

Pension and the Family

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Abstract

The effects of pension policies on fertility have been examined in the overlapping generation (OLG) model of unitary household in which no heterogeneity between wife and husband exists. This paper departs from the OLG model and focuses on the marital bargaining arising from the heterogeneity in a couple in a non-unitary model. Specifically, this paper examines how the pension policy affects the endogenous fertility of a bargaining couple who have different lifespans. The analysis finds out a new channel of pension policy on fertility decisions: an increase in pension size affects fertility not only via the changes in current and future income, but through a change in marital bargaining power. This channel leads a plausible argument that an increase in a pay-as-you-go (PAYG) pension further accelerates a decline in fertility through the empowerment of women.

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1 Introduction

Acceleration in demographic aging has caused many developed countries to reform their existing pension systems. Against a background of this policy concern, the mutual dependence relationship between fertility and public pension has come under intense study (Cigno, 1993; Zhang and Zhang, 1998; Wigger, 1999; Yakita, 2001; Groezen et al., 2003; Groezen and Meijdam, 2008; Hirazawa and Yakita, 2009). Economists are intrigued with the pay-as-you-go (PAYG) pension system as an inter-generational redistribution device that involves the intra-generational redistribution effect.¹ If the PAYG pension system is generous to be equally beneficial to all individuals, it induces the redistribution among heterogeneous households. Some studies deal with heterogeneity among households, but they draw the household as a single decision unit based on unitary model, and do not consider heterogeneity within the household. This paper adopts different approach. By focusing on the marital bargaining arising from the heterogeneity in a couple, we describe the intra-generational redistribution effect of the pension policy and how its expansion affects the balance of power between husband and wife, and the fertility of the couple having different lifespans.

Heterogeneity within a household can be factors that bring about intra-generational redistribution. For example, an expansion of a generous pension system means an implicit income transfer from the shorter longevity spouse to the spouse with longer longevity. Recent studies based on the non-unitary model have considered this intra-redistribution effect in the retirement period.²

¹Sinn (2004) considers redistribution from households with children to those without, because children can be insurance devices for households who cannot have children in the PAYG pension scheme. Cremer et al. (2008) consider redistribution under both funded and unfunded pension systems in the presence of different abilities in raising children among households. Hirazawa et al. (2013) focus on redistribution among households with different contributions as a result of different childcare schedules. Heterogeneity among households is discussed in the many studies on public policies. Bommier et al. (2011a, 2011b) consider the problem of redistribution among households with different longevity. Cremer et al. (2004) examine how the redistribution effect of implicit tax imposed on postponed retirement affects households' retirement activities in the presence of different productivities and health statuses. Cremer et al. (2010) consider a trade-off between redistribution due to heterogeneous productivities and redistribution caused by heterogeneous longevity (which is positively correlated with productivities).

²The distribution effect of public policy among family members in the young period is theoretically considered by Lundberg and Pollak (1993). Komura (2012, 2013) theoretically examines the intra-family distribution effect of policy shifts from in-cash child support to in-kind child support, and the shift of unit of income taxation from household to individual,

Theoretically, Browning (2000) showed that a generous pension system involves redistribution from husbands to wives following the fact that women tend to live longer, and that it results in increased savings, which is favorable household allocation for wives.³ Empirical study of Duflo (2003) also confirms the intra-generational redistribution effect of an expansion of a generous pension in South Africa, which is more likely to be beneficial for wives because of their longer period of life. Although they shed new light on the redistribution effect of public policies within the families in retirement period, the long-run effects of policies on household fertility decisions are not examined. The purpose of this paper is to explore the effects of the PAYG pension system on fertility, taking into account gender difference in longevity and its effect on redistribution within the household.

Our model has three features. The first is that the household makes a decision through intra-household bargaining.⁴ Homogeneous couples look like the picture of happiness, but the reality proves different. It is known that wives tend to be younger than their husbands, and that they tend to live longer than their husbands do.⁵ The difference in lifespan leads couples to bargain over the saving in the young because the wife wants to have greater wealth at the retirement stage (Lundberg and Ward-Butts, 2000; Lundberg et al., 2003), which may reduce the demand for private consumption and the number of children in the young period. To gain insight into the declining birthrate, we must find the channel of policy effects by accounting for the endogenous marital relationship of heterogeneous spouses. The second feature is considering the effect of the pension system on fertility in a family bargaining model in which the balance of power of the young couple is affected by social norms or peer pressure.⁶ In

respectively. Lundberg et al. (1997) found a significant redistribution effect caused by the shift of the child allowance recipient from fathers to mothers in the UK.

³Aura (2005) also uses the American legislation change of 1984 in favor of wives, who are likely to be widowed because of their higher life expectancies, to show that this implicit income transfer leads the household wealth portfolio to reflect the wife's intentions more.

⁴Social security is explored in recent studies with a non-unitary representation of the household, but in which household members behave non-cooperatively. In contrast to our setting of family bargaining, Glazer (2008) showed that couple's non-cooperative strategic interactions result in inefficient household savings, and that the social security system can improve welfare because it forces them to secure savings.

⁵The United Nations (2000), based on 236 countries, reported that husbands are older than their wives in all but one country. This husband-wife age gap tends to be larger in developing countries, especially African nations, but smaller in developed countries.

