggregate price index, $P^* = \alpha^{1/(1-\sigma)} \left[p_I(\theta_I, \theta_F)^{1-\sigma} + p_F(\theta_I, \theta_F)^{1-\sigma} \right]^{1/(1-\sigma)}$, and the normalization $P^* = 1$, the PC relationship can be written :

$$1 - \alpha p_I(\theta_I, \theta_F)^{1-\sigma} = \alpha p_F(\theta_I, \theta_F)^{1-\sigma}. \tag{59}$$

Given the properties of prices studied in step 1, this equation implicitly defines a decreasing relationship between θ_I and θ_F .

Step 6. Properties of the equilibrium.

An equilibrium is the pair (θ_I^*, θ_F^*) at the intersection of the IAL and PC curves studied in steps (4) and (5). The figure below illustrates the benchmark where an upward sloped IAL curve and an downward sloped PC establish the (unique) equilibrium.

Figure 13 about here

Comparative statics properties of the equilibrium result from shifts of these curve, and they are studied numerically.

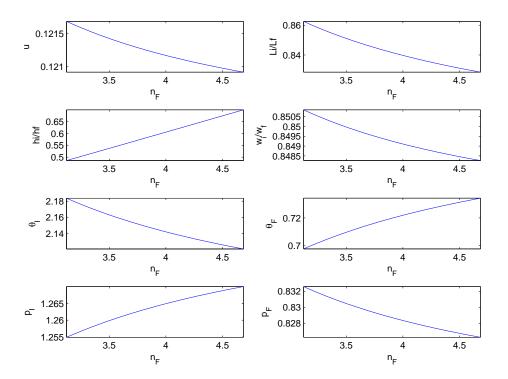


Figure 6: The short-run impact of varying competition.

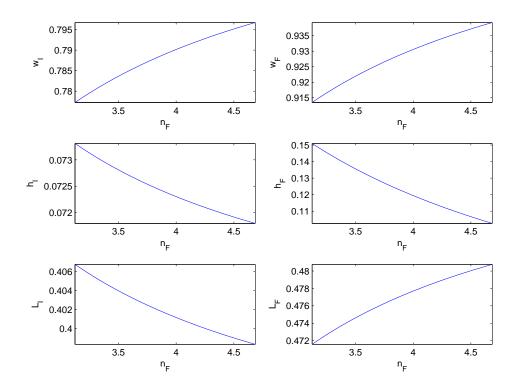


Figure 7: The short-run impact of varying competition (cont'd).

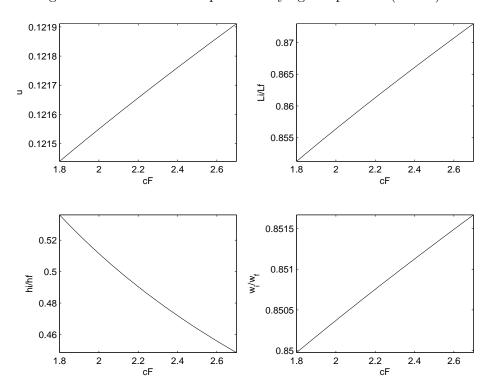


Figure 8: The long-run impact of varying barriers to entry in the formal sector

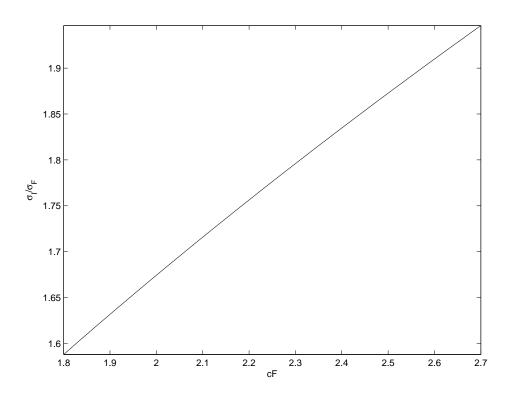


Figure 9: The long-run impact of varying barriers to entry in the formal sector (cont'd)

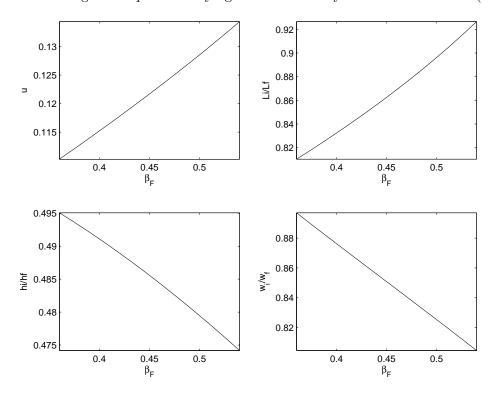


Figure 10: The long-run impact of varying bargaining power in the formal sector

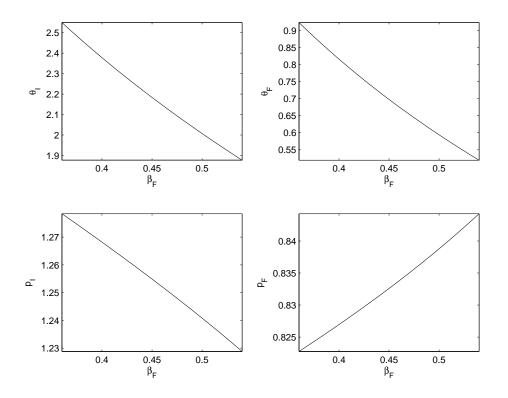


Figure 11: The long-run impact of varying bargaining power in the formal sector (cont'd)

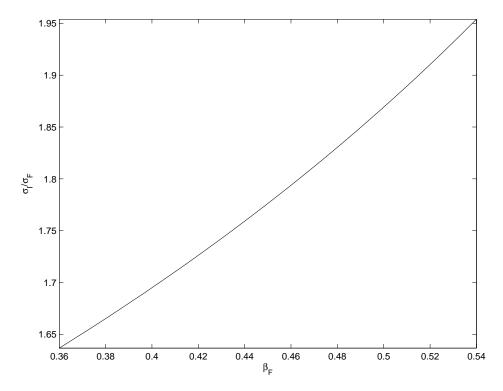


Figure 12: The long-run impact of varying bargaining power in the formal sector (cont'd)

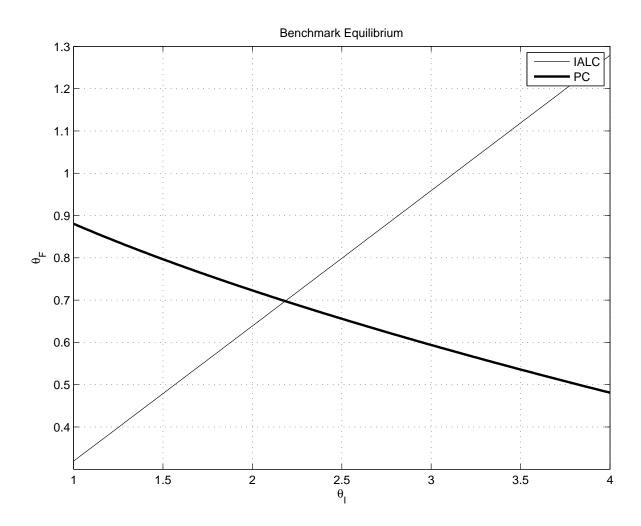


Figure 13: Equilibrium in the benchmark case ${\cal C}$