⁶This concept is based on Grossbard-Shechtman (1984) and Lundberg and Pollak (1993), both of which suggested that marriage relations are determined in a marriage market that

our model, the bargaining power depends on the difference between the average lifetime income of men and women in the economy, and hence, the bargaining positions of marriage are affected by the PAYG pension system. This reflects empirical evidence that social security affects the balance of power in a couple (Duflo, 2003). The third feature of our model is that fertility is determined endogenously. Most studies based on life-cycle models of a household with multiple decision units focus on household wealth or behaviors for the retirement period, with little interest in fertility. Here, we formulate a model of family bargaining in which fertility is endogenous under the PAYG pension system.

This study reveals a new channel of pension policy on fertility decisions; an increase in pension size affects fertility not only via the changes in current and future income, but also through a change in marital bargaining power. Specifically, the study presents a plausible argument that an increase in the PAYG pension further accelerates a decline in fertility compared to the unitary model, in which the bargaining power of the couple is not of interest. Increasing a generous pension system induces intra-household redistribution between spouses with different longevities, as well as the inter-generational income redistribution between young and old generations, as discussed in the traditional unitary model. Since this redistribution from short-living husbands to long-living wives alters the balance of power of couples through the changes in their relative expected lifetime incomes, this change favors wives who expect that they will live longer than their husbands will. The change in the balance of power within the couple affects their decision on the number of children they have, because the wife has the longer lifespan, so that she has a larger incentive for saving by reducing expenditure in the young period.

This paper is organized as follows. Section 2 presents a model of two family members with different longevity. Section 3 explores the equilibrium of our model. Section 4 carries out our policy analysis and Section 5 concludes the paper.

2 Model

Consider a small open economy, comprising one representative household and a government. The household consists of two individuals ($i = f, m$), where f and m reflects cultures or social norms.

m denote the female (wife) and male (husband), respectively. Each individual lives for at most two periods: young and old. Although everyone can certainly live through the young period, there is uncertainty in old age. For the sake of simplicity, we assume that the individual is either alive or dead at the beginning of the old period. The probability that individual i survives in the old period is denoted by λ_i . To incorporate the gender difference in longevity, we assume that the wife has a longer lifespan than the husband: $\lambda_f > \lambda_m$. In the young period, individuals get married with the partner j ($j \neq i$), raise their children, and earn an income by supplying their time in the labor market. After paying tax, they allocate their collective earnings among their private consumptions and saving for retirement. In the retirement period, they consume with the pension benefit and the return from their savings. The government employs the PAYG pension scheme for income distribution from young to old generations. It imposes a tax on each household in the young period to finance the pension benefit for the elderly living in the same period.

Household. Individual i in a household gains utility from consumption in the young and old periods, as well as the number of children. The utility function of individual i born at period t , who belongs to generation t , is assumed to be:

$$EU_{it} = \ln n_t + \ln c_t + \lambda_i \ln d_{t+1}, \quad (1)$$

where n_t is the number of children of each gender who belong to the couple in generation t , which means that one unit of n_t corresponds to a pair of son and daughter.⁷ In (1), c_t and d_{t+1} are the couple's consumption of private goods in the young and old periods, respectively. We assume that the wife and the husband consume the same amount of private goods. Our main results do not change if we remove this assumption. Even though their preferences are identical, there exists a gender gap in longevity within their expected utilities. The household welfare function is the sum of the weighted utilities of the spouses:

$$V_t = \theta_t EU_{ft} + (1 - \theta_t) EU_{mt}, \quad (2)$$

where $\theta_t \in [0, 1]$ represents the bargaining power of the wife. Following Chiap-

⁷This approach was also used in the theoretical models of Galor and Weil (1996), Abio et al. (2004), Doepke and Tertilt (2009), and de la Crox and Donckt (2010). Abio et al. examined the relationship between social security and fertility in the OLG model of two-earner household, but they treated household as decision unit and do not deal with the marital bargaining.

pori (1988, 1992) and Apps and Rees (1988), we assume that household members can always achieve an efficient allocation based on certain distributional rules within the household. Here, θ_t can be interpreted as the distribution rule in our model.⁸

Each individual is endowed with one unit of time in their young period, and supplies their time in market and domestic work. Childcare activities are the domestic production, so the husband and/or wife commit time to the upbringing of the children. The fixed time for parental attention per child is denoted by z and the time spent on market work by individual i is denoted by L_t^i . Based on the averages of the observations, we assume that husband's wage is higher than the wife's: $w_m > w_f$. Furthermore, we assume the parental time of the wife and the husband are completely substitutable. Thus, it is the most efficient for a couple if the wife takes care of their children, and the husband's endowed time is spent solely on market work: $L_t^f = 1 - zn_t$ and $L_t^m = 1$.⁹

In the young period, the couple chooses the number of children they have, n_t , and allocates the disposable income among their own private goods consumption, c_t , and their savings for retirement, s_t . The budget constraint of the household in the young period is given by:

$$c_t + w_f zn_t + s_t = w_f + w_m - \tau, \quad (3)$$

where τ denotes the lump-sum tax imposed on the household. Here, $w_f + w_m > \tau$ is assumed in the following analysis. In the retirement period, the household members enjoy their private goods consumption, financed by the return from their savings and the pension benefit. The budget constraint of the household in the retirement period is:

$$d_{t+1} = Rs_t + (\lambda_f + \lambda_m)P_{t+1}, \quad (4)$$

where P_{t+1} is the pension benefit to each individual and

⁸The classic formulation of intra-household bargaining was studied in the Nash bargaining model (Manser and Brown, 1980; McElroy and Horney, 1981). They regarded the statuses of single or divorced as threat-points. The threat-points of the Lundberg and Pollak (1993) bargaining model are statuses of non-cooperative equilibrium. Lundberg and Pollak (1996) give an excellent survey on intra-family bargaining.

⁹Easing the assumption of complete substitution does not affect our main results as long as the wife is better at caring for the children.

$$R \equiv \frac{1+r}{\lambda_f + \lambda_m - \lambda_m \lambda_f} \quad (5)$$

is the return rate for the savings after one period, while r is the interest rate. Here, (5) implies that the savings in the young period are returned to the household, as long as one member of the couple survives. In (4), the term $(\lambda_f + \lambda_m)P_{t+1}$ implies that the more probability that the household member i lives during the second period, the more likely he/she can obtain the total pension benefit.

Given the bargaining power, θ_t , the household maximizes (2) subject to (3) and (4). Solving the optimization problem, we have the following demand functions:

$$c_t = \frac{I_t}{2 + \theta_t \lambda_f + (1 - \theta_t) \lambda_m}, \quad (6)$$

$$d_{t+1} = \frac{RI_t [\theta_t \lambda_f + (1 - \theta_t) \lambda_m]}{2 + \theta_t \lambda_f + (1 - \theta_t) \lambda_m}, \quad (7)$$

$$n_t = \frac{I_t}{w_f z [2 + \theta_t \lambda_f + (1 - \theta_t) \lambda_m]}, \quad (8)$$

$$s_t = \frac{[\theta_t \lambda_f + (1 - \theta_t) \lambda_m] (w_f + w_m - \tau) R - 2(\lambda_f + \lambda_m) P_{t+1}}{[2 + \theta_t \lambda_f + (1 - \theta_t) \lambda_m] R}, \quad (9)$$

where $I_t \equiv w_f + w_m - \tau + (\lambda_f + \lambda_m)P_{t+1}R^{-1}$ is the net lifetime income for the couple. The demand functions show that, as the bargaining power of the wife rises, the private goods consumption in the young period and fertility fall, while the savings, and thus, the consumption in the old period, increases: $\partial c_t / \partial \theta_t < 0$, $\partial n_t / \partial \theta_t < 0$, $\partial s_t / \partial \theta_t > 0$ and $\partial d_{t+1} / \partial \theta_t > 0$. Intuitively, there is a conflict between spouses in terms of lifetime goals because the wife thinks she will outlive her husband, while the husband believes the opposite. Hence, the wife wants to save the more money for retirement than her husband. If the wife's bargaining position becomes more favorable than her partner, the household outcomes are more likely to reflect her intentions. Consequently, the private goods consumption in retirement age increases by reducing consumption in the young period, as well as the number of children they have.

PAYG Pension. The government operates the PAYG pension system. It imposes a tax on each household in the young period so that it can finance the

pension benefit for people living in the old period. The government's budget constraint in per household terms is given by:

$$n_t \tau = (\lambda_f + \lambda_m) P_{t+1}. \quad (10)$$

Bargaining Power. We assume that the power balance of young couples is shaped within the marriage market and is affected by social norms or peer pressure (Grossbard-Shechtman, 1984, 1993, 2013; Lundberg and Pollak, 1993; Komura, 2012, 2013).¹⁰ They anticipate the balance of power within the marriage by observing the behaviors and economic relations of their parents. Specifically, the balance of power of the couple in generation t depends on the difference in their average resources of men and women in generation $t - 1$, including the income from the pension benefits of men and women in the preceding generation.

$$\theta_t = \theta \left[w_f L_{t-1}^f - w_m L_{t-1}^m + \beta (\lambda_f - \lambda_m) P_t R^{-1} \right], \quad (11)$$

where $\theta' > 0$ is assumed. For simplicity of notation, we assume $\theta'' = 0$. In (11), the term $w_f L_{t-1}^f - w_m L_{t-1}^m$ represents the gap in labor income, and the term $\beta (\lambda_f - \lambda_m) P_t R^{-1}$ represents the gap in the expected pension benefits that affect the bargaining power of the couple. $\beta \in [0, 1]$ captures how the degree of how the pension policy (or income in the retirement period) affects the balance of power within the marital relationship. If $\beta = 1$, the gap in the expected pension benefits and the gap in labor income have the same effect on the bargaining power. Therefore, the determinant of power for the couple simply becomes the difference between the expected lifetime incomes of men and women. In contrast, $\beta = 0$ reduces our model to that of Komura (2012), in which the pension policy has no impact on the bargaining power.

Recalling that the husband spends his time solely in the labor market, (11) can be rewritten as:

$$\theta_t = \theta \left[w_f (1 - z \bar{n}_{t-1}) - w_m + \beta (\lambda_f - \lambda_m) P_t R^{-1} \right], \quad (12)$$

where \bar{n}_{t-1} stands for the average number of children per household in generation $t - 1$. Note that the wife's bargaining power decreases as the average

¹⁰Using data of European countries and Japan, Feyrer et al. (2008) pointed out that women's status is affected not only by common economic factors but also by the longstanding cultural and social factors.

number of children in the society increases, $\partial\theta_t/\partial\bar{n}_{t-1} = -\theta'w_fz < 0$. This implies that having children by couples in the previous generation weakens the wife's say in the next generation, because a reduction in her earning is expected because of peer pressure. It is also worth mentioning that the expansion of a public pension, which mainly aims to transfer income from young to old, plays a role in the income transfer from husbands to wives in our model, and hence, it increases the wife's bargaining power, $\partial\theta_t/\partial P_t = \theta'\beta(\lambda_f - \lambda_m)R^{-1} > 0$.

3 Equilibrium

3.1 Dynamics

Using (8), (10) and (12), the dynamics of bargaining power can be obtained as:

$$\theta_{t+1} = \theta \left(w_f - w_m - \frac{R(w_f + w_m - \tau)A}{w_fz[2 + \theta_t\lambda_f + (1 - \theta_t)\lambda_m]R - \tau} \right), \quad (13)$$

where

$$A \equiv zw_f - \frac{\beta\tau(\lambda_f - \lambda_m)}{R(\lambda_f + \lambda_m)}. \quad (14)$$

Differentiation gives:¹¹

$$\frac{\partial\theta_{t+1}}{\partial\theta_t} = \frac{(\lambda_f - \lambda_m)z\theta'n_t^2w_fA}{w_f + w_m - \tau}, \quad (15)$$

$$\frac{\partial^2\theta_{t+1}}{\partial\theta_t^2} = -\frac{2z^2w_f^2(\lambda_f - \lambda_m)^2n_t^3\theta'A}{(w_f + w_m - \tau)^2}, \quad (16)$$

If τ is sufficiently small, the sign of (14) tends to be positive, $A > 0$. This corresponds to the case in which the pension policy is inactive, or $\tau = 0$. In contrast, when the pension policy is active and τ is sufficiently large, (14) is likely to take a negative sign, $A < 0$. Supposing that $\theta_{t+1}|_{\theta_t=0} > 0$, (15) and (16) reveal that the bargaining power converges monotonically (cyclically) to the steady-state if $A > (<)0$.¹²

Figure 1. HERE

¹¹See Appendix A.

¹²The stability of the steady-state is ensured by assuming $|\partial\theta_{t+1}/\partial\theta_t| < 1$.

Behind the dynamics of the bargaining power, the dynamics of fertility can be derived in a similar way to show that the fertility converges to the steady state monotonically (cyclically) if $A > (<)0$.

3.2 Steady state

Using (8), (10), and (12), the steady-state value of the bargaining power and the fertility satisfy:

$$\theta = \theta \left(\frac{\beta\tau n(\lambda_f - \lambda_m)}{(\lambda_f + \lambda_m)R} - w_f z n + w_f - w_m \right), \quad (17)$$

$$n = \frac{R(w_f + w_m - \tau)}{w_f z [2 + \theta\lambda_f + (1 - \theta)\lambda_m] R - \tau}. \quad (18)$$

To plot combinations (θ, n) that satisfy (17) and (18) we first reveal how the fertility affects the bargaining power in the steady state equilibrium. From (17) and $\theta'' = 0$, we have:

$$\frac{\partial\theta}{\partial n} = -\theta' A, \quad (19)$$

$$\frac{\partial^2\theta}{\partial n^2} = 0. \quad (20)$$

In (19), if $\tau = 0$ (or $\beta = 0$), then $A > 0$, the effect of fertility on the bargaining power is negative, $\partial\theta/\partial n < 0$. This implies that having another child reduces women's bargaining position since the wife is forced into child rearing, reducing her income from the labor market. Having a child as a factor against women's bargaining power is captured by the first term in (14). If $\tau > 0$ (and $\beta \neq 0$), the sign of $\partial\theta/\partial n$ depends on the relative magnitude of two terms. The second term in the angle bracket of (16) captures the positive effect of having a child on the wife's bargaining power, owing to the PAYG pension system. The more children there are in society, the more the pension benefit increases for the elderly. Because the wife is more likely to survive in the retirement period, her expected benefit from the PAYG pension system is higher than that of her husband's. As the weight of pension benefit in the bargaining power increases, owing to an increase in fertility, the wife becomes invulnerable, strengthening her power within the couple.

Figure 2. HERE

Figure 3. HERE

$\theta(n)$ in Figures 2(a) and 3(a) represents (17) when the pension policy is inactive, i.e., $\tau = 0$ (or $\beta = 0$) or τ is sufficiently small to cause the sign of (19) negative. In contrast, $\theta(n)$ in Figures 2(b) and 3(b) represent the alternative case, in which the pension policy is active, $\tau > 0$ (and $\beta \neq 0$) leading the sign of (19) to be positive.

We next study how fertility is related to the bargaining power in the steady-state. From (18), differentiating n with respect to θ gives: ¹³

$$\frac{\partial n}{\partial \theta} = -\frac{n^2 z w_f (\lambda_f - \lambda_m)}{w_f + w_m - \tau} < 0, \quad (21)$$

$$\frac{\partial^2 n}{\partial \theta^2} = 2n \left[\frac{n z w_f (\lambda_f - \lambda_m)}{w_f + w_m - \tau} \right]^2 > 0. \quad (22)$$

(18) is illustrated as $n(\theta)$ in Figure 2 and Figure 3, showing that the number of children the couple has decreases as the woman's bargaining power increases. This is simply because the wife lives longer than the husband does. As women are likely to live longer, they want to save more money for future consumption rather than spending it on raising children. In such situation, therefore, a rise in women's bargaining power leads to a fall in fertility rate, reflecting their intentions in household decisions.

4 Effects of Pension Policy

In this section, we examine the effects of the changes in the size of a PAYG social security system on fertility and women's bargaining power, focusing on the stable steady-state equilibrium of E_1 in Figures 2(a) and 3(a), and E_5 in Figures 2(b) and 3(b).

First, we come back to the traditional argument in which the bargaining power is fixed. Using (18), this can be confirmed by differentiating n with respect to τ ,¹⁴

¹³See Appendix A.

¹⁴See Appendix A.

$$\frac{dn}{d\tau}\Big|_{d\theta=0} = -\frac{n(R-n)}{R(w_f + w_m - \tau)}. \quad (23)$$

Here, (23) shows that, given bargaining power θ , an increase in the tax rate reduces (increases) the fertility if $R > (<)n$.

An increase in the size of the pension policy, represented by τ , affects fertility via the change in the lifetime full income in two ways: (i) the reduction in the disposable income of the working period decreases the number of children, and (ii) the increase in the pension benefit allows the household to reduce their savings for the old period and increases their fertility. In other words, the comparison between R and n means whether the present value of leaving τ as disposable income in the young period is larger or smaller than the present value of the pension benefit as a return of tax payments. The well-known Aaron-Samuelson condition states that the inter-generational transfer under the lump-sum financed PAYG pension benefits future generations if the economy is dynamically inefficient, $1 + r < n$ (Samuelson, 1958; Aaron, 1966). While the interest factor is adjusted by the longevity in our model, there is strong support for the government operating the PAYG pension system, and that examining the effects of pension policy is relevant if $R < n$. When $R < n$, the positive effects of a pension expansion on lifetime income overwhelms the negative effects. As a result, an increase in lifetime income induces a rise in the number of children, as children are normal goods in our model.

On the other hand, if the economy is dynamically efficient, $1 + r > n$, the introduction of the lump-sum financed PAYG-scheme basically loses its theoretical foundation. However, as summarized by Groezen et al. (2003), the political incentives may promote the introduction of an unfunded pension scheme or, a drastic policy reform is often difficult from a practical standpoint, even if the environment surrounding the economy becomes against a PAYG pension. If the PAYG pension system is operated under the condition that $R > 1 + r > n$, and the government increases the size of the pension policy, the negative effect on fertility of a decrease in disposable income in the young period outweighs the positive effect of an increase in pension benefit, which results in a fall in fertility rate.

In Figures 2(a) and 2(b), the policy effects on the fertility, given θ , are depicted by the shift of the $n(\theta)$ curve. When $R < n$, the sign of (23) becomes

positive, becomes positive, which shifts the curve from $n(\theta)$ to $n^1(\theta)$. In contrast, if $R > n$, (23) becomes negative, and the curve $n(\theta)$ shifts left (see Figures 3(a) and 3(b)).

The important feature of our model is that the pension policy influences the bargaining power in the couple, which also has an impact on the fertility. From (17), given n , we find that, as the pension policy increases, so does the woman's bargaining power:

$$\frac{d\theta}{d\tau}\Big|_{dn=0} = \frac{\beta n(\lambda_f - \lambda_m)}{(\lambda_f + \lambda_m)R} > 0. \quad (24)$$

This indicates that an increase in the size of a pension policy, represented by τ , induces an upward shift of the $\theta(n)$ curve in Figure 2 and Figure 3. This is simply because the increase in pension works to the longer-living woman's advantage, increasing her bargaining power. In this case, as β is larger, the pension benefit is appreciated in determining the balance of power between men and women, so that the change in the pension policy affects θ significantly. Similarly, as the gender gap in life expectancy $\lambda_f - \lambda_m$ is larger, the gap in the expected pension benefit between men and women widens, resulting in a significant change in θ . In such situations, an increase in τ induces a relatively large upward shift in $\theta(n)$.

The steady-state equilibrium, n^* and θ^* , satisfy (17) and (18). We first explain the effects of an increase in τ on (n^*, θ^*) when $R < n$, i.e., $(dn/d\tau)|_{d\theta=0} > 0$ in (23). Figures 2(a) and 2(b) show the cases in which, given other variables, the effect of an increase in pension size on fertility is modest, while an increase in the pension has a great impact on bargaining power. This case tends to take place when β and $\lambda_f - \lambda_m$ are large as explained above. In Figure 2(a), for instance, if we assume that the bargaining power is an exogenous parameter, then the increase in the size of the pension increases fertility along the course from E_1 to E_3 . However, as the bargaining power is endogenous in our model, the woman's bargaining power is strengthened by the increase in the size of the pension, moving the stable equilibrium from E_1 to E_4 . This shows that a rise in τ induces a fall in fertility. The same holds for Figure 2(b). If the bargaining power is exogenous, the increase in increases fertility, along the course from E_5 to E_6 . However, it decreases fertility by shifting the equilibrium from E_5 to E_7 as the bargaining power of the wife increases. Consequently, the fertility rate in

the economy may fall if the bargaining power is determined endogenously.

The case of $R > n$, i.e., $(dn/d\tau)_{d\theta=0} < 0$, can be interpreted in a similar fashion, by making use of Figures 3(a) and 3(b). Both figures show that fertility decreases not only through the decrease in lifetime net income but also through the increase in the bargaining power of the wife, if the pension policy changes the balance of power significantly.

Some empirical studies with unitary models support the case in which the pension expansion by an increase in τ causes a decline in fertility (Cigno and Rosati, 1996; Boldin et al., 2005). Our model shows that the fertility rate falls not only because of the negative income effect (i.e., the leftward shift of the $n(\theta)$ curve) but also the negative bargaining effect (i.e., the upward shift of the $\theta(n)$ curve). If there is no heterogeneity within a household, $\lambda_f = \lambda_m$, the pension policy has no influence on the bargaining power (see (24)), and thus the effects of the pension policy are essentially the same as that the traditional unitary model found. This is because the spouses' lifetime objects are identical, so that they do not need to negotiate household allocations. In the real economy with gender differences, if policy makers ignore the bargaining power effect, the negative effects of a pension reform on fertility could be biased or could reverse the sign of the impact estimated initially.

Using (17) and (18), the graphical analysis mentioned above can be formally restated as follows:

$$\frac{dn^*}{d\tau} = \left(\frac{\partial n}{\partial \tau} + \frac{\partial n}{\partial \theta} \frac{\partial \theta}{\partial \tau} \right) \Delta^{-1} = \frac{n}{\tau \Delta} \left(\underbrace{\epsilon_{n\tau}}_{+-} + \underbrace{\epsilon_{n\theta}}_{-} \underbrace{\epsilon_{\theta\tau}}_{+} \right), \quad (25)$$

$$\frac{d\theta^*}{d\tau} = \left(\frac{\partial \theta}{\partial \tau} + \frac{\partial \theta}{\partial n} \frac{\partial n}{\partial \tau} \right) \Delta^{-1} = \frac{\theta}{\tau \Delta} \left(\underbrace{\epsilon_{\theta\tau}}_{+} + \underbrace{\epsilon_{\theta n}}_{+-} \underbrace{\epsilon_{n\tau}}_{+-} \right), \quad (26)$$

where $\Delta \equiv 1 - (\partial n / \partial \theta)(\partial \theta / \partial n) > 0$ and ϵ_{km} ($k \neq m$) denotes the elasticity of $k(= n, \theta)$ with respect to $m(= \tau, n, \theta)$ ¹⁵.

The first term in (25) represents the effects of an increase in τ on fertility through changes in lifetime full income, which is regarded as an inter-generational distribution effect by conventional studies. The sign can be positive or negative, depending on the relative magnitude between R and n as in (23). The second term in (25) stands for the effect caused by a change in the power

¹⁵See Appendix B.

balance within a household, and can be interpreted as an intra-generational distribution effect. As other studies on intra-generational distribution effects, this effect is caused by heterogeneity among individuals in the same generation, but that within the family. Because the pension expansion by an increase in τ leads women with higher longevity to a more favorable position, the sign of $\partial\theta/\partial\tau$ ($\epsilon_{\theta\tau}$) is positive. On the other hand, $\partial n/\partial\theta$ ($\epsilon_{n\theta}$) is negative because women want to reduce the number of children so that they can ensure resources in the retirement period, taking into account their higher probability to survive. Thus, overall, the second term is negative. The sign of the total effect of the change in τ on n^* , therefore, is not determined a priori. If the negative effect of an increase in pension size on fertility due to a change in bargaining power exceeds the positive effect of the increase in τ , then fertility is decreased by an increase in τ .

Now, we turn to the total effects of a change in τ on θ^* . The first term in (26) captures the direct positive effect of a change in τ on bargaining power by changing the gap of the pension benefit between wife and husband. The second term in (26) represents the indirect effect through a change in fertility caused by an increase in τ . The sign of $\partial\theta/\partial n$ ($\epsilon_{\theta n}$) depends on the relative magnitude of the effects of n on women's bargaining power as a result of reduced labor income and an increased pension benefit, as compared to that of their husbands. Consequently, the sign of the overall effect is determined by these direct and indirect effects.

5 Concluding Remarks

The family is the key constitutional unit of human society. It offers comfort, security, and a place to grow. However, the role and the structure of family change according to the influence of many factors, such as changing lifestyles and increasing personal mobility. Public policy is also a significant factor affecting the family shape. The decision on having children must be affected by the system of childcare leave, educational costs, and various family policies. The systems of taxation and social security are also factors that influence the way couples work and the balance of power within the family. Our paper can be placed as a variant on a line that examines the intra-familial structure, focusing on the balance of power and the number of children in the family.

There has been intense research into the effects of pension policy on the fertility. Most studies approach this matter using an overlapping generation (OLG) model with a unitary household, assuming no interaction between wife and husband. These studies are successful in analyzing long-run macroeconomic steady-state outcomes. At the same time, these standard approaches rely on some strong assumptions. In particular, they assume a unitary household with no heterogeneity in preferences or the lifespans of wives and husbands. This means they assume that a couple never bargains over household resource allocation, such as the number of children they have and/or the amount they save for the future. Approaching by different perspective from the orthodox homogeneous couple, to explore the effects of a public pension on the household resource allocation by the bargaining couple with heterogeneity is the principal subjects of this paper.

Following the trend of analyses on the heterogeneous couples, we also consider a setting with heterogeneity in the lifespan between husband and wife. The wife tends to live longer than her husband does, causing incentives for them to bargain over the amount of saving they do and the number of children they have. The bargaining power between wife and husband is endogenously determined in the social level based on their relative average lifetime income, including pension benefit. This is affected critically by a pension reform, which may in turn influence endogenous fertility. To demonstrate our results simply, we consider a small, open economy characterized by an exogenous interest rate and wages. The interest rate is the same for both the husband and wife, but the wage rate is not. Men tend to get a higher wage rate than the women, therefore the women often decide against participating in labor market.

Using this setup, this paper finds out a new channel of pension policy on fertility decisions. An increase in pension size affects not only via the changes in current and future incomes, but it affects the fertility through the change in marital bargaining power. The conventional OLG literature has always seen marital bargaining power as fixed, which meant that the increase in the pension benefit of the old accompanied by the tax increase in the young simply changes the lifetime income. As a result, this change in lifetime income caused by an increase in the pension size affects the household fertility behaviors. In our model, however, the development of a pension alters the marital relationship

defined by the gender gap in lifetime incomes, because the wife lives longer and is expected to gain higher amount of pension benefit. The change in the balance of power within the heterogeneous couple affects their saving behavior as well as their fertility. This results in the PAYG pension accelerating the falling birthrate, in contrast to the case of homogenous couples.

Appendices

Appendix A

Derivation of (15) and (16). From (13), we have

$$\frac{\partial \theta_{t+1}}{\partial \theta_t} = \frac{\theta' R^2 (w_f + w_m - \tau) A w_f z (\lambda_f - \lambda_m)}{\{w_f z [2 + \theta_t \lambda_f + (1 - \theta_t) \lambda_m] R - \tau\}^2}. \quad (27)$$

From (8) and (10), we have

$$n_t = \frac{R(w_f + w_m - \tau)}{w_f z [2 + \theta_t \lambda_f + (1 - \theta_t) \lambda_m] R - \tau}. \quad (28)$$

Substituting (28) into (27), we have (15).

The differentiation of (27) gives

$$\frac{\partial^2 \theta_{t+1}}{\partial \theta_t^2} = - \frac{2(\lambda_f - \lambda_m)^2 w_f^2 z^2 \theta' R^3 (w_f + w_m - \tau) A}{\{w_f z [2 + \theta_t \lambda_f + (1 - \theta_t) \lambda_m] R - \tau\}^3}. \quad (29)$$

Substituting (28) into (29), we (16).

Derivation of (21) and (22). From (18), we have

$$\begin{aligned} \frac{dn}{d\theta} &= - \frac{w_f z R^2 (\lambda_f - \lambda_m) (w_f + w_m - \tau)}{\{w_f z [2 + \theta \lambda_f + (1 - \theta) \lambda_m] R - \tau\}^2} < 0, \\ \frac{d^2 n}{d\theta^2} &= \frac{2z^2 w_f^2 (\lambda_f - \lambda_m)^2 R^3 (w_f + w_m - \tau)}{\{w_f z [2 + \theta \lambda_f + (1 - \theta) \lambda_m] R - \tau\}^3} > 0. \end{aligned}$$

(18) is rewritten as

$$2 + \theta \lambda_f + (1 - \theta) \lambda_m = \frac{R(w_f + w_m - \tau) + \tau n}{n w_f z R},$$

which is used to derive (21) and (22).

Derivation of (23). From (18), we have

$$\frac{\partial n}{\partial \tau} \Big|_{d\theta=0} = \frac{(w_f + w_m)R - (2 + \theta\lambda_f + (1 - \theta)\lambda_m)zw_fR^2}{(w_fz[2 + \theta\lambda_f + (1 - \theta)\lambda_m]R - \tau)^2}.$$

Substituting (18) into this equation, we have (23).

Appendix B

Derivation of (25) and (26). Fertility and bargaining power in the steady-state are given by total differentiation:

$$\begin{aligned} dn^* - \frac{\partial n}{\partial \theta} d\theta^* &= \frac{\partial n}{\partial \tau} d\tau, \\ -\frac{\partial \theta}{\partial n} dn^* + d\theta^* &= \frac{\partial \theta}{\partial \tau} d\tau. \end{aligned}$$

Using these equations, we have

$$\begin{bmatrix} 1 & -\partial n/\partial \theta \\ -\partial \theta/\partial n & 1 \end{bmatrix} \begin{bmatrix} dn^* \\ d\theta^* \end{bmatrix} = \begin{bmatrix} \partial n/\partial \tau \\ \partial \theta/\partial \tau \end{bmatrix} d\tau,$$

where the determinant of the coefficient matrix is $1 - (\partial n/\partial \theta)(\partial \theta/\partial n)$, which is reasonable to assume positive. Solving this, we have (25) and (26).

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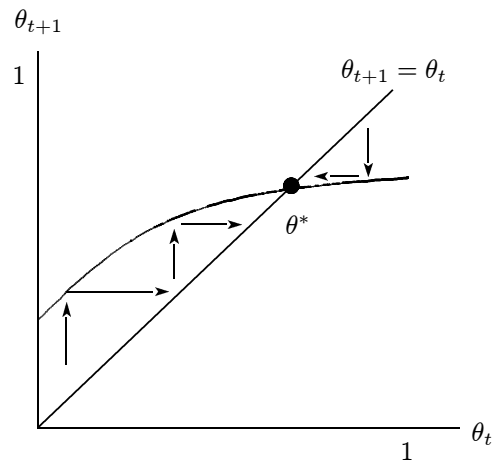


Figure 1(a). Steady-state bargaining power; $A > 0$.

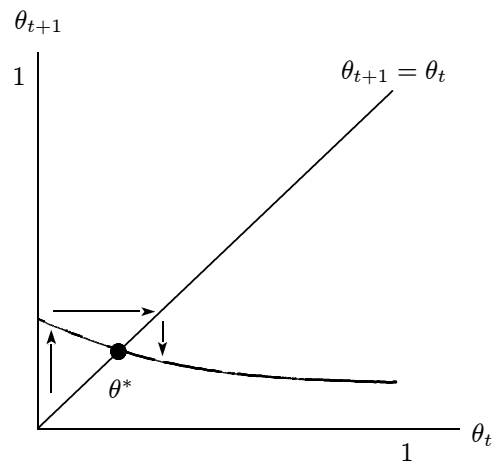


Figure 1(b). Steady-state bargaining power; $A < 0$.

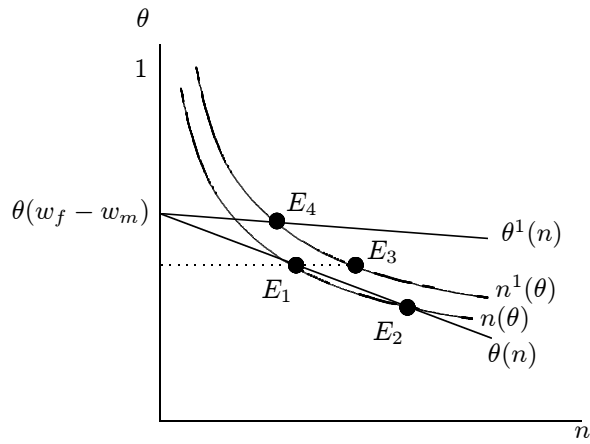


Figure 2(a). Effect of increase in τ when $R < n$ and the pension policy is inactive, $A > 0$.

Note. An increase in the size of pension policy shifts a stable equilibrium from E_1 to E_4 . E_2 is an unstable equilibrium.

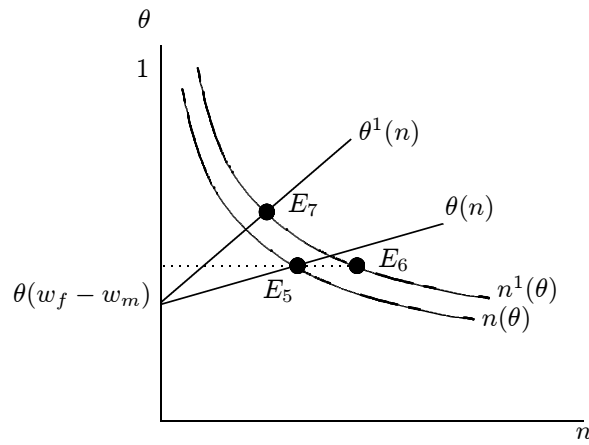


Figure 2(b). Effect of increase in τ when $R < n$ and the pension policy is active, $A < 0$.

Note. An increase in the size of pension policy shifts a stable equilibrium from E_5 to E_7 .

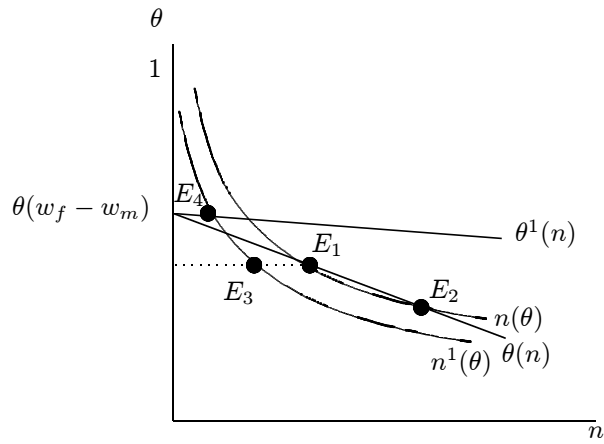


Figure 3(a). Effect of increase in τ when $R > n$ and the pension policy is inactive, $A > 0$.

Note. An increase in the size of pension policy shifts a stable equilibrium from E_1 to E_4 . E_2 is an unstable equilibrium.

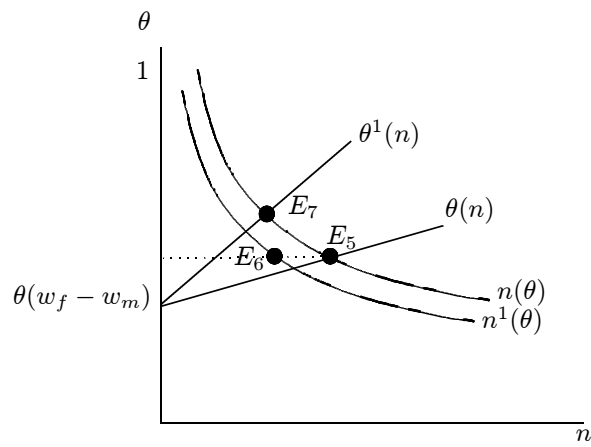


Figure 3(b). Effect of increase in τ when $R > n$ and the pension policy is inactive, $A < 0$.

Note. An increase in the size of pension policy shifts a stable equilibrium from E_5 to E_7 .